



COLLEGE OF
**NANOTECHNOLOGY,
SCIENCE, AND ENGINEERING**
UNIVERSITY AT ALBANY | STATE UNIVERSITY OF NEW YORK

*Mueller Matrix Spectroscopic Ellipsometry based
Scatterometry of Nanosheet Structures for GAA
Transistors using a Hybrid Metrology Approach*

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FCMN



- **Graduate Student Ezra Mel Pasikatan**

- **Scatterometry Funding from *ONTO Innovations / Discussions, etc.***
 - ▣ **Andy Antonelli**
 - ▣ **Nick Keller**

- **Discussions and XRD/XRR with Markus Kuhn of Rigaku**

- **Samples from TEL -- Dave Hetzer**
 - ▣ **Subhadeep Kal**
 - ▣ **Matthew Rednor**

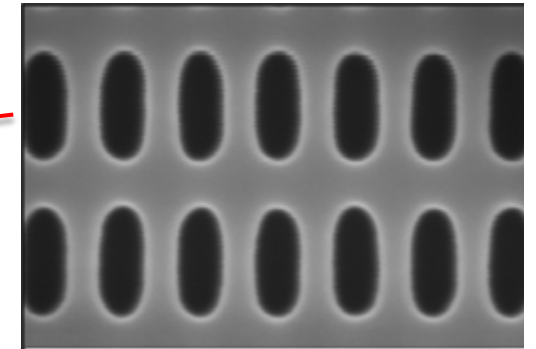
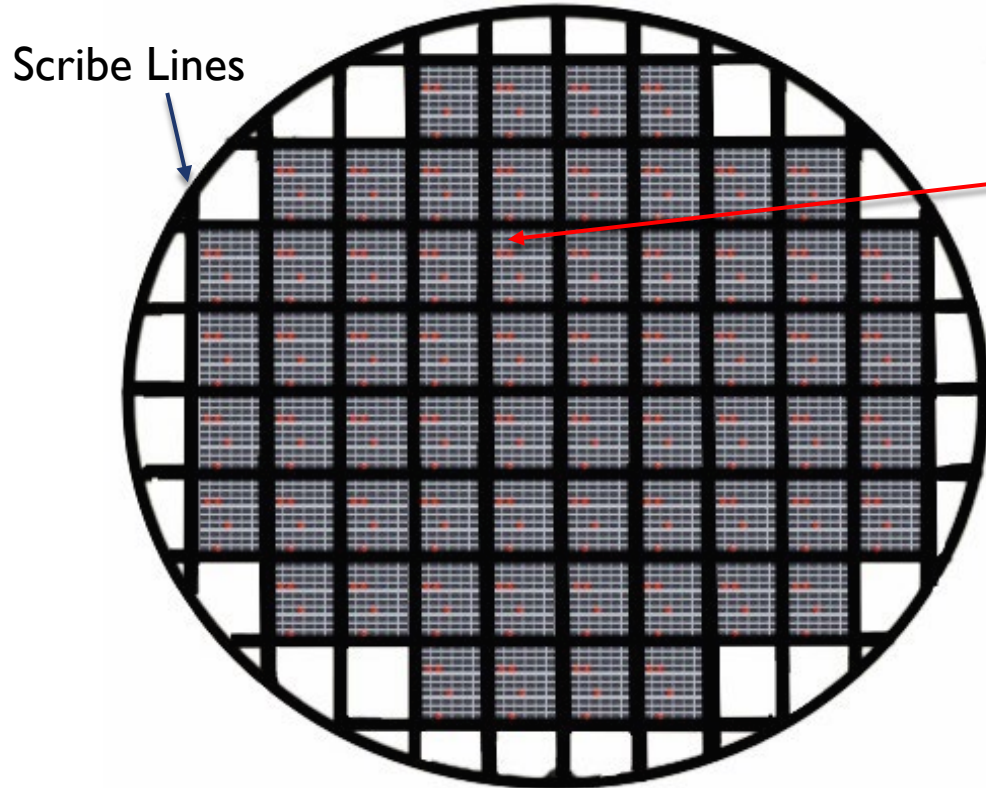


- ❑ **What is Scatterometry & Requirements for Scatterometry**
- ❑ **3D Structures, 3D Devices, and Nanoscale Materials**
- ❑ **X-Ray Characterization**
- ❑ **MMSE-Scatterometry**
- ❑ **3D Nanowire Test Structures**
- ❑ **Conclusions**



Lithography Metrology via Scatterometry

Determine feature shape and dimension changes in a grating test structure with measurements sites for each die in scribe line or in-die



In-Line Ellipsometer

Multiple wafers/hour

Multiple sites/wafer



Capable of Wafer Mapping



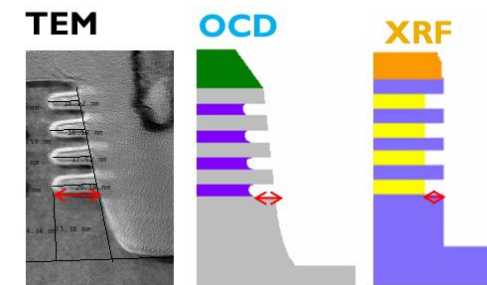
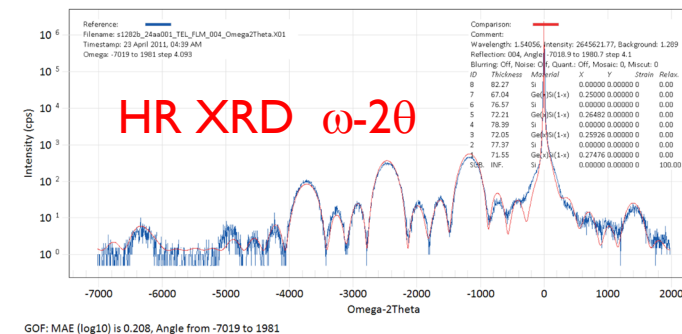
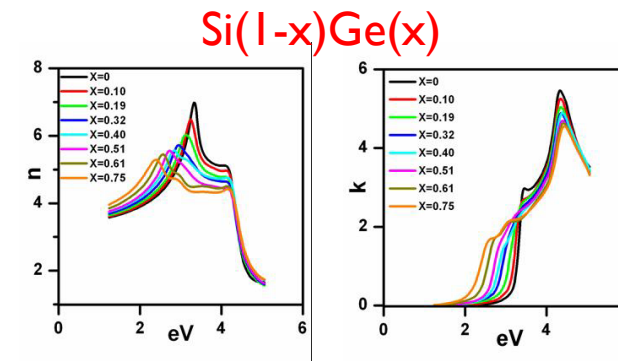
As practiced in the semiconductor industry scatterometry is used to rapidly characterize feature shape and structure of test structures:

- ❑ Spectroscopic Ellipsometer – measures grating test structure representative of structure of interest at *multiple areas across the wafer*.
- ❑ Model structure & vary a specific set of features using simulation.
- ❑ Data analyzed using Rigorous Coupled Wave Analysis solution to Maxwell's Equations
 - ❑ Often done by finding a best match from a library of simulations
 - ❑ Sometimes done by finding best fit simulation



What is Needed for Scatterometry ?

- Optical Properties of Fabricated Materials
 - Most process materials have different properties than standard materials –especially dielectric films
- Reference Measurements to assure film stack and structure shape and dimensions
 - TEM/STEM & XRD/XRR
- Ultimately – a Hybrid approach to account for across wafer variation
 - XRD/XRR/XRF & TEM/STEM & Scatterometry





- **S. Zollner**
- **Optical Properties and Band Structure of Unstrained and Strained Si_{1-x}Ge_x and Si_{1-x-y}Ge_xC_y alloys**
- **CH 12 in Silicon-Germanium Alloys Growth Properties and Applications**
- Eds. S.T. Pantelides and **S. Zollner**, Vol 15, *Optoelectronic Properties of Semiconductors and Superlattices*, Ed. M.O. Manasreh, (Taylor and Francis, N.Y., 2002), 387.

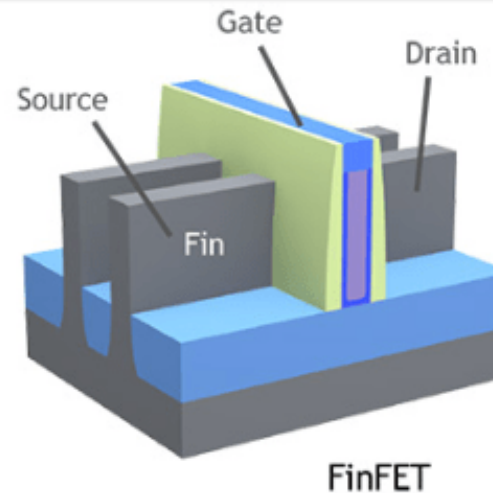
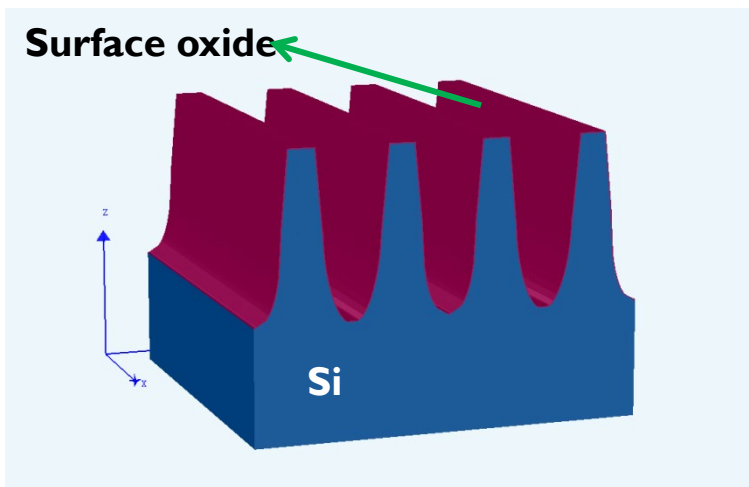


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- ❑ **3D Nanowire Test Structures**
- ❑ **Conclusions**



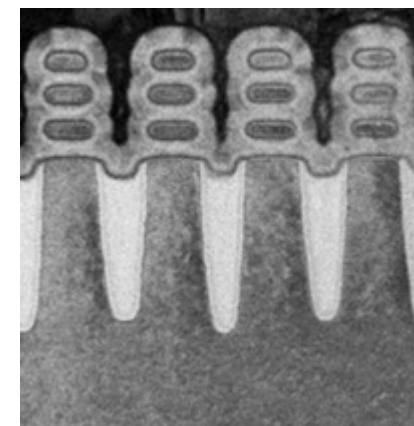
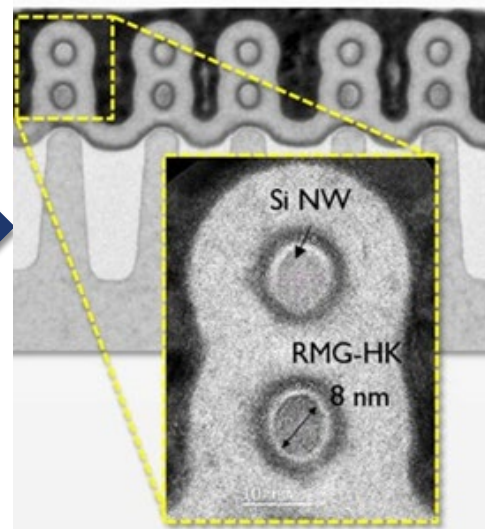
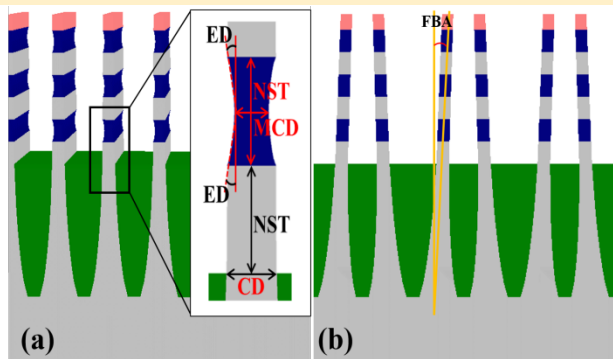
Today 14 nm to < 5 nm FinFETs to Nanowire/sheet FETs

FinFET



**Fins fabricated from
a Superlattice of Si/SiGe**

NanoWire /
NanoSheet
FET





- ❑ **What is Scatterometry & Requirements for Scatterometry**
- ❑ **3D Structures, 3D Devices, and Nanoscale Materials**
- ❑ **X-Ray Characterization** (Intro to Pseudomorphic $\text{Si}_{1-x}\text{Ge}_x$)
- ❑ **MMSE-Scatterometry**
- ❑ **3D Nanowire Test Structures**
- ❑ **Conclusions**

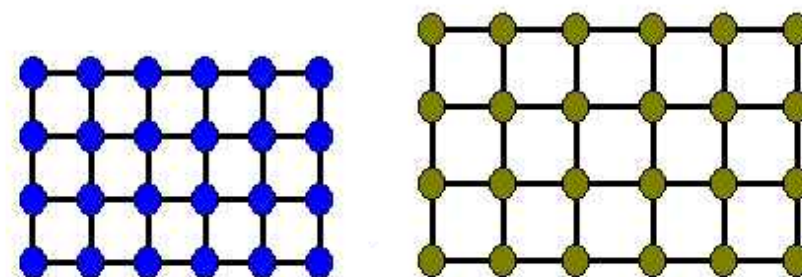


Strained Silicon - Germanium

Silicon and Germanium lattice constants differ by more than 4 %.

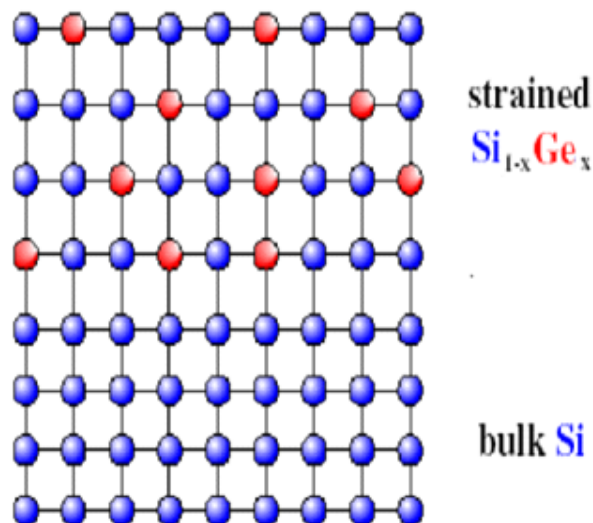
$\text{Si}_{1-x}\text{Ge}_x$ has a larger lattice than that of Silicon

$\text{Si}_{1-x}\text{Ge}_x$ undergoes bi-axial stress to match Silicon's in-plane lattice.



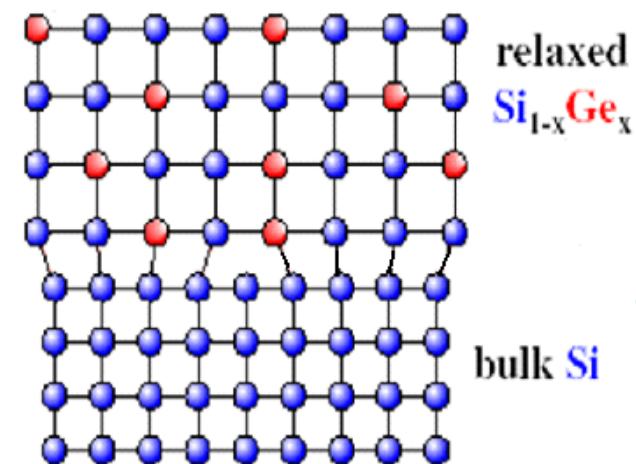
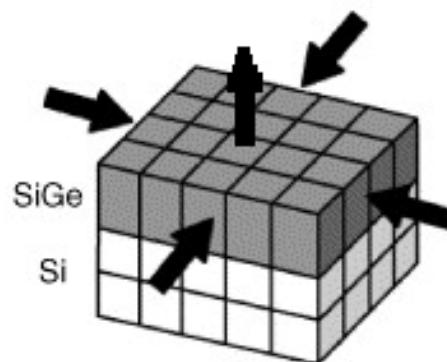
Bulk (relaxed)
Si

