

Small Organisms Making Big Problems: Modeling *Heterosigma Akashiwo*

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Harmful Algal Blooms



Harmful Algal Blooms



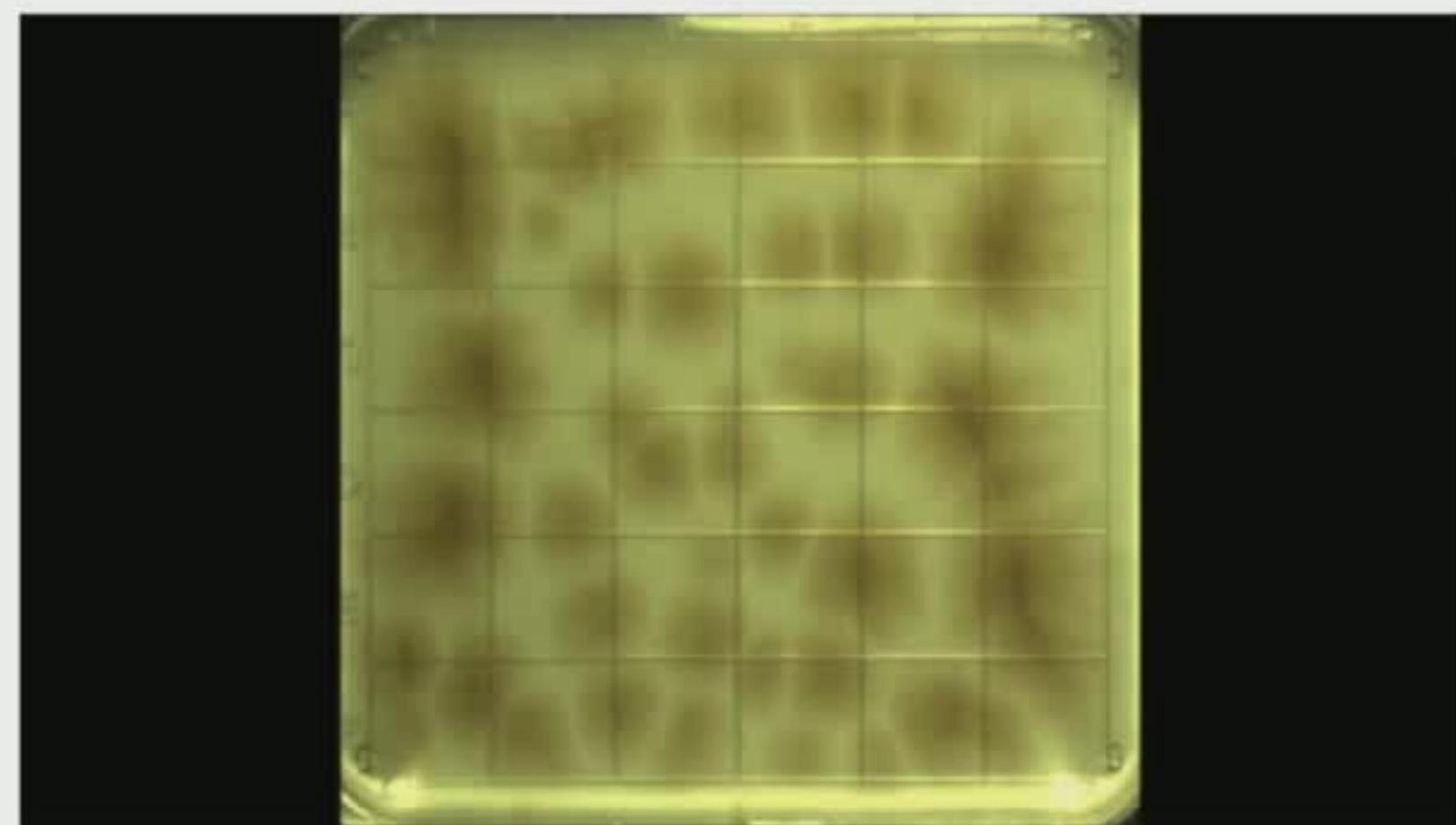
Our Lab



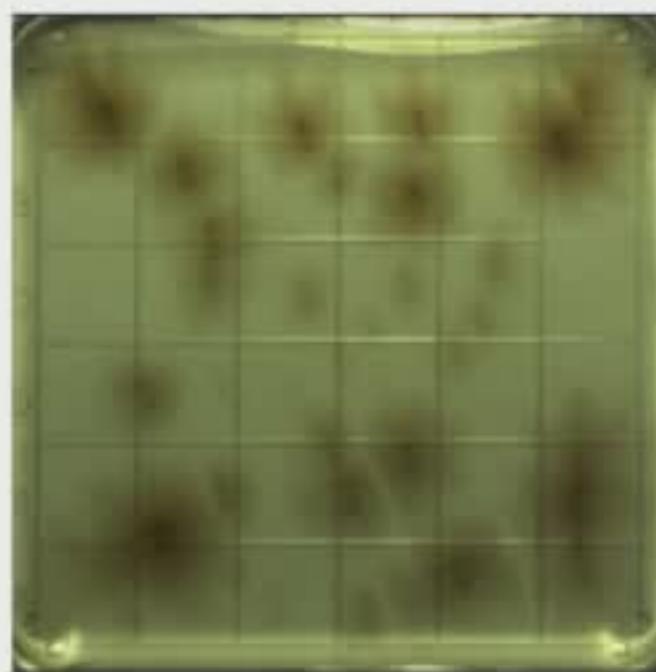
Example Experiment