Bulk (relaxed)
SiGe



strained
 $\text{Si}_{1-x}\text{Ge}_x$

bulk Si



relaxed
 $\text{Si}_{1-x}\text{Ge}_x$

bulk Si



□ First we consider a single layer of $\text{Si}_{1-x}\text{Ge}_x$ on Si



Superlattice Effects on XRD

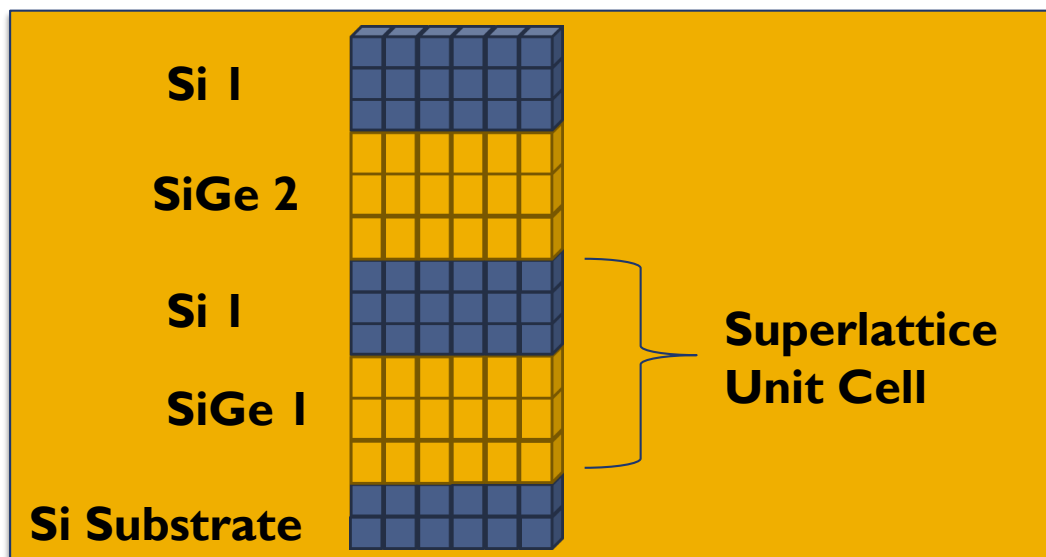
- Superlattice structure results in diffraction from main SiGe Peak
- Si/SiGe Bilayer can be considered a large unit cell

$$F_{hkl} = \sum_{j=1}^N f_j e^{[-2\pi i(hx_j + ky_j + lz_j)]},$$

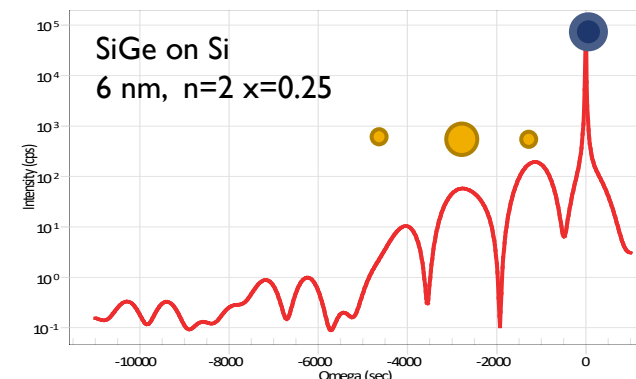
Single Unit Cell

$$F_H = \sum_j^N f_j \exp(-2\pi \mathbf{H} \cdot \mathbf{r}_j)$$

Large Unit Cell
Structure Factor



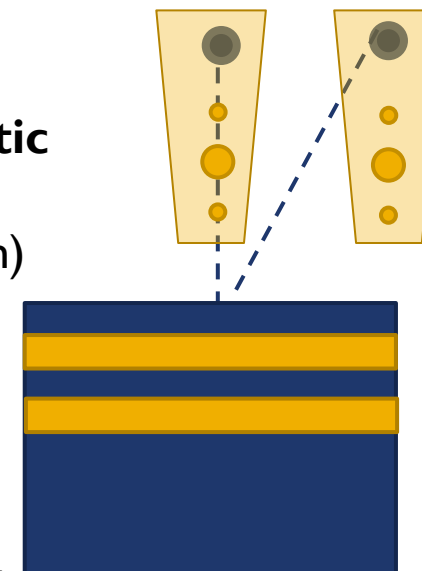
004 $\omega - 2\theta$ scan



004

224

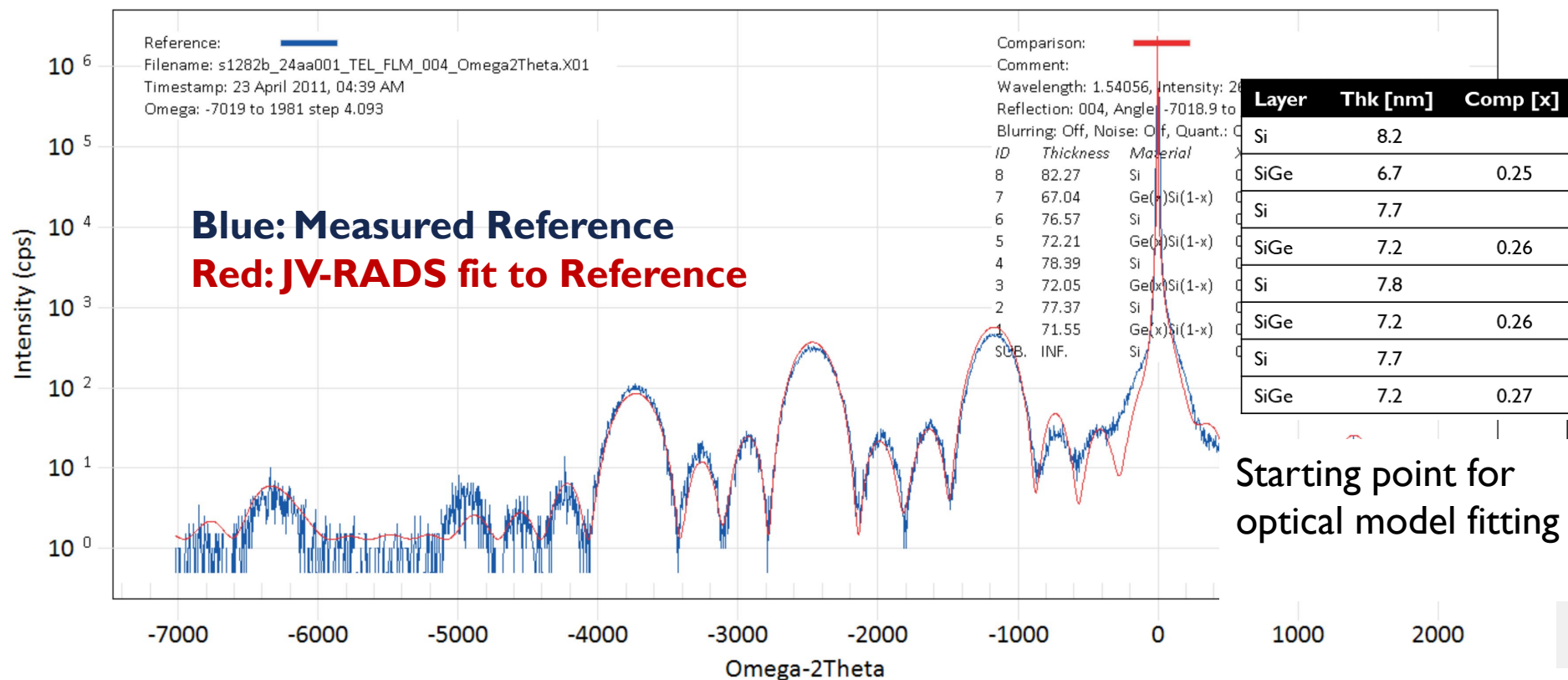
RSM
Schematic
(Strained
Condition)





XRD $\omega - 2\theta$: Thickness & Composition Results

- Scanning $\omega - 2\theta$ around Si (004) shows SiGe peak at expected angular offset
- Two additional peaks are due to the superlattice effect (repeating Si/SiGe layers)

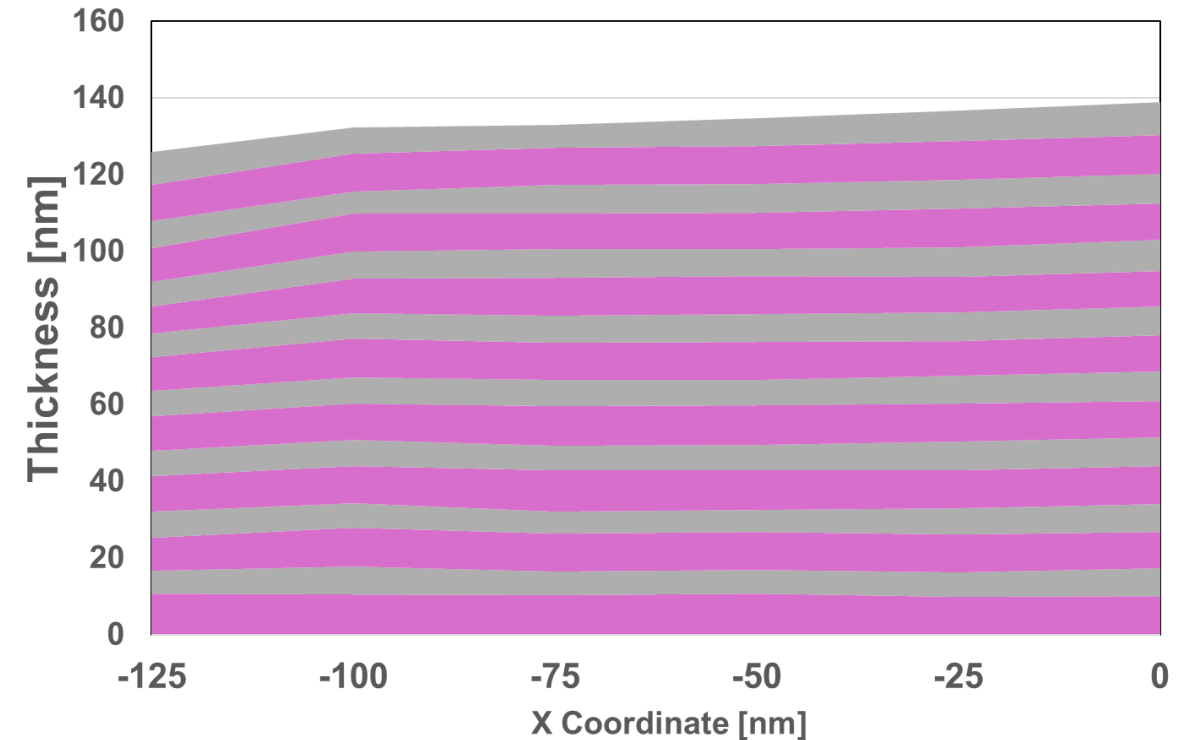
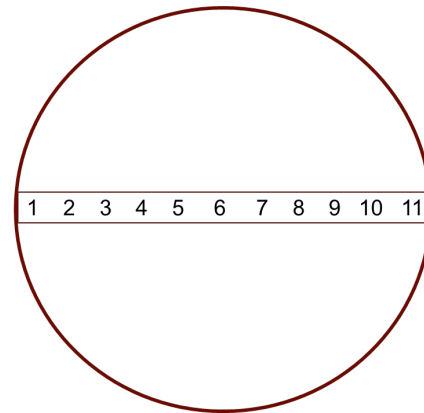
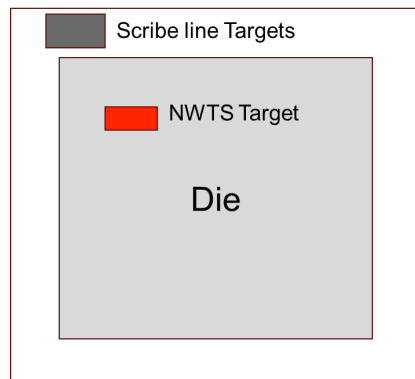
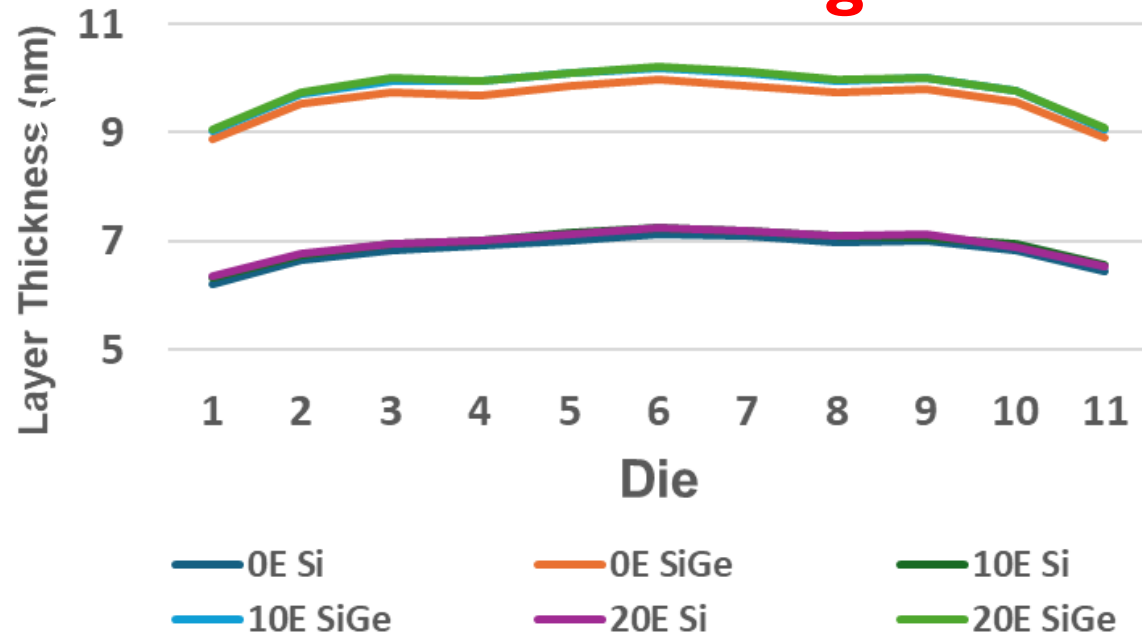


GOF: MAE (log10) is 0.208, Angle from -7019 to 1981



8X superlattice Film Variation

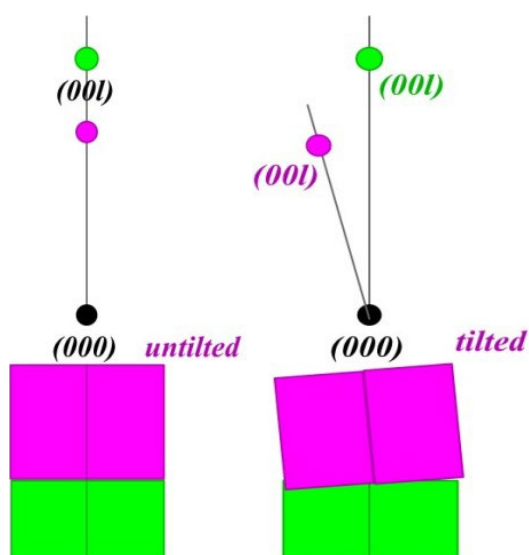
Average HR-XRD Layer Thickness



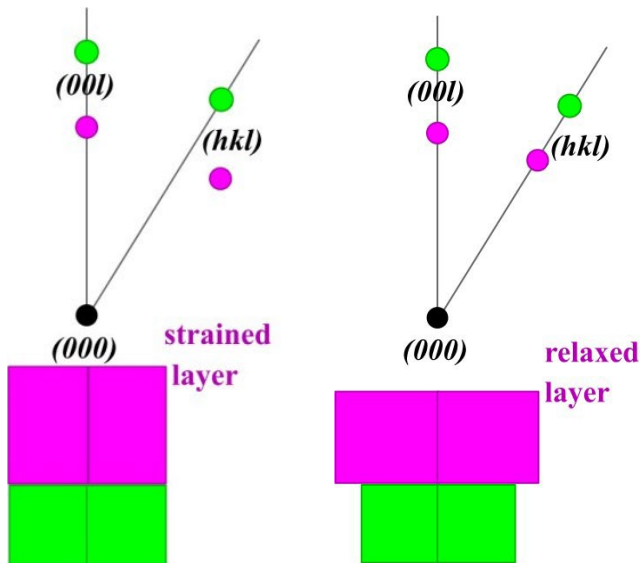
Magnified view of area for Dies 1 to 6



- A scan around a reciprocal lattice point (rlp) provides good interpretation of the structure of a material
- Any relaxation/tilt on the layers with respect to the substrate is shown as a peak shift away from the substrate peak.

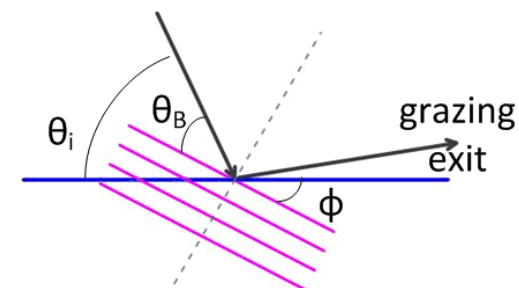


**Symmetric scans to
determine tilt of the layer**



**Asymmetric scans to determine
relaxation in the layer**

- Grazing Incidence $\theta_i = \theta_B - \phi$
- Grazing Exit $\theta_i = \theta_B + \phi$



Grazing Exit 224 $\phi = \sim 35.3^\circ$



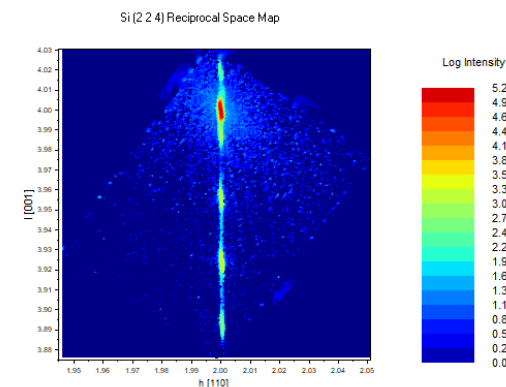
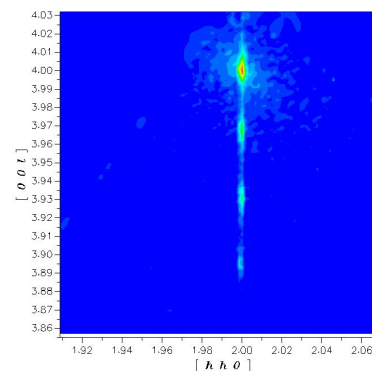
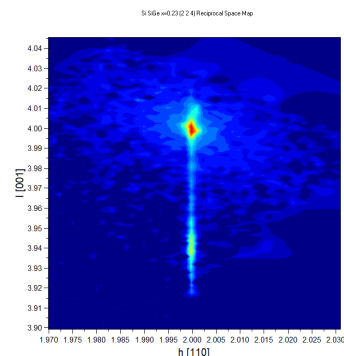
- No relaxation of superlattice layers

**Single SiGe
Epilayer on Si
 $X=0.23$
52.9 nm**

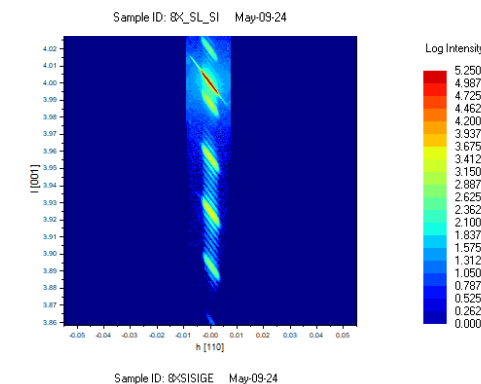
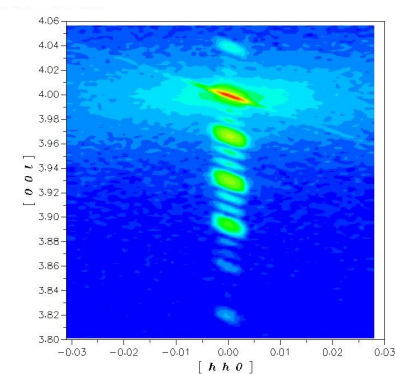
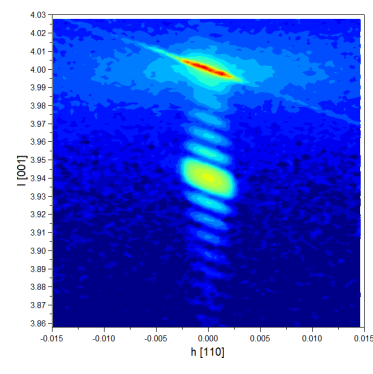
**Superlattice
4 Layer Si/SiGe
 $X \sim 0.25$
6 nm**

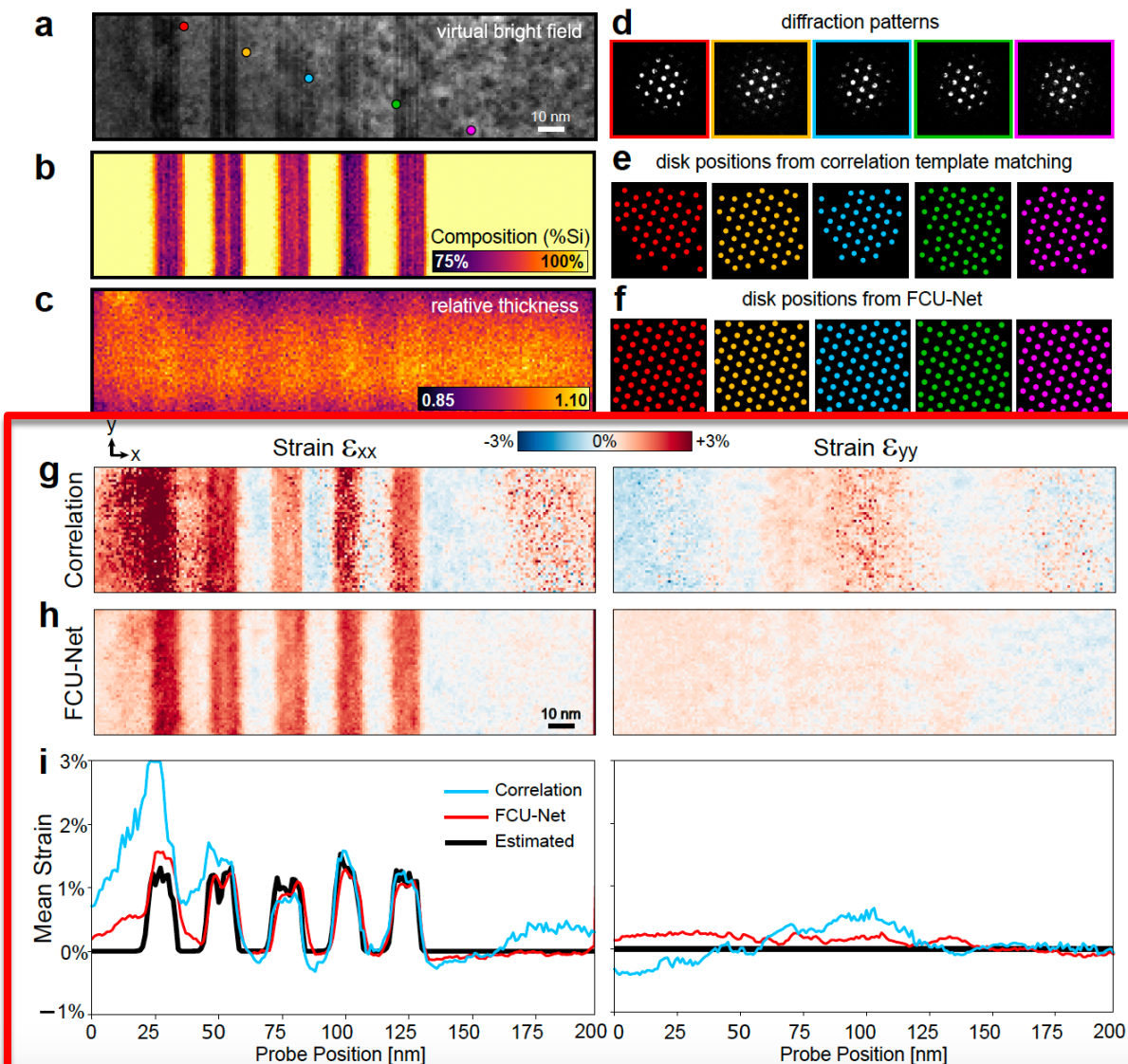
**Superlattice
8 Layer Si/SiGe
 $X \sim 0.25$
< 10 nm**

224 RSM



004 RSM





Analysis of experimental
CBED strain data using
(*Fourier-space complex U
net (FCU-Net) deep neural
network*

X direction is perpendicular to
the layer interfaces

*Si/Si(1-x)Ge(x) with $x=0.13$
(?). Here, strain refers
difference from Si lattice.*

Munshi, J., *et al.*

Disentangling multiple scattering with
deep learning: application to strain
mapping from electron diffraction
patterns.

npj Comput Mater **8**, 254 (2022).

<https://doi.org/10.1038/s41524-022-00939-9>



- Reference Measurements for Si(1-x)Ge(x)/Si superlattice spectroscopic ellipsometry
 - ▣ ω -2 θ coupled scans and RSM limited to < 32 layers for transistor stacks – see specifics in J. Micro/Nanopattern. Mater. Metrol. 23, (2024), 044004.
 - ▣ Need multiple TEM/STEM measurements per wafer
- For Nanowire test structures (next part of presentation), the SiN hard mask roughness limits ellipsometry measurement of Si(1-x)Ge(x)/Si superlattice



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Scatterometry / Ellipsometry of Grating Structures

- Inline optical metrology tool for critical dimension (CD) measurement for advanced process control. Fast, accurate & non-destructive.

- Diffraction from a periodic grating.

- **Optical simulator is used to generate the optical response for the structure of interest (Forward problem) and regression based or library based approach is used to extract the feature dimensions/additional information (Reverse problem).**

$$S = \begin{bmatrix} s_0 \\ s_1 \\ s_2 \\ s_3 \end{bmatrix} = \begin{bmatrix} I_x + I_y \\ I_x - I_y \\ I_{\pi/4} - I_{-\pi/4} \\ I_{LCP} - I_{RCP} \end{bmatrix}$$

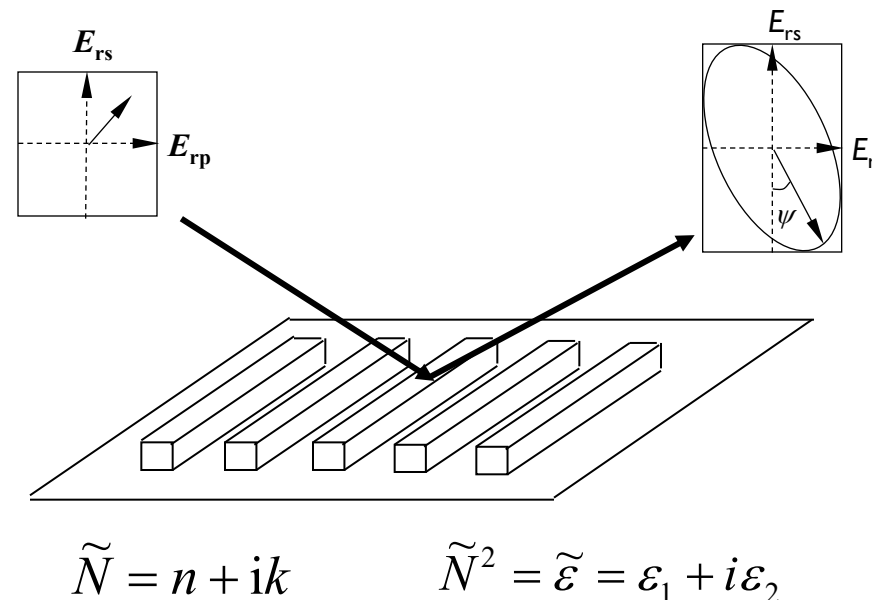
Optical Response

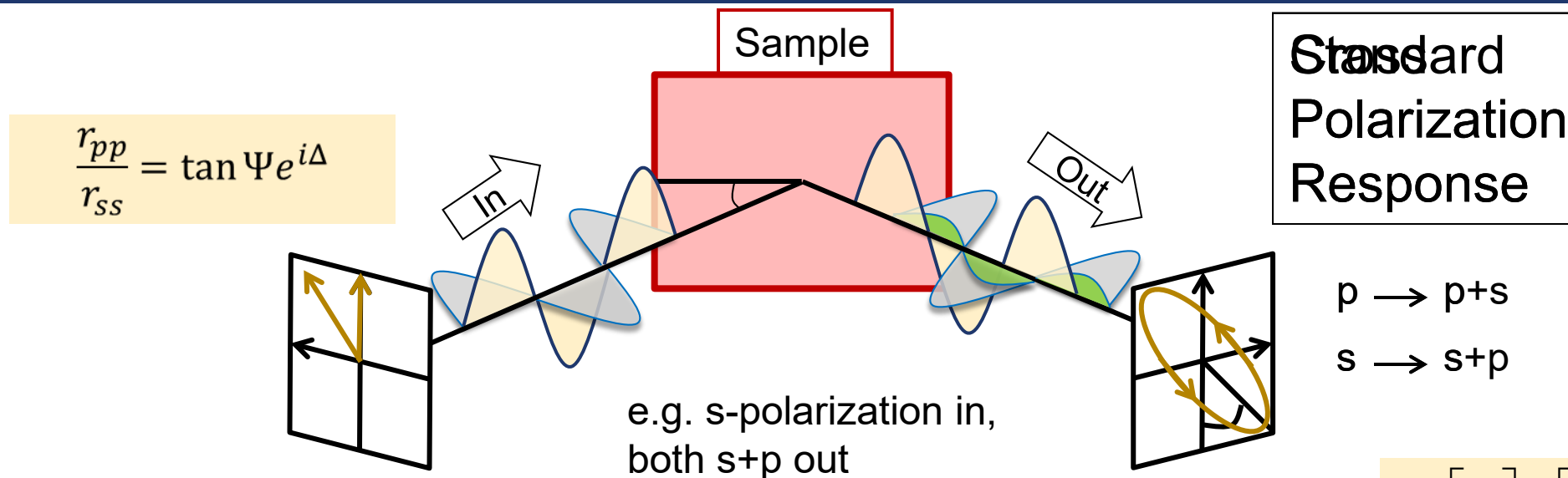
$$\tan \Psi e^{j\Delta} = \frac{R^p}{R^s}$$

Ellipsometric Response

$$\begin{bmatrix} S_{0,\text{out}} \\ S_{1,\text{out}} \\ S_{2,\text{out}} \\ S_{3,\text{out}} \end{bmatrix} = \begin{bmatrix} M_{11} & M_{12} & M_{13} & M_{14} \\ M_{21} & M_{22} & M_{23} & M_{24} \\ M_{31} & M_{32} & M_{33} & M_{34} \\ M_{41} & M_{42} & M_{43} & M_{44} \end{bmatrix} \begin{bmatrix} S_{0,\text{in}} \\ S_{1,\text{in}} \\ S_{2,\text{in}} \\ S_{3,\text{in}} \end{bmatrix}$$

Mueller Response





- Isotropic samples
 - Refractive indices of thin films lack spatial dependence
 - Thus, no azimuthal dependence or cross-polarization
- Anisotropic structures
 - Patterned surfaces result in spatially varying refractive indices
 - Thus, azimuthal dependence reflects sample symmetry

$$S = \begin{bmatrix} s_0 \\ s_1 \\ s_2 \\ s_3 \end{bmatrix} = \begin{bmatrix} I_x + I_y \\ I_x - I_y \\ I_{\pi/4} - I_{-\pi/4} \\ I_{LCP} - I_{RCP} \end{bmatrix}$$

$$\begin{bmatrix} s_{0,out} \\ s_{1,out} \\ s_{2,out} \\ s_{3,out} \end{bmatrix} = \begin{pmatrix} M_{11} & M_{12} & M_{13} & M_{14} \\ M_{21} & M_{22} & M_{23} & M_{24} \\ M_{31} & M_{32} & M_{33} & M_{34} \\ M_{41} & M_{42} & M_{43} & M_{44} \end{pmatrix} \begin{bmatrix} s_{0,in} \\ s_{1,in} \\ s_{2,in} \\ s_{3,in} \end{bmatrix}$$



Dual Rotating Compensator Ellipsometer (RC2)

$$S = \begin{bmatrix} S_0 \\ S_1 \\ S_2 \\ S_3 \end{bmatrix} = \begin{bmatrix} I_x + I_y \\ I_x - I_y \\ I_{\pi/4} - I_{-\pi/4} \\ I_{LCP} - I_{RCP} \end{bmatrix} \quad \text{Stokes Vector}$$

System Mueller Matrix

$$\begin{bmatrix} S_{0,out} \\ S_{1,out} \\ S_{2,out} \\ S_{3,out} \end{bmatrix} = \begin{bmatrix} M_{11} & M_{12} & M_{13} & M_{14} \\ M_{21} & M_{22} & M_{23} & M_{24} \\ M_{31} & M_{32} & M_{33} & M_{34} \\ M_{41} & M_{42} & M_{43} & M_{44} \end{bmatrix} \begin{bmatrix} S_{0,in} \\ S_{1,in} \\ S_{2,in} \\ S_{3,in} \end{bmatrix}$$

Rotation Mueller Matrix

$$\text{RM} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos 2\alpha & \sin 2\alpha & 0 \\ 0 & -\sin 2\alpha & \cos 2\alpha & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$\begin{bmatrix} S_{0,in} \\ S_{1,in} \\ S_{2,in} \\ S_{3,in} \end{bmatrix}$$

$$\text{RM} \frac{1}{2} \begin{bmatrix} 1 & 1 & 0 & 0 \\ 1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix} \text{RM} \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & \cos \delta & \sin \delta \\ 0 & 0 & -\sin \delta & \cos \delta \end{bmatrix}$$

Sample MM

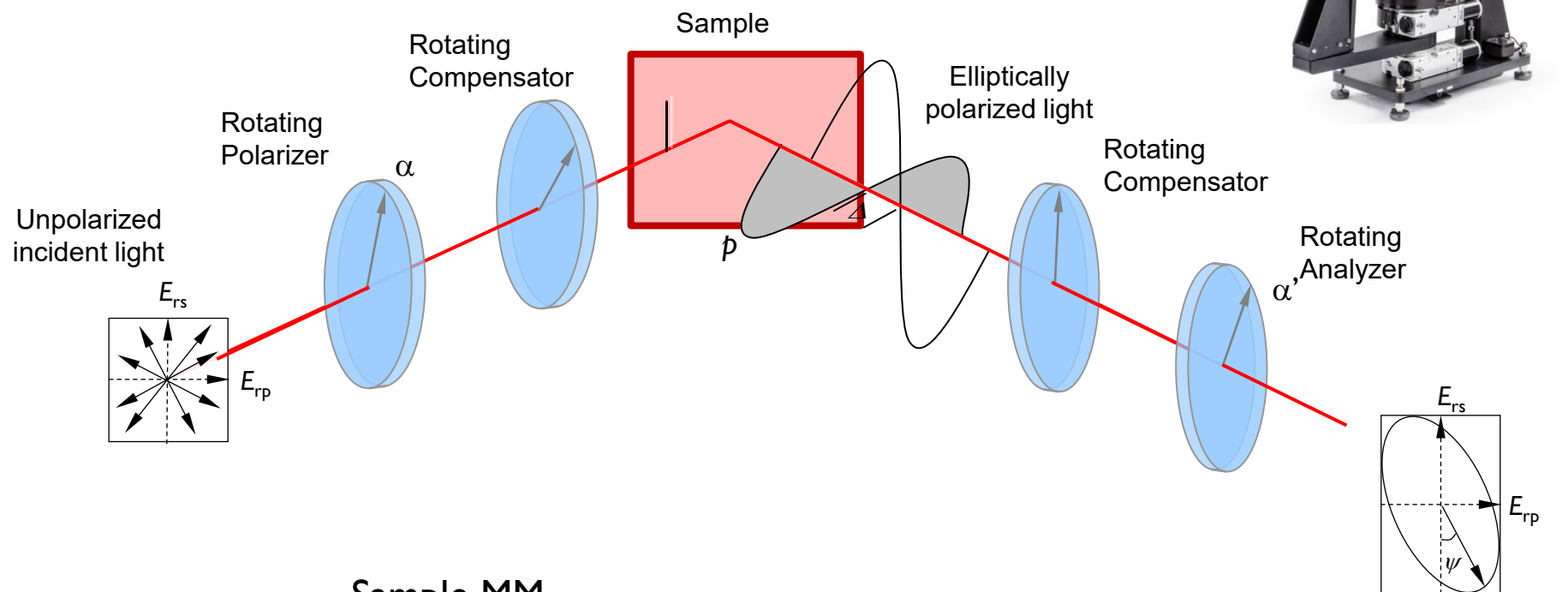
$$\begin{bmatrix} M_{11} & M_{12} & M_{13} & M_{14} \\ M_{21} & M_{22} & M_{23} & M_{24} \\ M_{31} & M_{32} & M_{33} & M_{34} \\ M_{41} & M_{42} & M_{43} & M_{44} \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & \cos \delta & \sin \delta \\ 0 & 0 & -\sin \delta & \cos \delta \end{bmatrix}$$

$$\text{RM} \frac{1}{2} \begin{bmatrix} 1 & 1 & 0 & 0 \\ 1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

$$\text{RM} = \begin{bmatrix} S_{0,out} \\ S_{1,out} \\ S_{2,out} \\ S_{3,out} \end{bmatrix}$$

Laboratory Ellipsometer Great for All Types of Samples





Post-normalization

Anisotropic, generalizing

$$M = \begin{pmatrix} M_{11} & M_{12} & M_{13} & M_{14} \\ M_{21} & M_{22} & M_{23} & M_{24} \\ M_{31} & M_{32} & M_{33} & M_{34} \\ M_{41} & M_{42} & M_{43} & M_{44} \end{pmatrix} = \begin{pmatrix} 1 & -N - \alpha_{sp} & C_{sp} + \zeta_1 & S_{sp} + \zeta_2 \\ -N - \alpha_{ps} & 1 - \alpha_{sp} - \alpha_{ps} & -C_{sp} + \zeta_1 & -S_{sp} + \zeta_2 \\ C_{ps} + \xi_1 & -C_{ps} + \xi_1 & C_{pp} + \beta_1 & S_{pp} + \beta_2 \\ -S_{ps} + \xi_2 & S_{ps} + \xi_2 & -S_{pp} - \beta_2 & C_{pp} - \beta_1 \end{pmatrix}$$