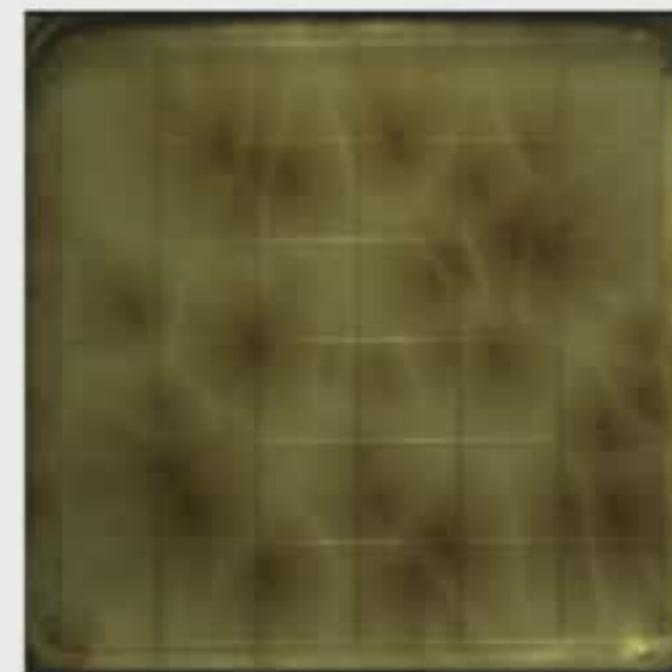
Example Experiment



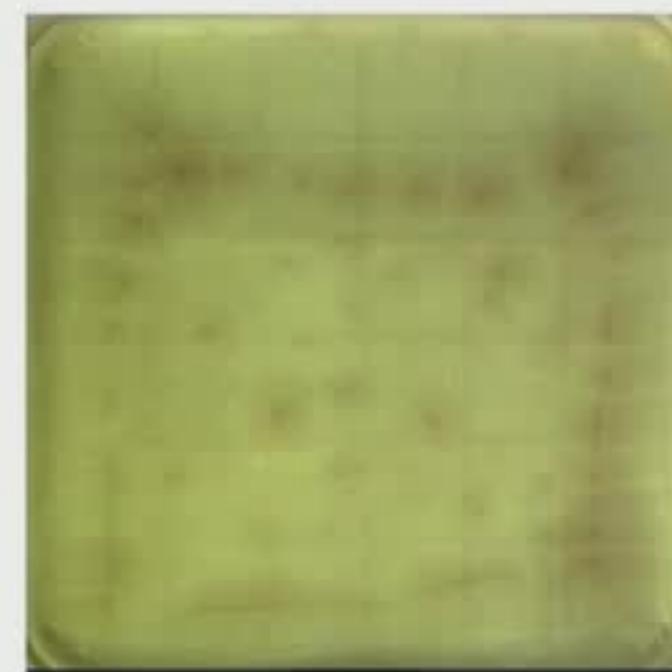
Intensity of Light



High Intensity



Low Intensity