- Matrix contains complete optical response of a sample
- Symmetry reduces number of independent elements
- 15 distinct elements in general

$$D = 1 + \tan^2(\psi_{pp}) + \tan^2(\psi_{ps}) + \tan^2(\psi_{sp})$$

$$N = \frac{1 - \tan^2(\psi_{pp}) - \tan^2(\psi_{ps}) - \tan^2(\psi_{sp})}{D}$$

$$C_{ij} = \frac{2 \tan(\psi_{ij}) \cos \Delta_{ij}}{D}$$

$$S_{ij} = \frac{2 \tan(\psi_{ij}) \sin \Delta_{ij}}{D}$$

$$\alpha_{ij} = \frac{2 \tan^2(\psi_{ij})}{D}$$

$$\zeta_i = \frac{D (C_{ps}^2 + S_{ps}^2 (-1)^{i+1 \bmod 2})}{2}$$

$$\xi_i = \frac{D (C_{sp}^2 + S_{sp}^2 (-1)^{i+1 \bmod 2})}{2}$$

$$\beta_i = \frac{D (C_{sp} C_{ps} + S_{sp} S_{ps} (-1)^{i+1 \bmod 2})}{2}$$

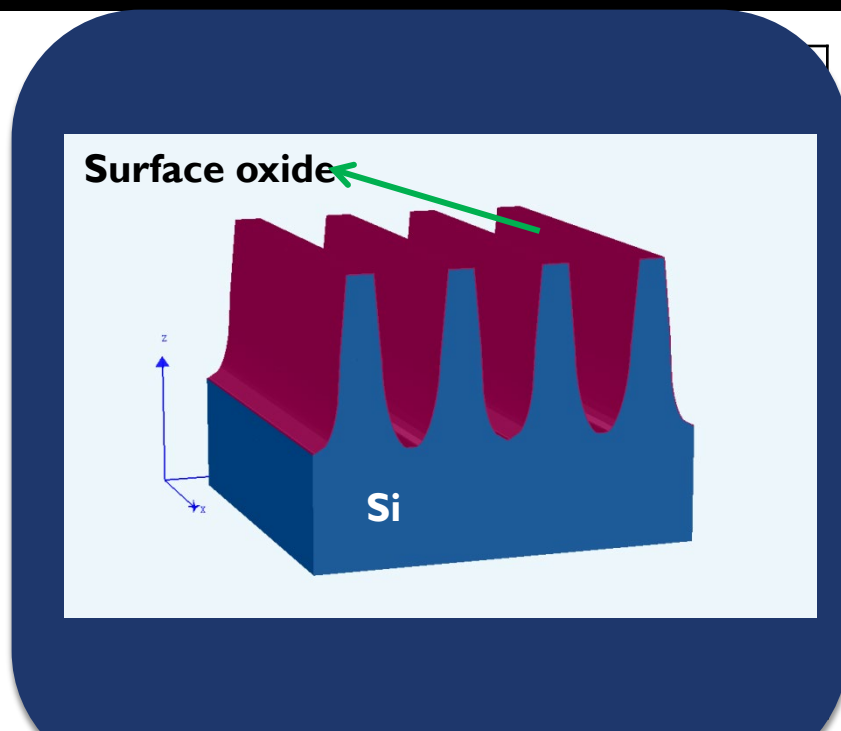


Mueller Matrix Basics

Symmetric (Ideal) Grating

$$M = \begin{pmatrix} M_{11} & M_{12} & M_{13} & M_{14} \\ M_{21} & M_{22} & M_{23} & M_{24} \\ M_{31} & M_{32} & M_{33} & M_{34} \\ M_{41} & M_{42} & M_{43} & M_{44} \end{pmatrix} = \begin{pmatrix} 1 & -N - \alpha_{sp} & C_{sp} + \zeta_1 & S_{sp} + \zeta_2 \\ -N - \alpha_{ps} & 1 - \alpha_{sp} - \alpha_{ps} & -C_{sp} + \zeta_1 & -S_{sp} + \zeta_2 \\ C_{ps} + \xi_1 & -C_{ps} + \xi_1 & C_{pp} + \beta_1 & S_{pp} + \beta_2 \\ -S_{ps} + \xi_2 & S_{ps} + \xi_2 & -S_{pp} - \beta_2 & C_{pp} - \beta_1 \end{pmatrix}$$

$M_{13}+M_{31}$ and $M_{14}-M_{41}$ non zero = sample asymmetry



M_{11}	M_{12}	M_{13}	M_{14}
M_{12}	M_{22}	M_{23}	M_{24}
$-M_{13}$	$-M_{23}$	M_{33}	M_{34}
M_{14}	M_{24}	$-M_{34}$	M_{44}



Rigorous Coupled Wave Approximation (RCWA)

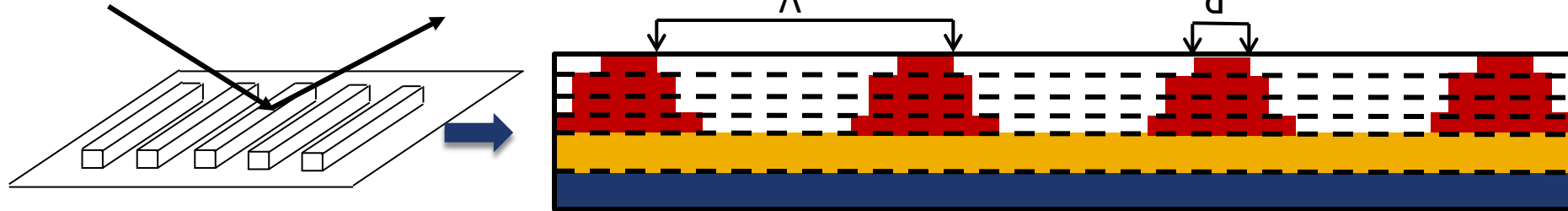
- Approximate full Fourier series for dielectric function

$$\varepsilon(x) = \sum_{n=-N}^N \varepsilon_n e^{i2\pi nx/\Lambda}$$

- Slice structure into stack of layers, coefficients determined:

$$\varepsilon_{n=0} = \varepsilon_{\text{line}} d / \Lambda + \varepsilon_{\text{space}} (1 - d / \Lambda)$$

$$\varepsilon_{n \neq 0} = (\varepsilon_{\text{line}} - \varepsilon_{\text{space}}) \sin(n\pi d / \Lambda) / n\pi$$



- Solve Maxwell's equations for incident TE and TM polarized waves

$$H = \left(\frac{i}{\omega\mu} \right) \nabla \times E$$

$$E = \left(\frac{i}{\omega\mu n^2} \right) \nabla \times H$$

- Equations cast in Matrix Form

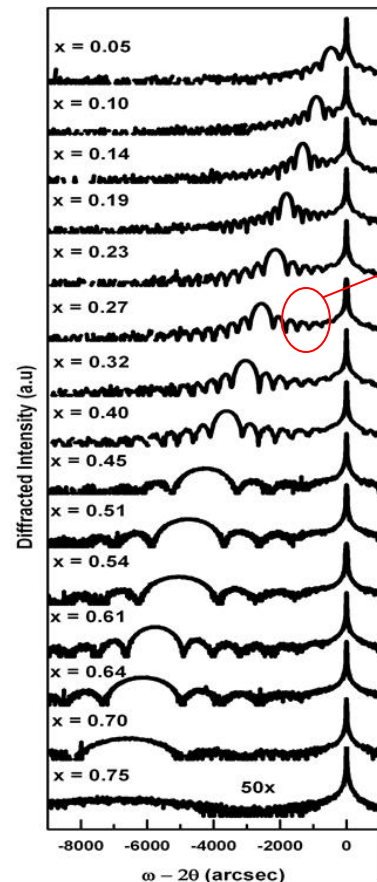


- Semi – Analytical Form of Maxwell's Equations in Fourier Space
- Transform only in-plane (x and y) and have a uniform layer in z
- Transform Maxwell's equations into a computer solvable matrix form
- Alternate name: Transfer matrix method with a plane wave basis

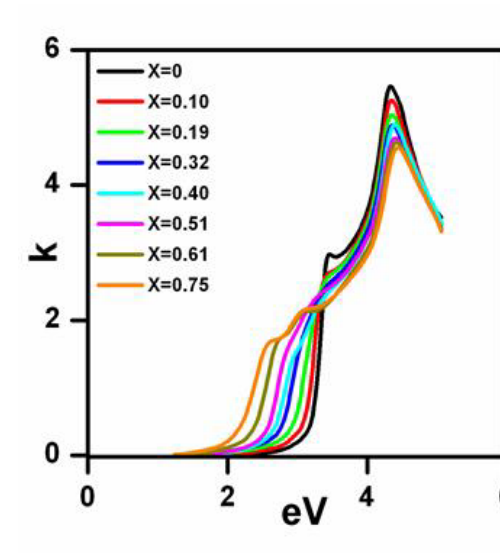
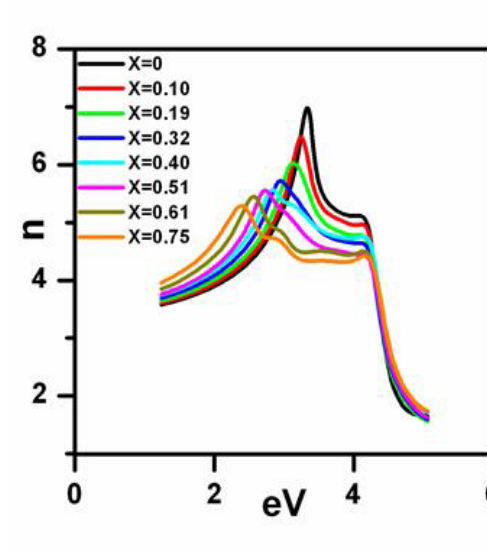
See **EM Possible** - [Implementation of 3D RCWA in MATLAB](#)



Reference Method – HR-XRD (example $\text{Si}_{1-x}\text{Ge}_x/\text{Si}$)



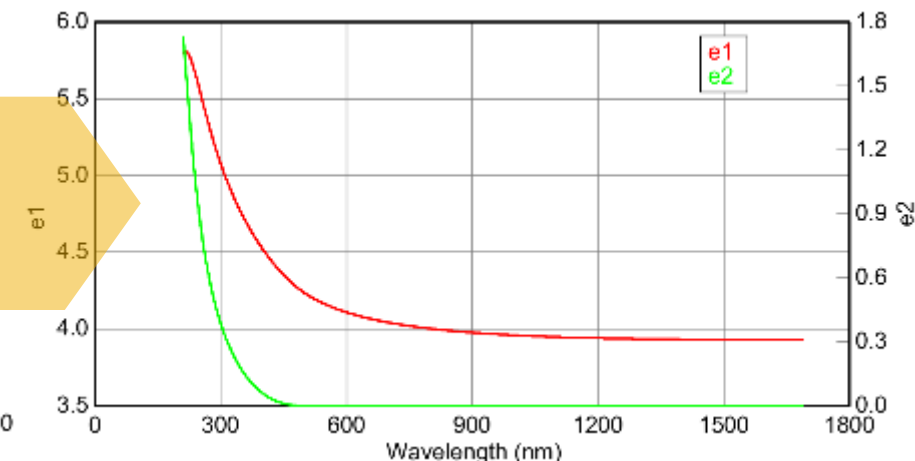
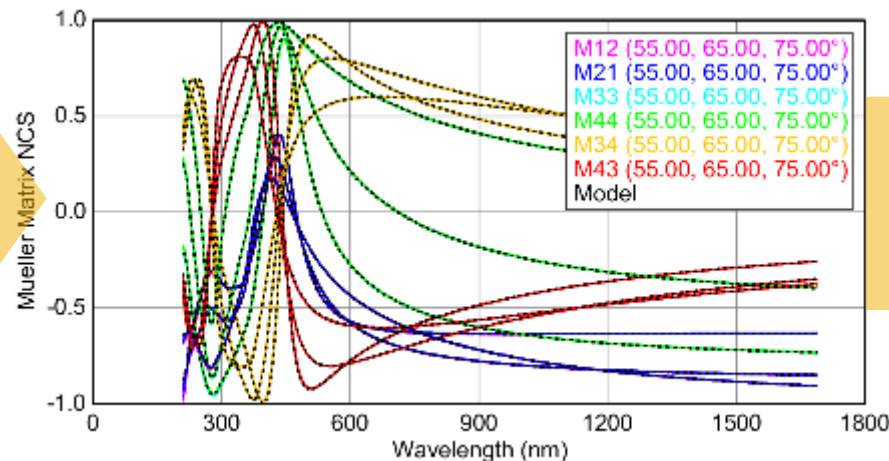
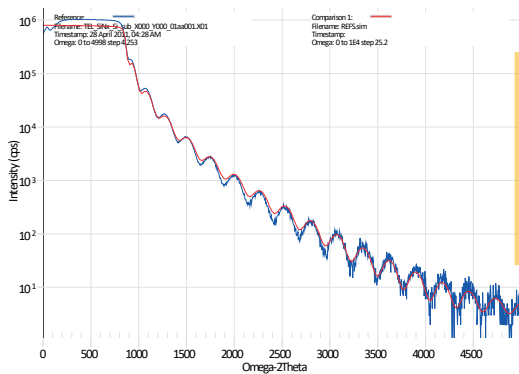
$$\frac{\text{Thickness}}{\lambda} = \frac{2\Delta\omega_{\text{fringes}} \cos\theta_B}{\lambda}$$





Optical Properties of SiN Hard Mask

- SiN_x film optical properties are dependent on process conditions
- Deposited SiN_x film on Si substrate deposited at the same process conditions superlattice stack
- Derived material file based on XRR thickness and SE data





4X superlattice Si/Si(1-x)Ge(x) w/< 10nm films

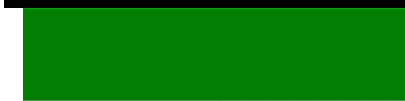
- XRD thickness based fits improve MSE slightly compared to floating avg Si and SiGe SE fits
- EMA (Effective Medium Approximation) improves the fit by modeling the stack as a mix of Si and SiGe properties
- EDC (Effective Dielectric Constant) improved the model further by determining the dielectric constant for the layer set wavelength by wavelength

Superlattice Fit Strategy	Fix thk. based on XRD	Avg. Si and SiGe thk.	Superlattice EMA	Superlattice EDC
SiN Roughness [nm]	3.00	2.66	0.26	0.00
SiN Hardmask [nm]	47.96	47.90	48.23	48.30
Si [nm]	8.06	7.15		
Si(1-x)Ge(x) [nm]	6.74 (x=0.29)	6.08 (x=0.27)		
Si [nm]	8.02	7.15		
Si(1-x)Ge(x) [nm]	6.99 (x=0.27)	6.08 (x=0.27)	58.57	60.93
Si [nm]	8.12	7.15		
Si(1-x)Ge(x) [nm]	6.33 (x=0.27)	6.08 (x=0.27)		
Si [nm]	8.09	7.15		
Si(1-x)Ge(x) [nm]	6.55 (x=0.26)	6.08 (x=0.27)		
MSE	15.941	16.883	10.788	3.64

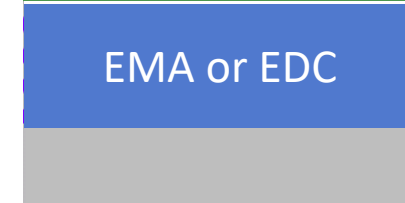
Standard Superlattice



EMA/EDC approx

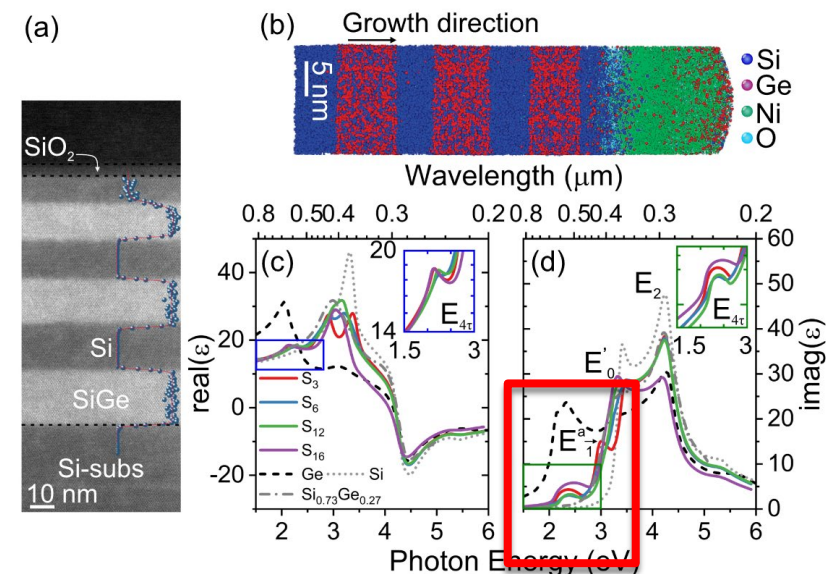
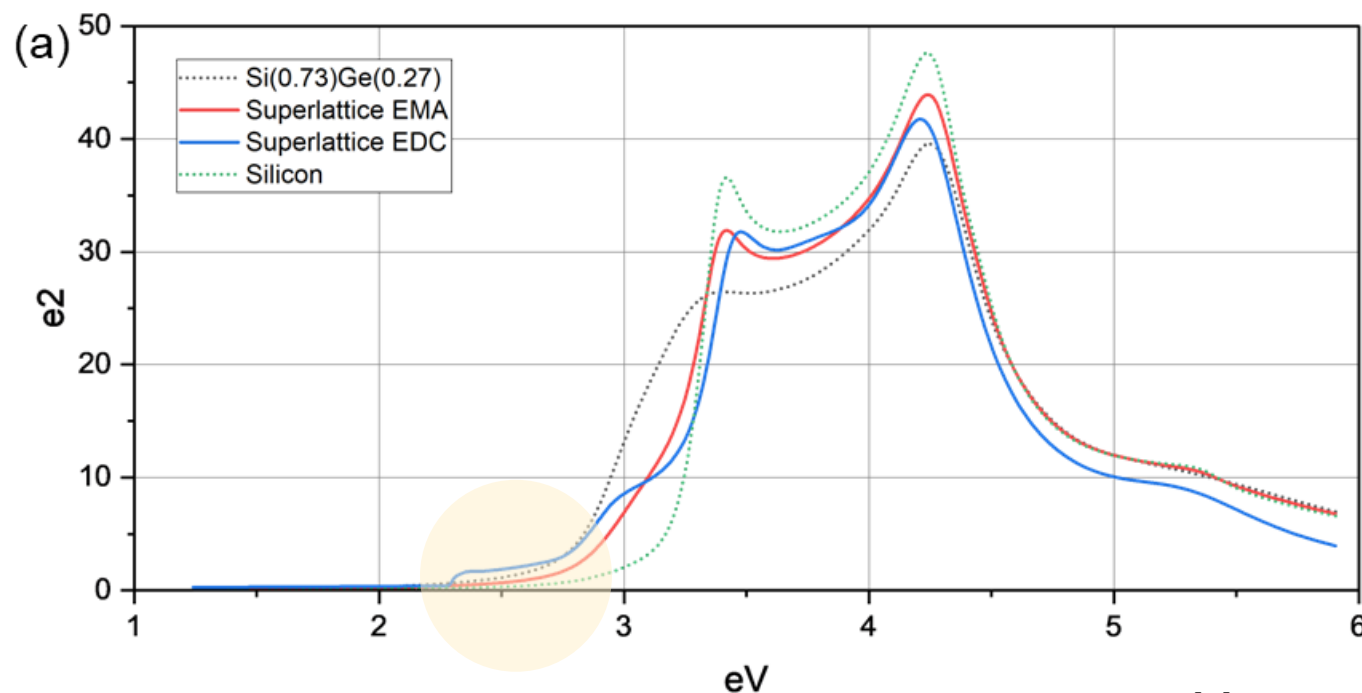