Darkness

Depth



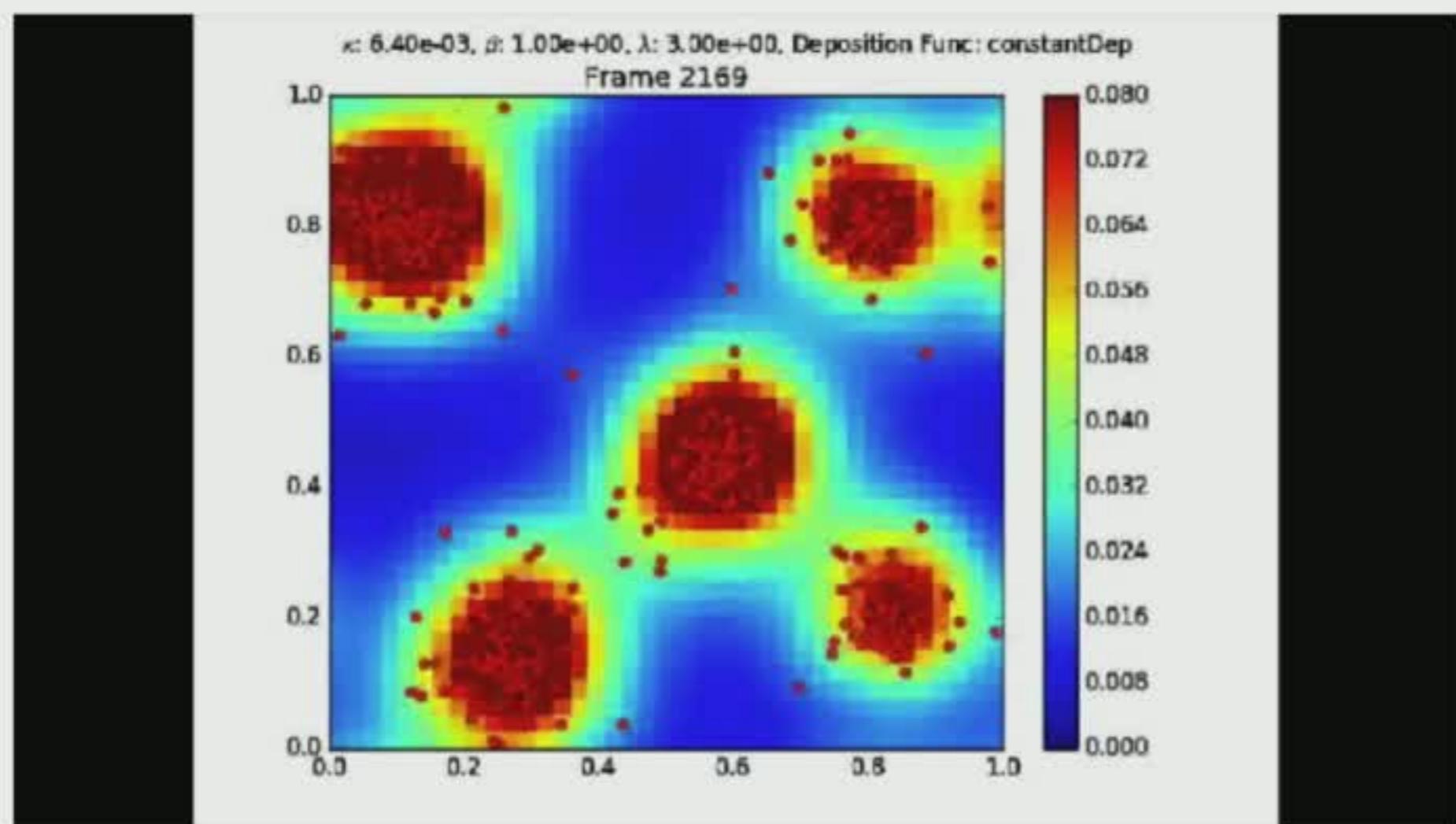
Depth



Computational Experiment: Constant



Computational Experiment: Constant