EMA or EDC

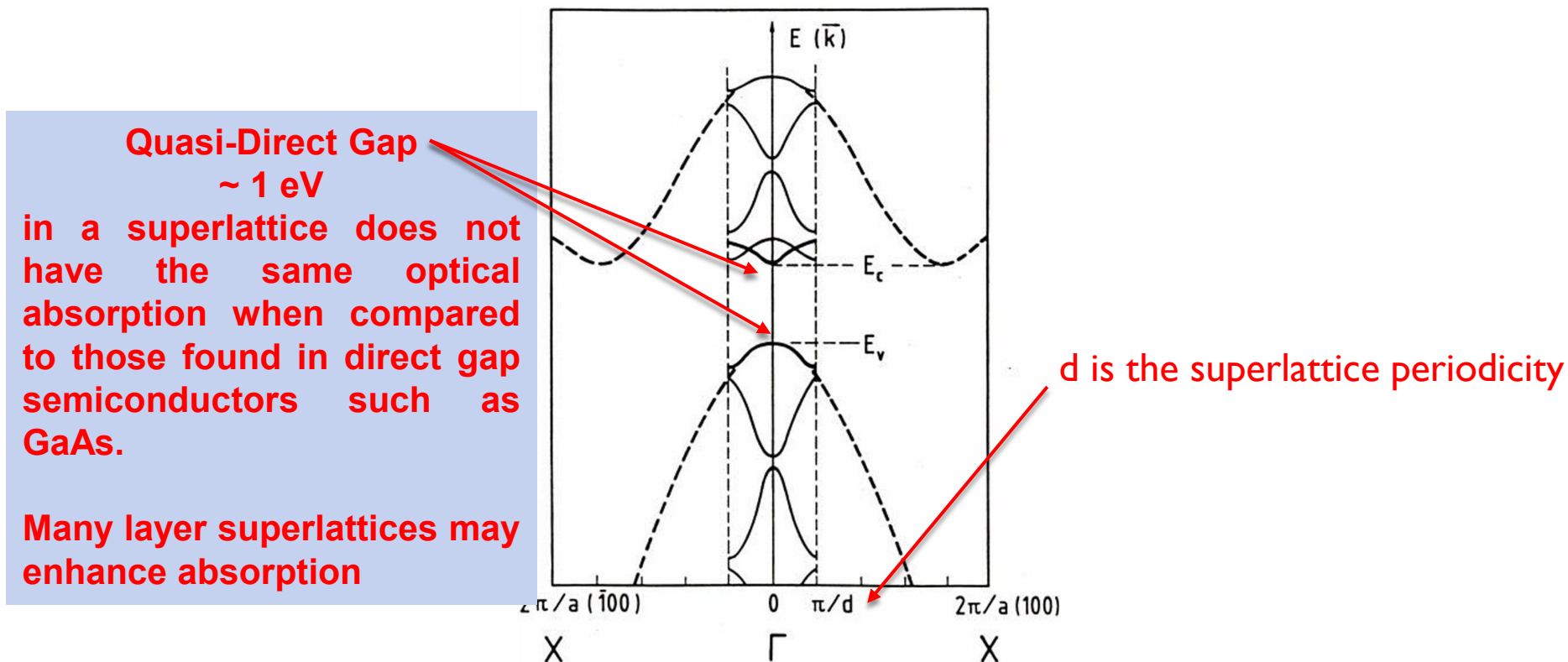




- Extra absorption feature observed at 2.4 eV indicates the *interfacial* superlattice properties affect the effective dielectric constant (EDC)
- Observed broadening in 4-layer SL is similar to Attiaoui 2022 result



[1] A. Attiaoui et al., "Electronic Signature of Subnanometer Interfacial Broadening in Heterostructures," Nano Lett. **22**(17), 7080–7086 (2022)
[doi:[10.1021/acs.nanolett.2c02042](https://doi.org/10.1021/acs.nanolett.2c02042)].



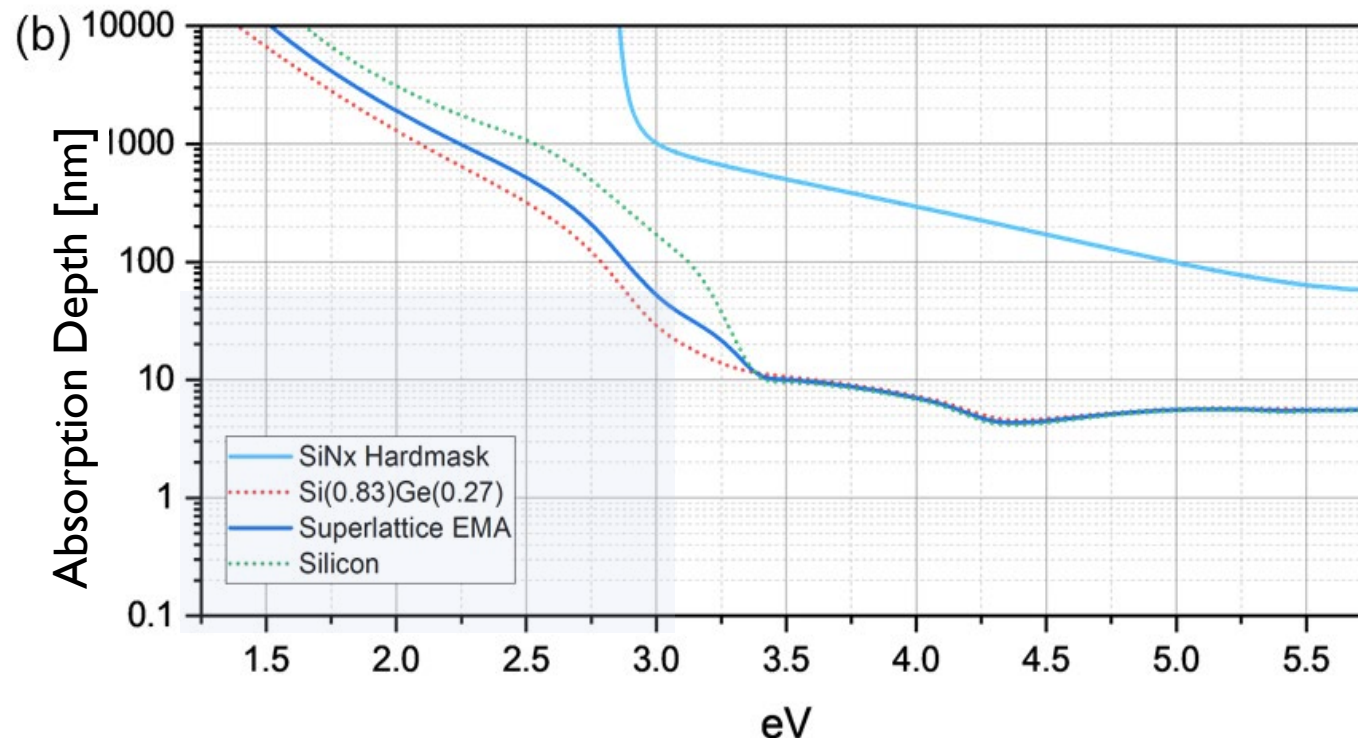
Schematic representation of the Brillouin zone-folding concept in Si resulting from the new superlattice periodicity in the growth direction.

Here, the conduction band minimum along the X direction is folded back into the Γ point when the superlattice period is about 10 monolayers of Si (Kasper and Schäffler, 1991).

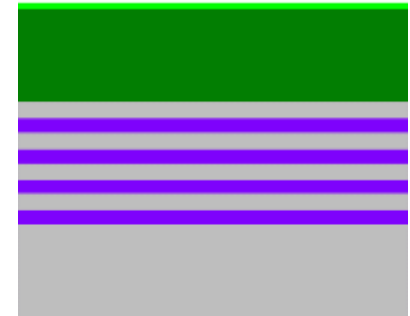


Absorption Depth

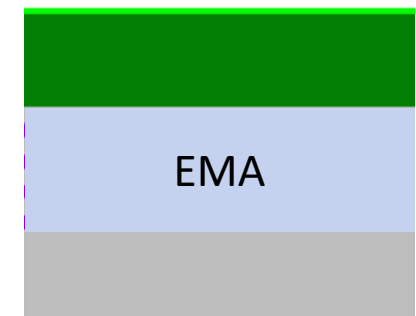
- Absorption depth can be estimated using the Effective Medium Approximation model for Si/Si(0.75)Ge(0.25) based on
- Significant absorption of current 56 nm n=4 stacks occurs below 3 eV
- Absorption will be more significant for thicker future logic and 3D DRAM film stacks



Standard Superlattice



Effective Medium Approximation (EMA) Model



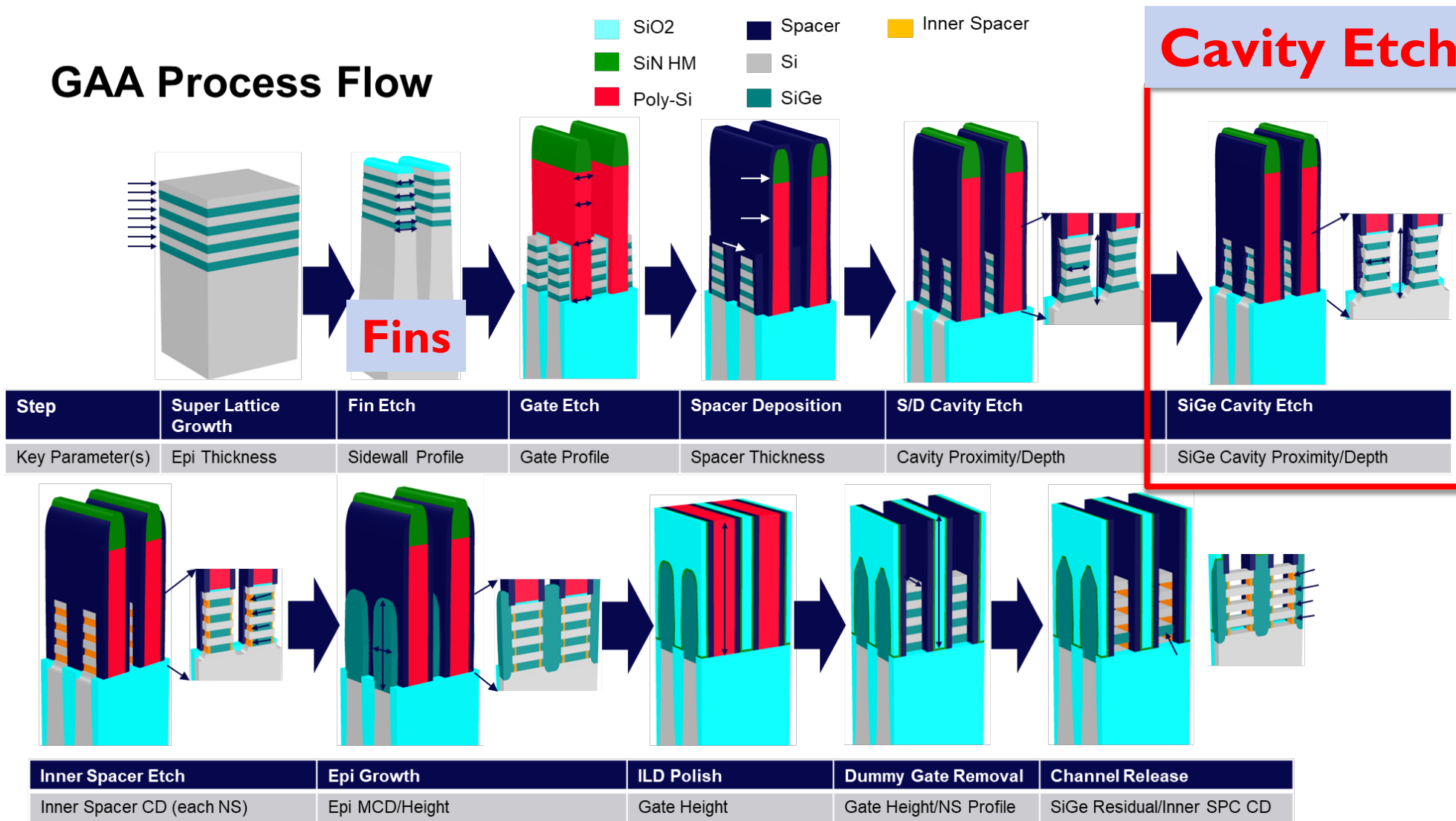


- ❑ **What is Scatterometry & Requirements for Scatterometry**
- ❑ **3D Structures, 3D Devices, and Nanoscale Materials**
- ❑ **X-Ray Characterization**
- ❑ **MMSE-Scatterometry**
- ❑ **3D Nanowire Test Structures**
- ❑ **Conclusions**



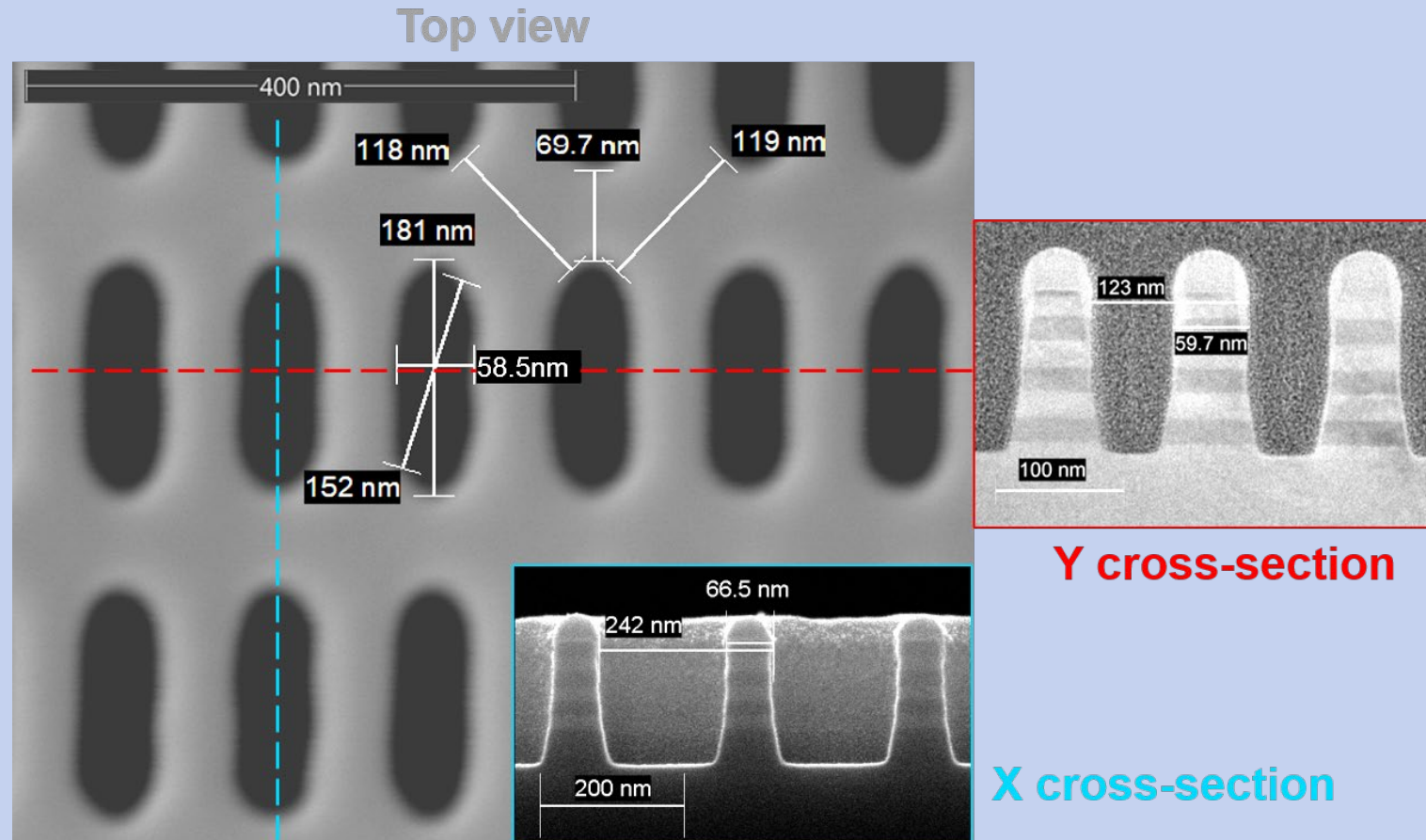
Gate All Around Transistor Process Flow

GAA Process Flow





Nanowire Test Structure





Nanowire Test Structure

Nanowire Test Structures(NWTS) structure based on STEM

Materials:

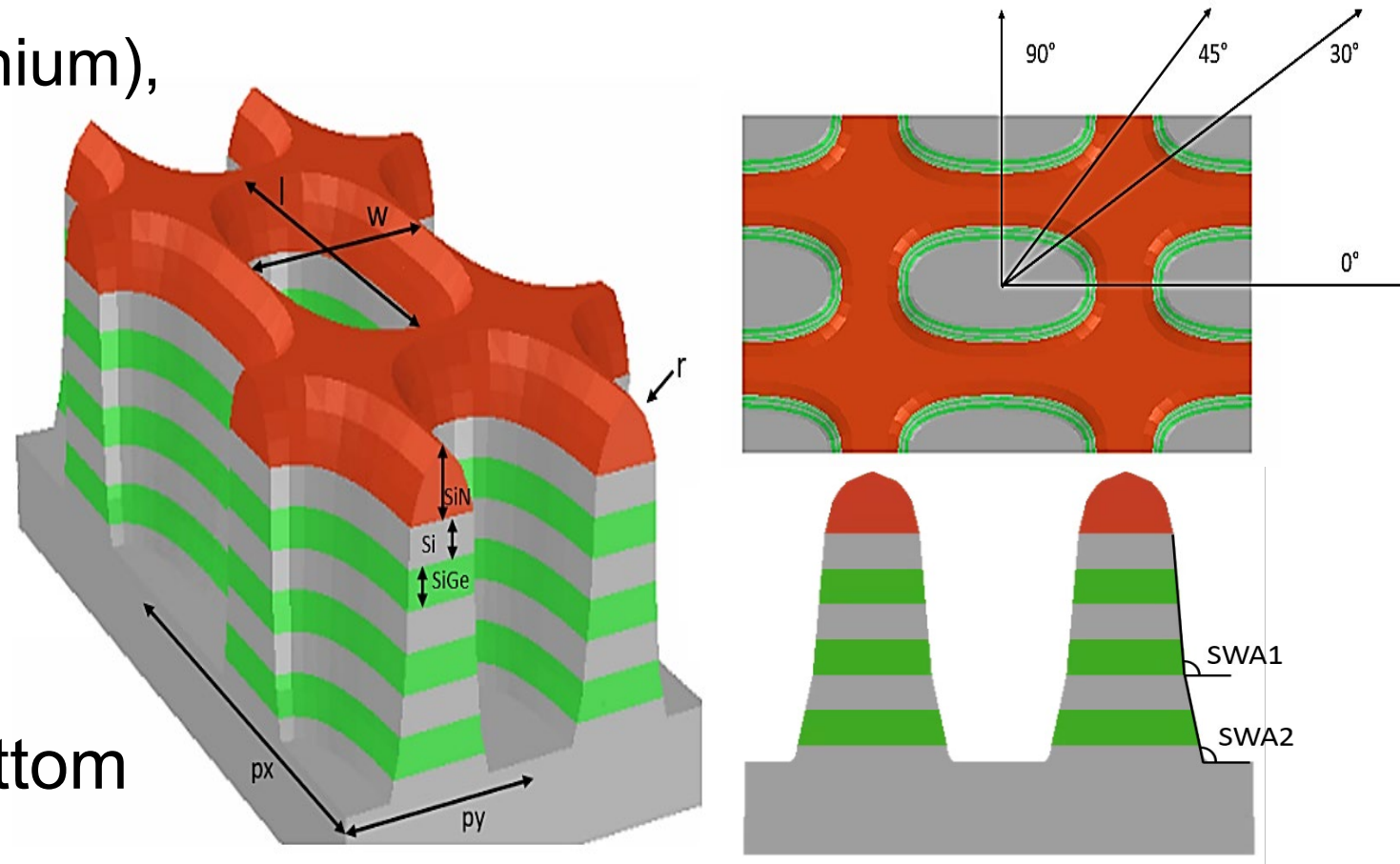
- Si, SiGe (20% - 28% Germanium), SiN

Parameters:

- X pitch – 240nm
- Y pitch – 120nm

Hole dimensions:

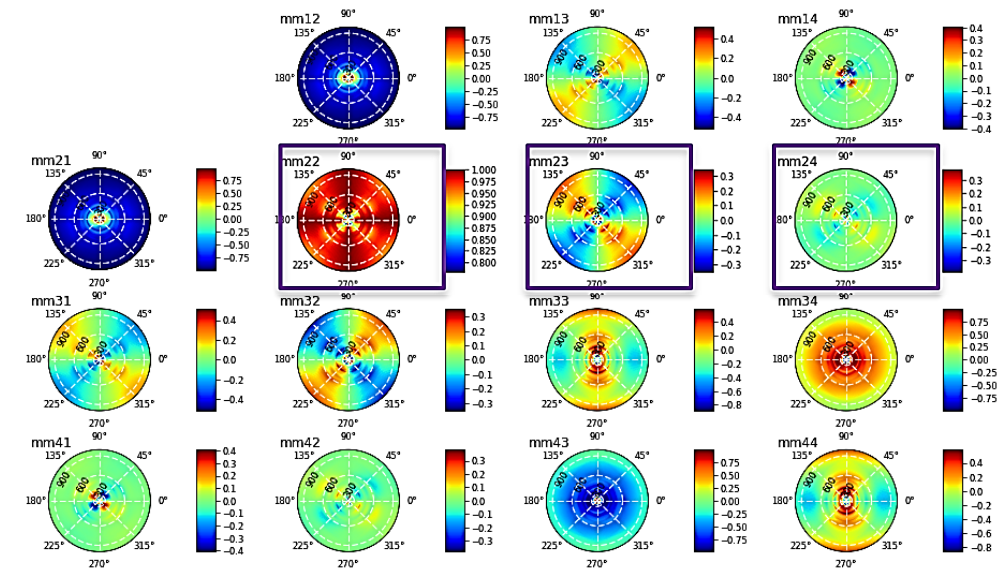
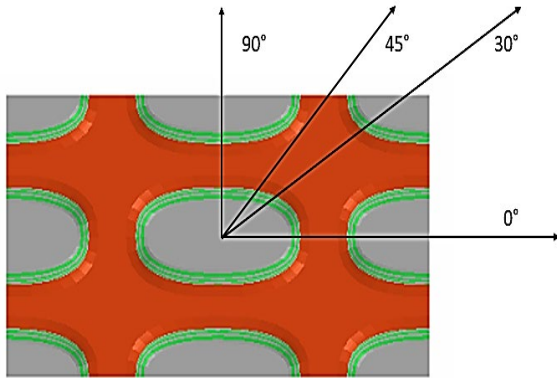
- 161.5nm*39.9nm at the bottom
- 180nm*64.5nm at the top





Polar plots: Comparison Etched vs Unetched

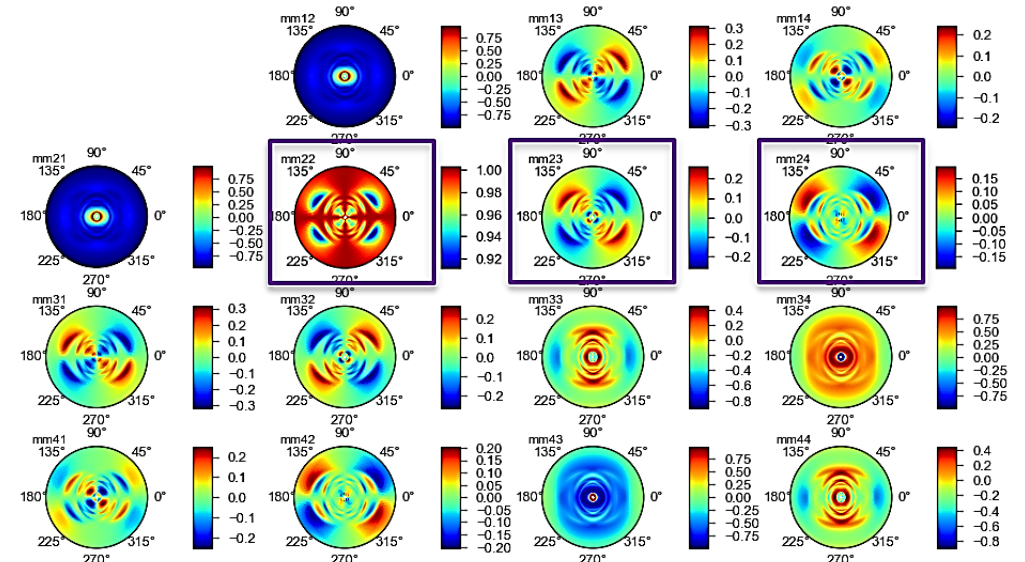
Unetched Nanowire Test Structure



Etched Nanowire Test Structure

- (For a SiGe etch of 20 nm)
- More sensitive MM Elements
- More intricate features

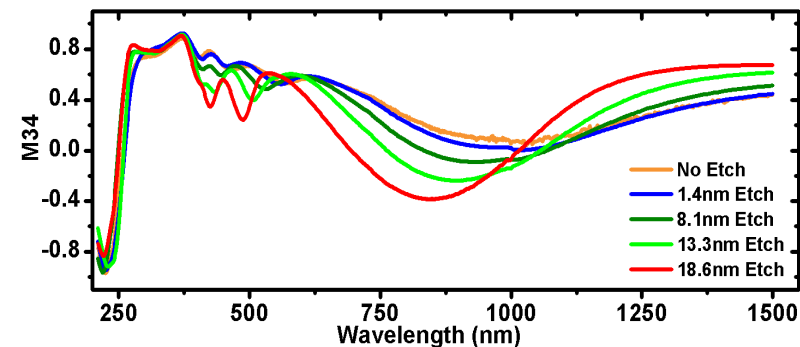
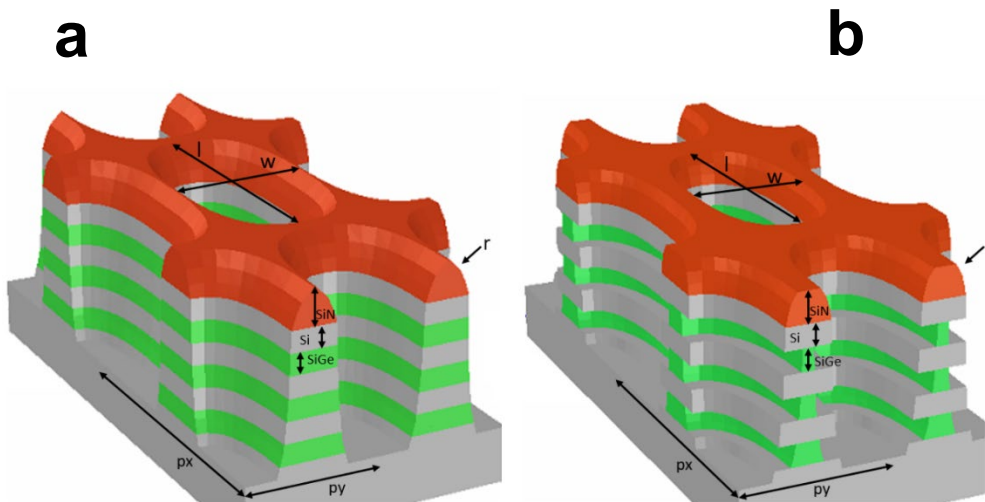
Asymmetric angles 30° and 45 have more symmetry





Experimental Sensitivity to SiGe layer etch aka : Cavity Etch

20 nm Si and SiGe layers

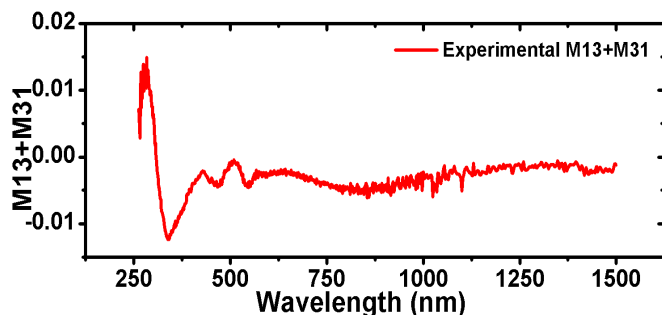


Selective etch analysis: Experimental data for MM34 at 45° azimuthal angle

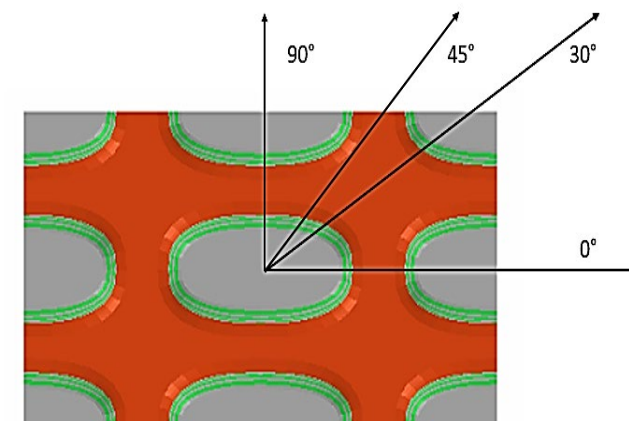
Final Scatterometry model after fitting experimental data:

(a) Unetched Nanowire Test Structure after regression analysis

(a) Etched Nanowire Test Structure 10.5nm



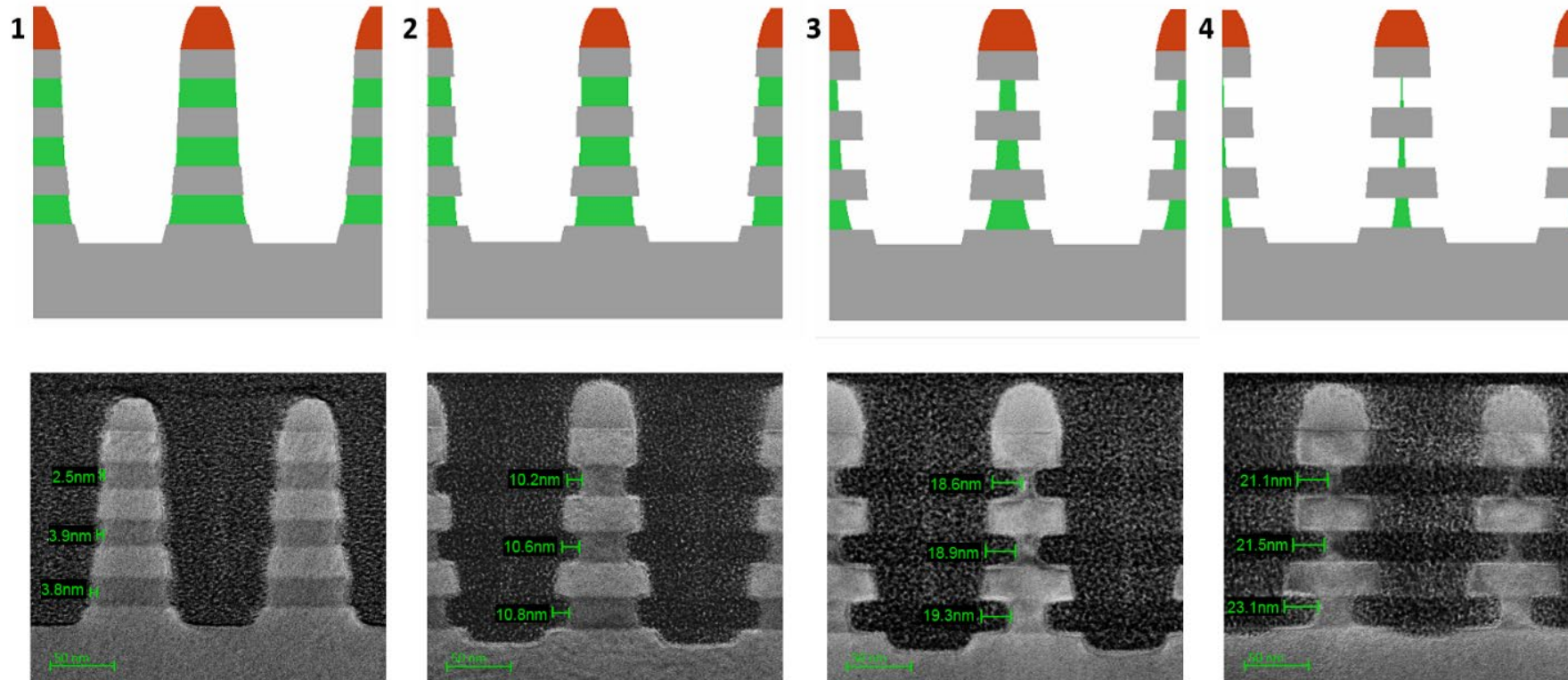
**The residual value for
M13+M31 for the 21.9 nm
etched NWTS**





Experimental Sensitivity to SiGe layer etch

Average amount of selective etch of the SiGe layers from each side :
3.4nm 10.5nm 18.9nm 21.9nm



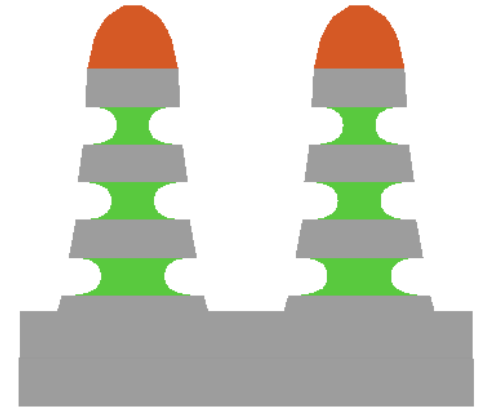
Y cross-sections
Selective etch of the SiGe layers in the NWTS

20 nm Si and SiGe layers



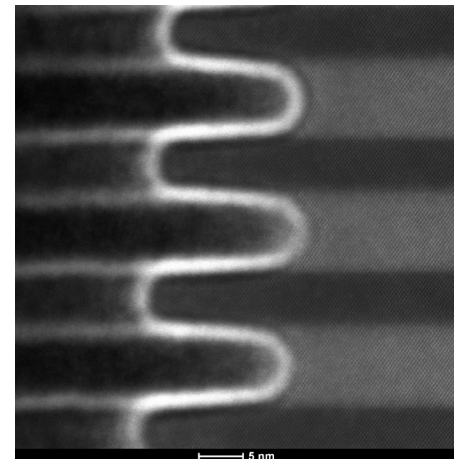
Experimental Sensitivity to SiGe layer etch

**Curved Cavity Profile Model does not
fit the 20 nm Si/ 20 nm Si(1-x)Ge(x)
data.**



**Curved Cavity Profile Model
does fit the < 10 nm Si/< 10 nm
Si(1-x)Ge(x) .**

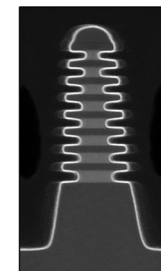
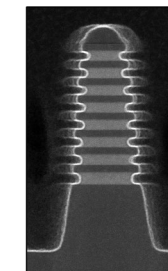
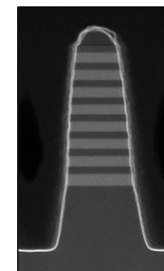
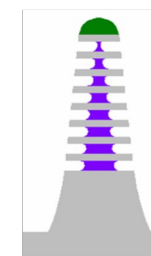
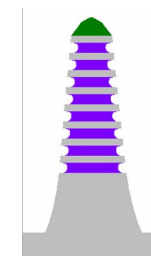
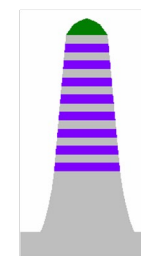
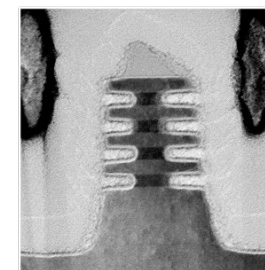
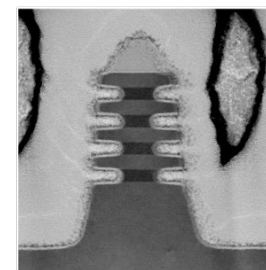
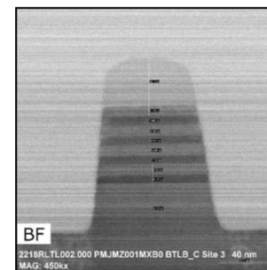
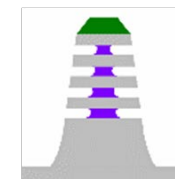
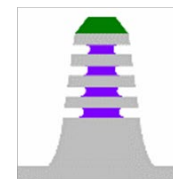
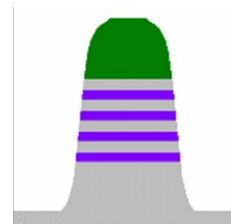
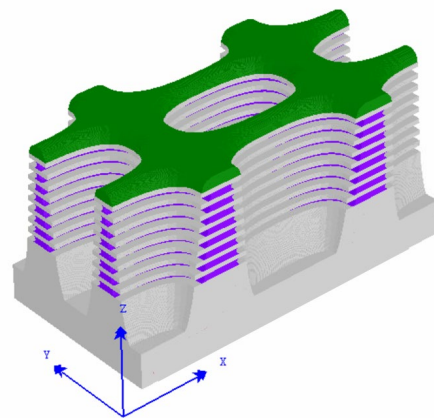
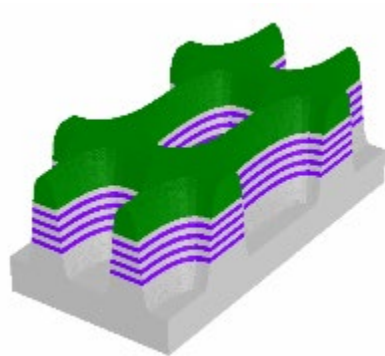
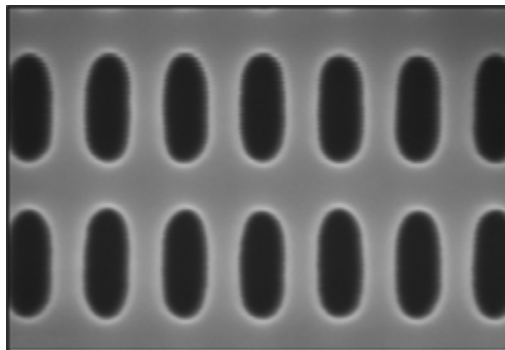
It also matches STEM images.





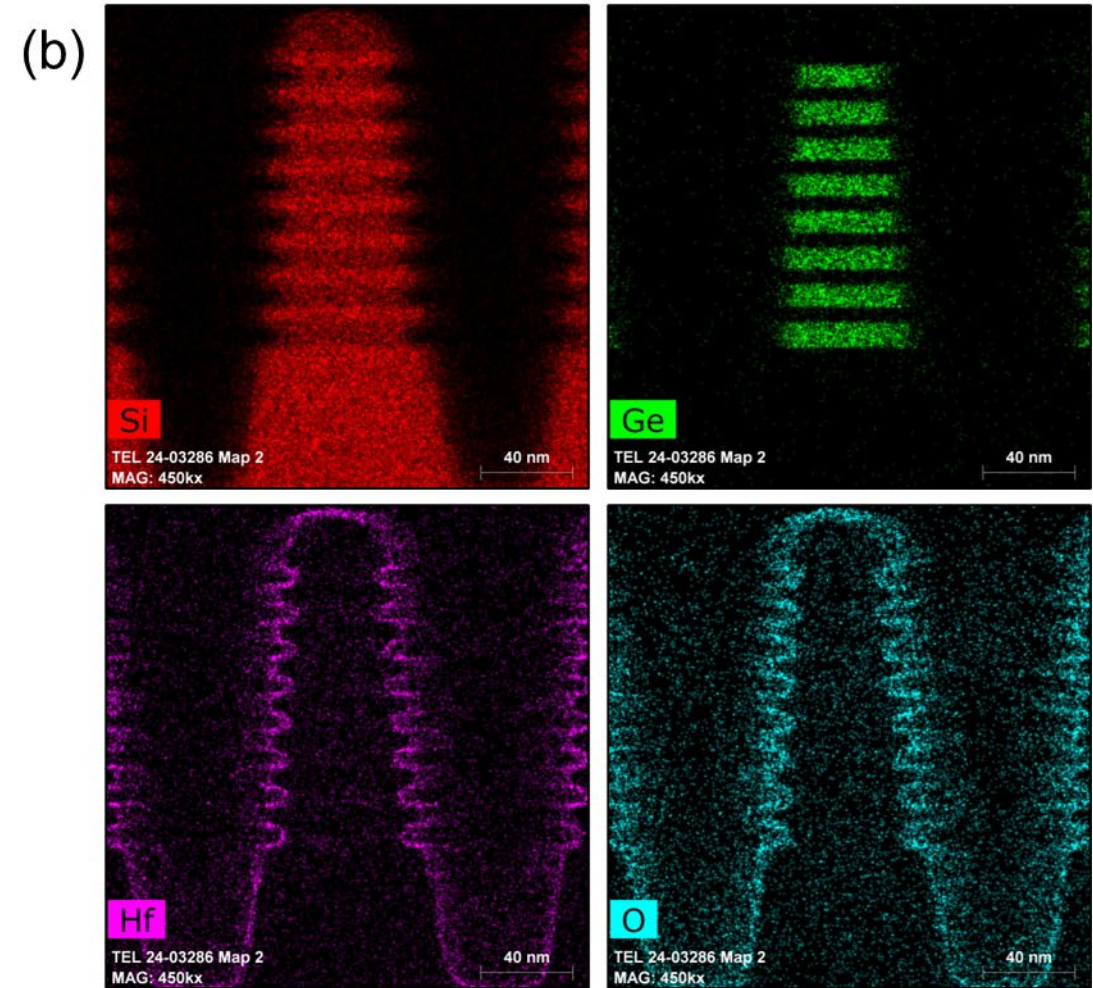
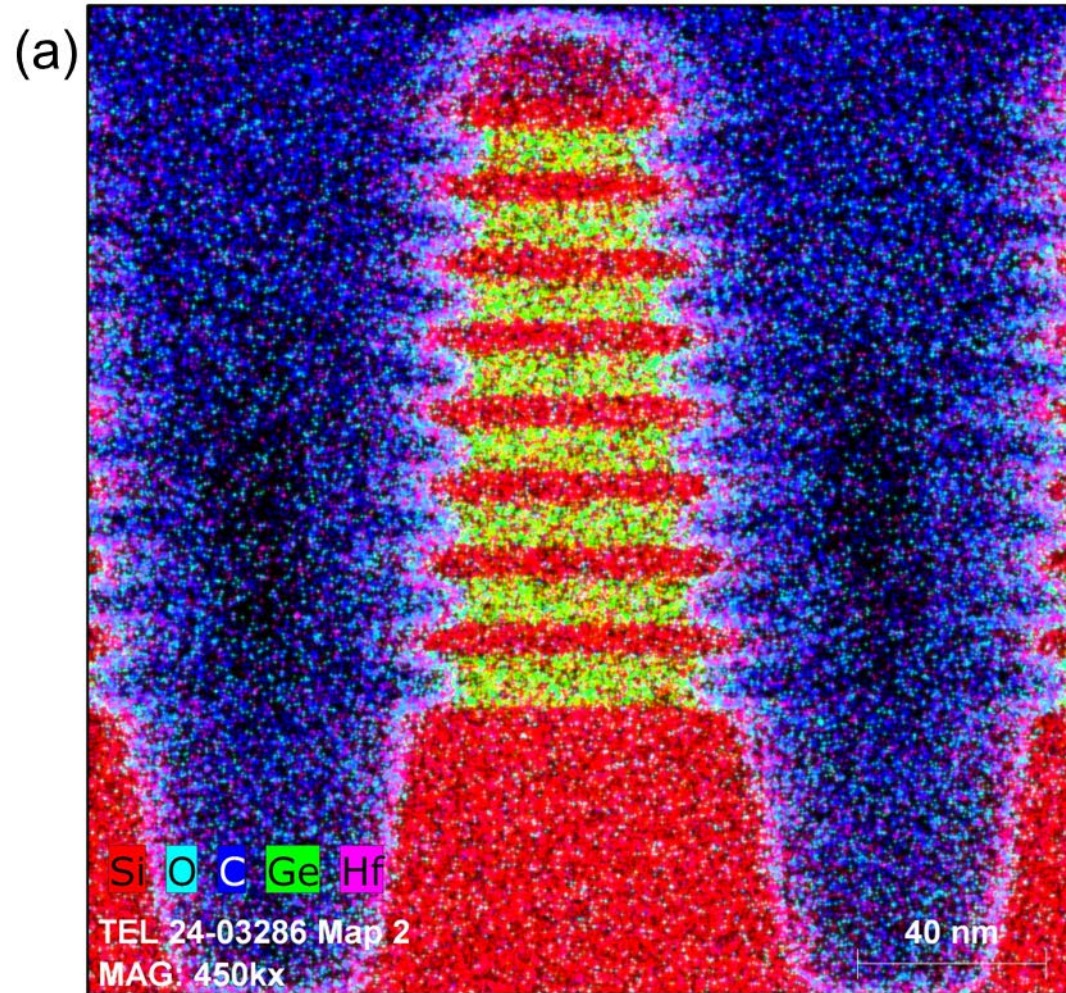
4x and 8x Superlattice NWTS

< 10 nm Si & Si(1-x)Ge(x) films





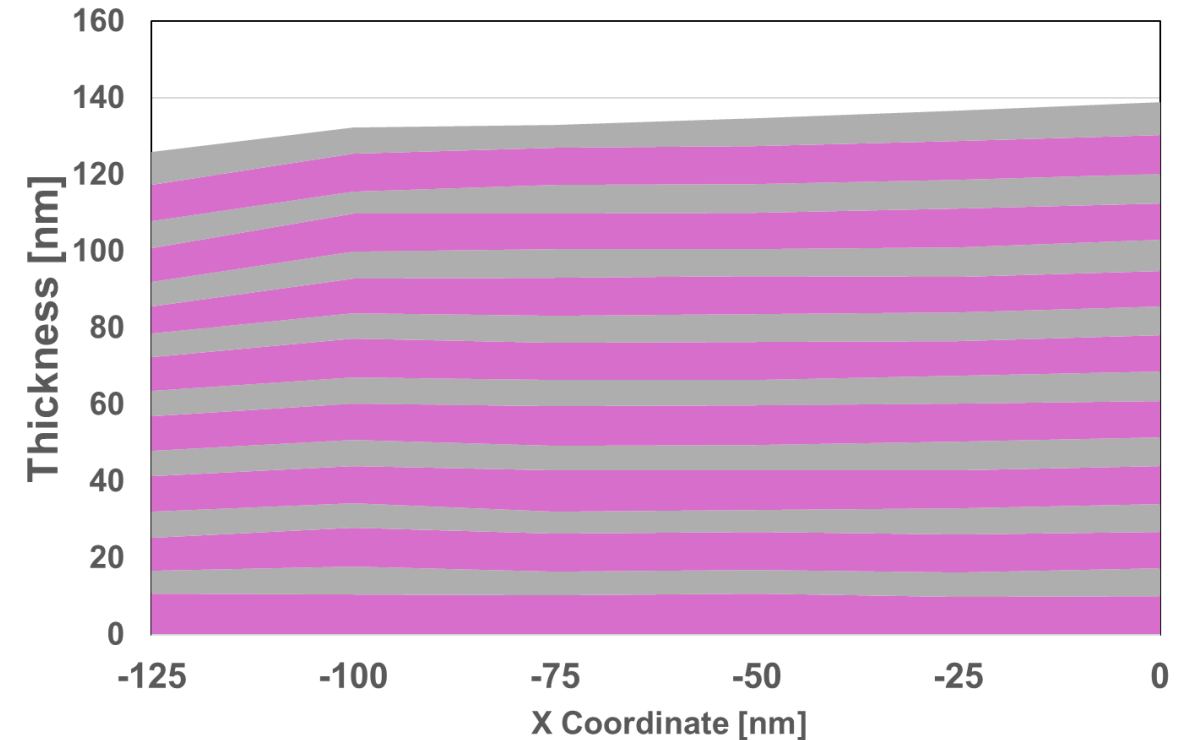
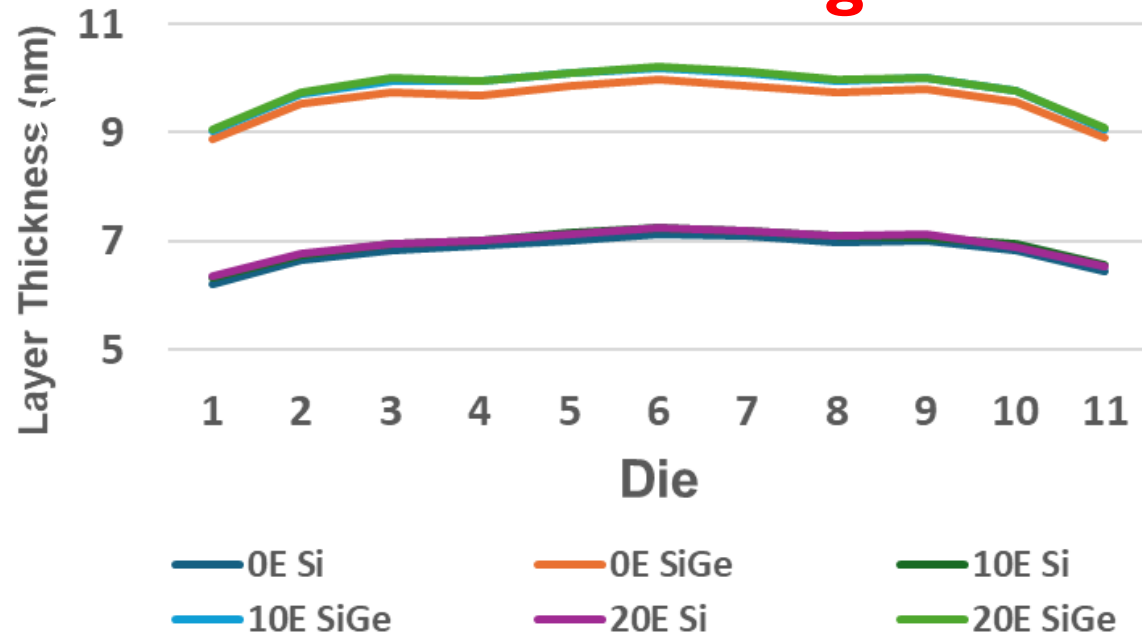
STEM/EDS of 8X Superlattice



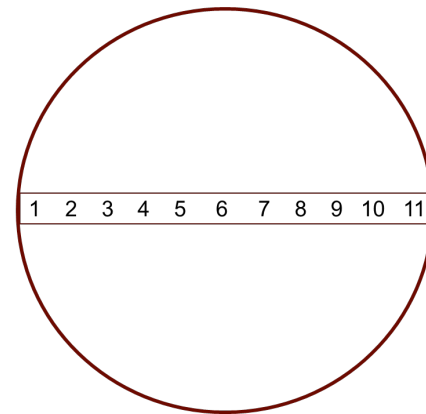
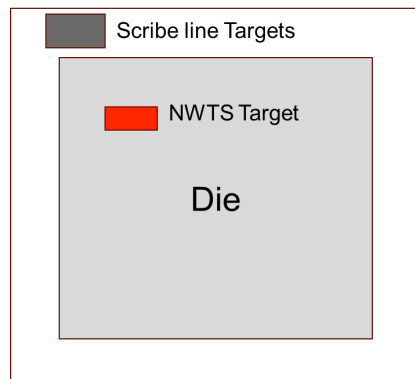
Critical Part of STEM -- Hf oxide protective coating before FIB sample preparation