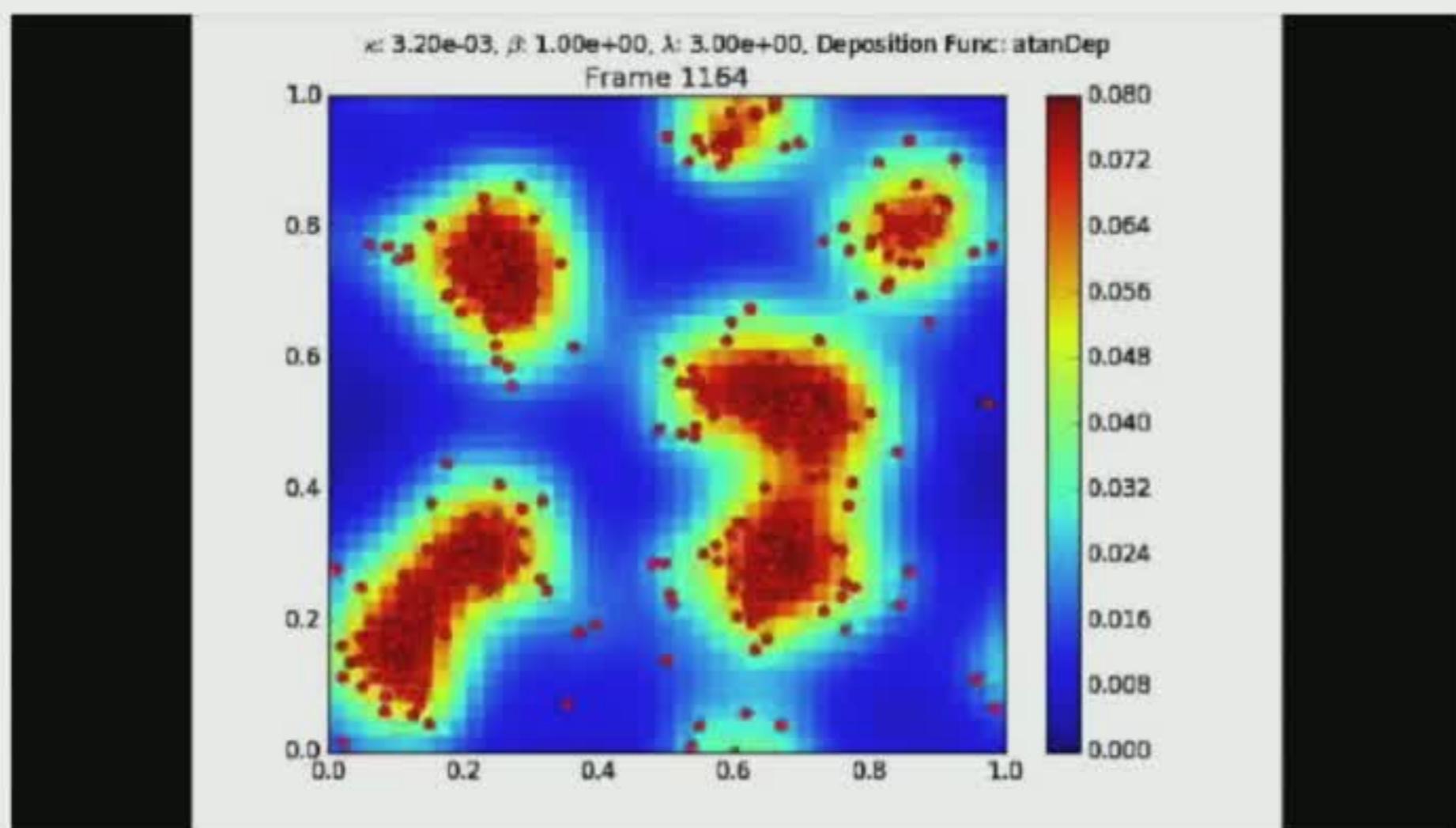


Computational Experiment: Switch

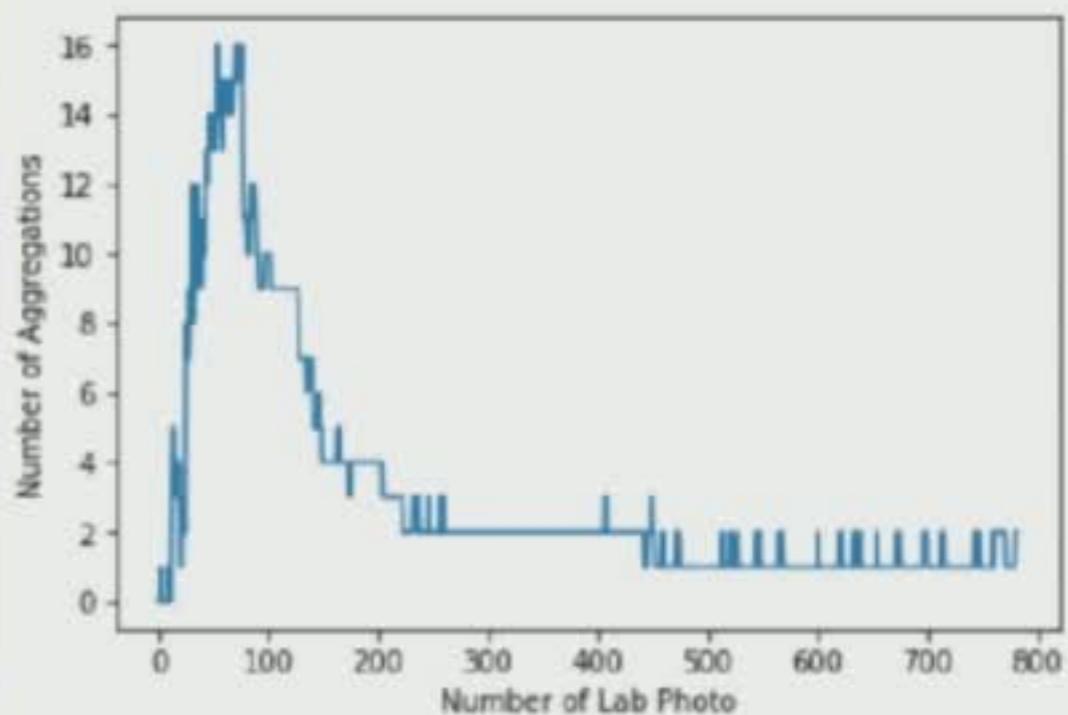
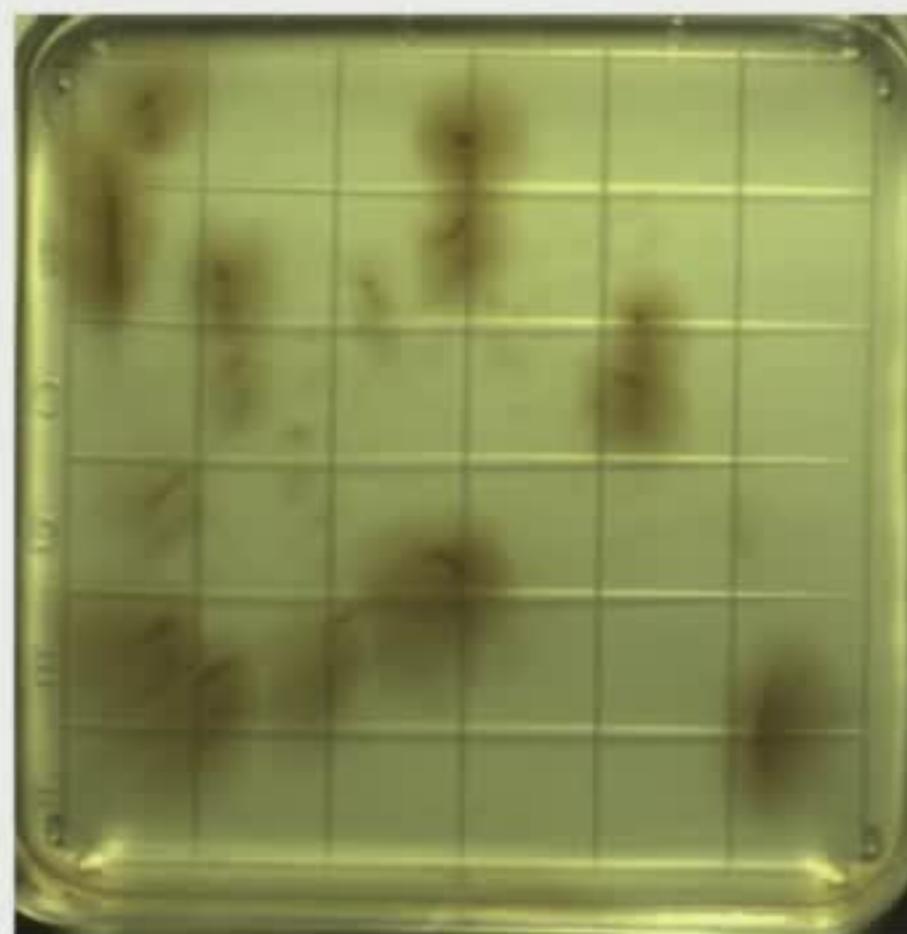