Average HR-XRD Layer Thickness

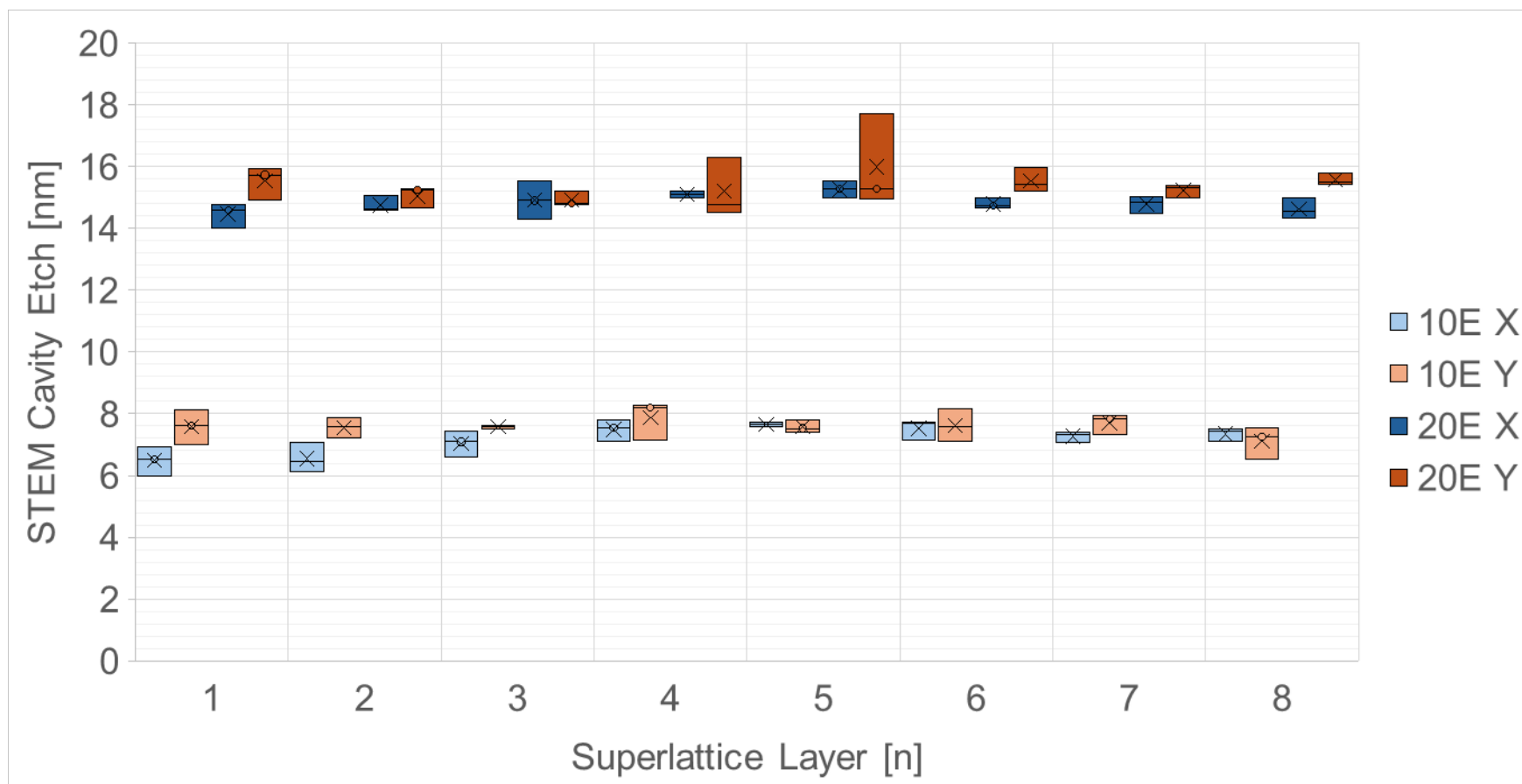


28.4 % Ge



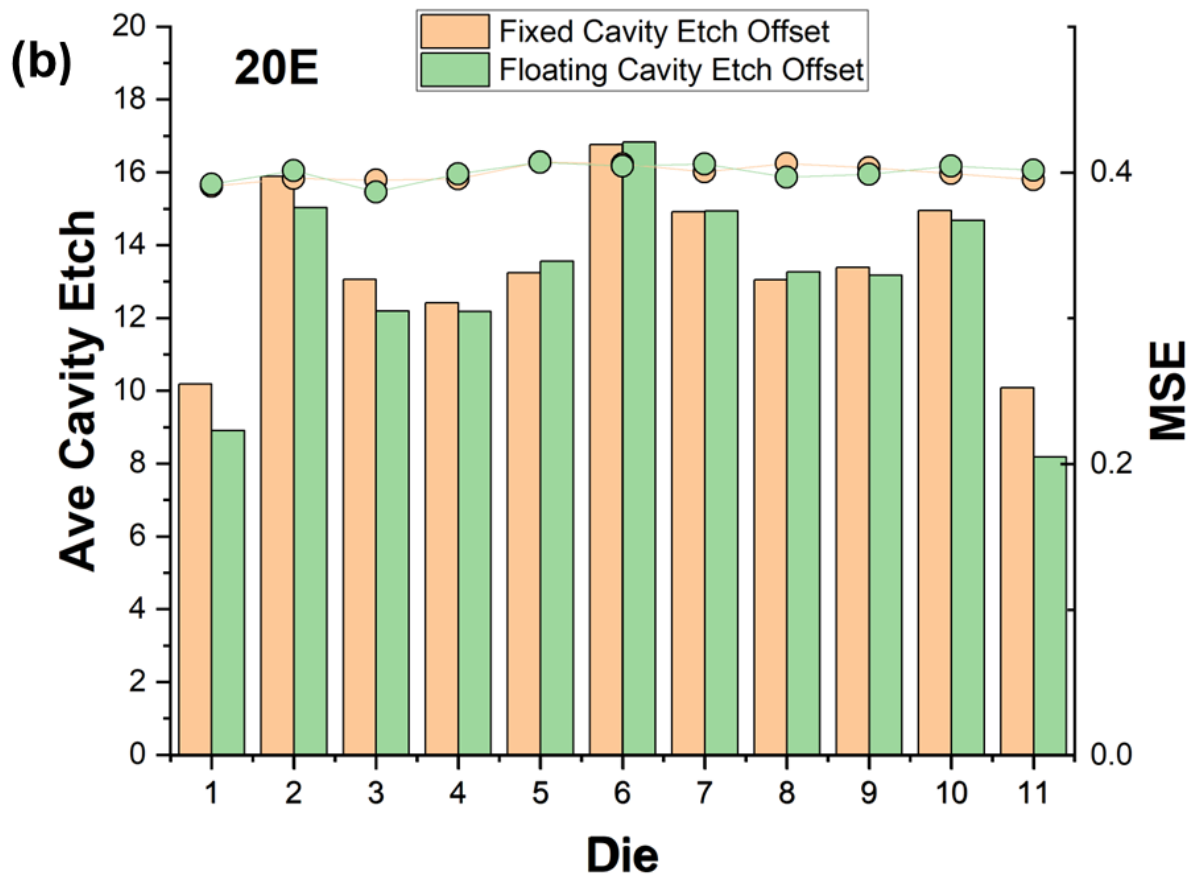
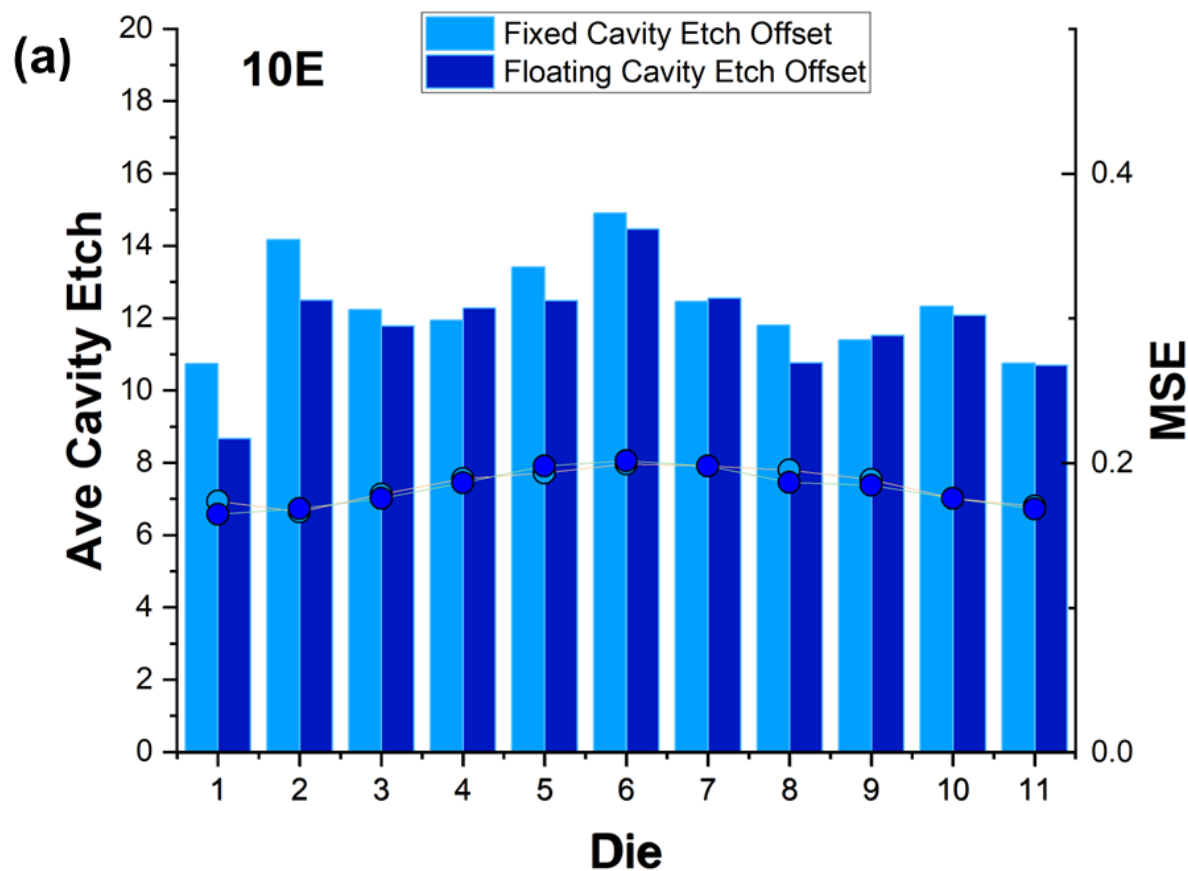


STEM Cavity Etch Variation between layers Die 1

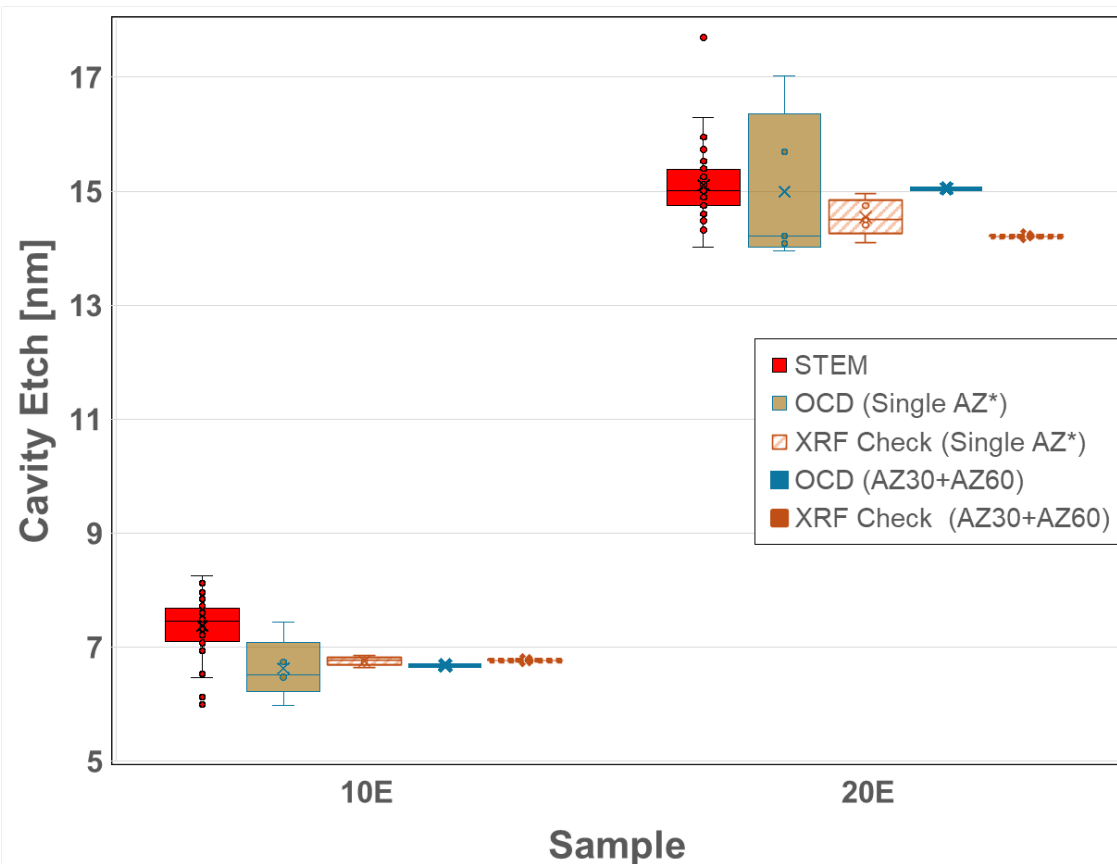




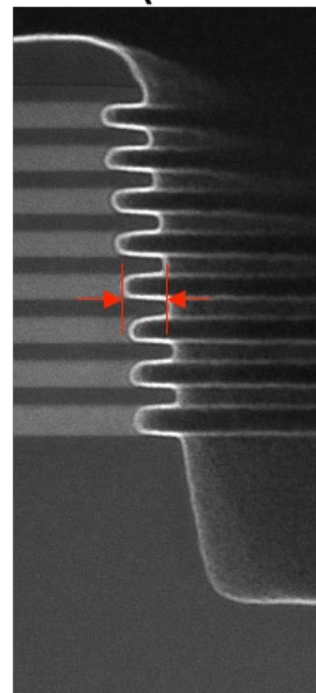
8X Superlattice Across-Wafer Variation



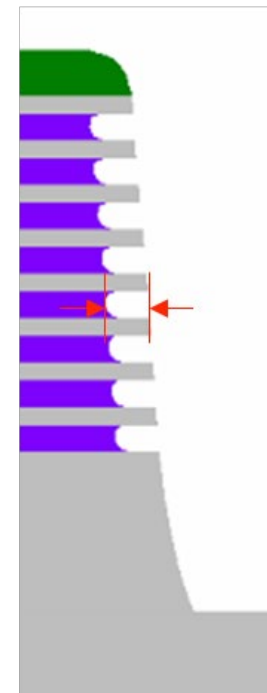
8X Superlattice : OCD vs STEM vs XRF



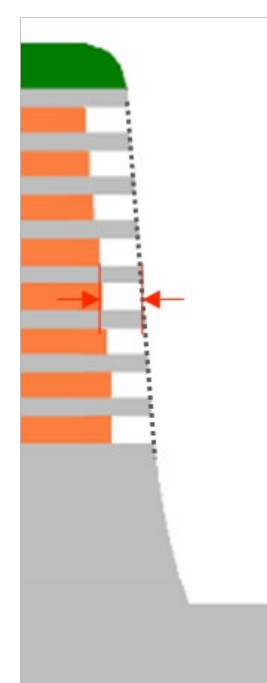
STEM (HAADF)



OCD Model



XRF Check



Sample	STEM	OCD (Single AZ*)	XRF Check (Single AZ*)	OCD (AZ30+AZ60)	XRF Check (AZ30+AZ60)
10E Avg. Cav. Etch [nm]	7.37	6.63	6.76	6.68	6.78
$\Delta = 10E$ Fit vs. STEM [nm]	--	-0.74	-0.61	-0.69	-0.59
20E Avg. Cav. Etch [nm]	15.11	14.99	14.54	15.05	14.22
$\Delta = 20E$ Fit vs. STEM [nm]	--	-0.12	-0.56	-0.06	-0.89



8X Superlattce Cavity Etch Correlation Tables

(a) AZ30: Abs. Correlation

Y Tilt [deg]	1								High	0.9
X Tilt [deg]	0.56	1							Elevated	0.8
SWA [deg]	0.3	0.17	1						Low	0.5
Si Overetch [nm]	0.32	0.17	0.83	1						
Hole Width [nm]	0.27	0.08	0.04	0.22	1					
Hole Length [nm]	0.36	0.16	0.84	0.85	0.49	1				
Cavity Etch [nm]	0.18	0.08	0.87	0.73	0.02	0.79	1			
SiN Thk. [nm]	0.08	0.03	0.23	0.22	0.1	0.11	0.01	1		
SiN HM SWA [deg]	0.1	0	0.27	0.27	0.09	0.15	0.02	0.99	1	
	Y Tilt [deg]	X Tilt [deg]	SWA [deg]	Si Overetch [nm]	Hole Width [nm]	Hole Length [nm]	Cavity Etch [nm]	SiN Thk. [nm]	SiN HM SWA [deg]	

AZ60: Abs Correlation

Y Tilt [deg]	1								High	0.9
X Tilt [deg]	0.62	1							Elevated	0.8
SWA [deg]	0.26	0.1	1						Low	0.5
Si Overetch [nm]	0.31	0.19	0.7	1						
Hole Width [nm]	0.19	0.06	0.25	0.15	1					
Hole Length [nm]	0.33	0.09	0.69	0.79	0.45	1				
Cavity Etch [nm]	0.17	0.04	0.85	0.65	0.18	0.7	1			
SiN Thk. [nm]	0.08	0.02	0.22	0.14	0.26	0.07	0.04	1		
SiN HM SWA [deg]	0.09	0.01	0.22	0.15	0.26	0.07	0.05	0.99	1	
	Y Tilt [deg]	X Tilt [deg]	SWA [deg]	Si Overetch [nm]	Hole Width [nm]	Hole Length [nm]	Cavity Etch [nm]	SiN Thk. [nm]	SiN HM SWA [deg]	

(b) AZ30+ AZ60: Abs. Correlation

Y Tilt [deg]	1								High	0.9
X Tilt [deg]	0.31	1							Elevated	0.8
SWA [deg]	0.06	0.02	1						Low	0.5
Si Overetch [nm]	0.04	0.03	0.76	1						
Hole Width [nm]	0.11	0.04	0.33	0.21	1					
Hole Length [nm]	0.12	0.01	0.84	0.7	0.12	1				
Cavity Etch [nm]	0.05	0.06	0.75	0.59	0.5	0.6	1			
SiN Thk. [nm]	0.07	0.11	0.19	0.32	0.24	0.02	0.06	1		
SiN HM SWA [deg]	0.07	0.08	0.23	0.34	0.2	0.06	0.02	0.99	1	
	Y Tilt [deg]	X Tilt [deg]	SWA [deg]	Si Overetch [nm]	Hole Width [nm]	Hole Length [nm]	Cavity Etch [nm]	SiN Thk. [nm]	SiN HM SWA [deg]	



- ❑ **What is Scatterometry & Requirements for Scatterometry**
- ❑ **3D Structures, 3D Devices, and Nanoscale Materials**
- ❑ **X-Ray Characterization**
- ❑ **MMSE-Scatterometry**
- ❑ **3D Nanowire Test Structures**
- ❑ **Conclusions**



- **HYBRID Metrology –**
 - ▣ X-Ray methods provide key information about superlattice structures
 - ▣ STEM provides feature dimensional reference
- (for ~ 6 layer superlattice) **Superlattice effect on optical properties due to interfacial layer (or roughness) not due to Brillouin zone folding.**
- Mueller Matrix Spectroscopic Ellipsometry enables scatterometry of complex structures
- MMSE-scatterometry is capable of non-destructively measuring sub-surface etching of complicated 3D structures --- **Requires individual layer optical properties for etched SiGe**



- ❑ E. Pasikatan, C. Wadsworth, N. Keller, G.A. Antonelli, A.C. Diebold. Characteristic Mueller matrix responses and correlation analysis for vertical GAA nanowire structure manufacturing using RCWA simulated spectra, **submitted**.
- ❑ E. Pasikatan, G.A. Antonelli, N. Keller, S. Kal, M. Rednor, K. Tapily, D. Hetzer, M. Schaefer, M. Kuhn, S. Murakami, and A.C. Diebold, Superlattice effects and limitations of non-destructive measurement of advanced Si/Si_{1-x}Ge_x superlattice structures using Mueller matrix scatterometry and high-resolution X-ray diffraction, **J. Micro/Nanopattern. Mater. Metrol. 23, (2024), 044004**.
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