The Model

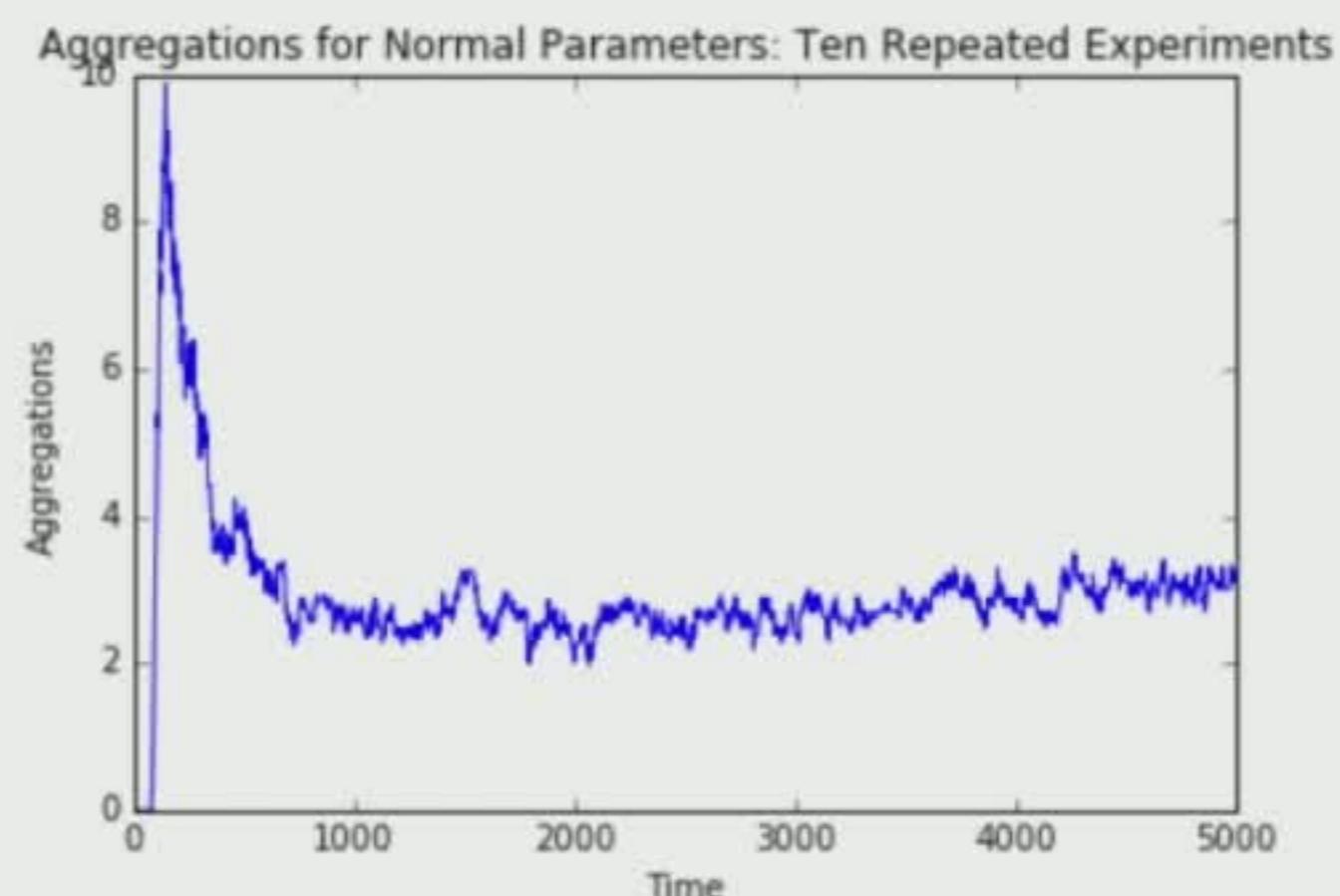
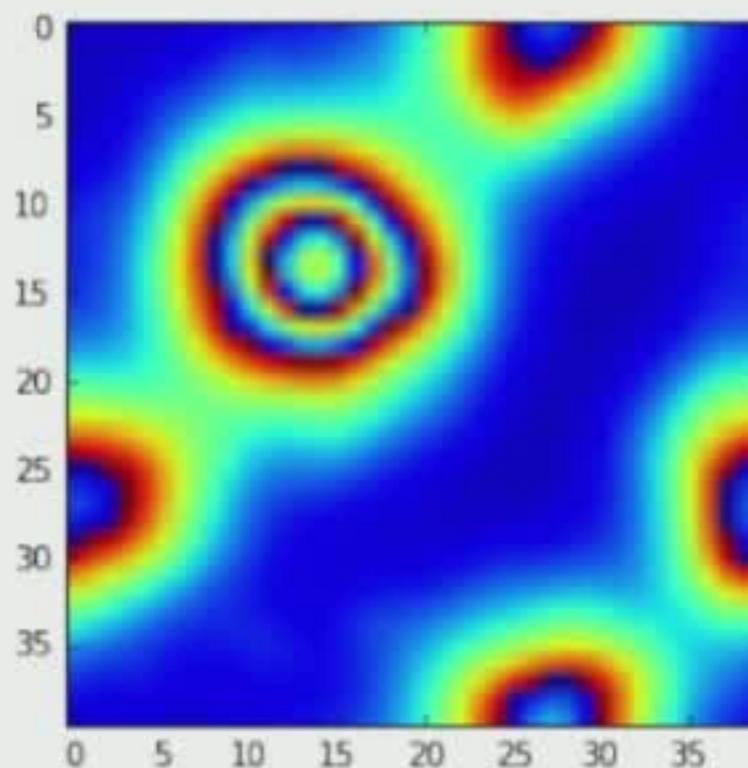
Computational Experiment: Switch



Observed Aggregation Count



Example of Aggregation Count



Steady States

$$c_t = d_1 c_{xx} - d_2 c + f(c)\rho$$

↓ Constant Solution ↓

$$d_2 \bar{c} = f(\bar{c})\bar{\rho}$$

Perturbations:

- ▶ Density: $\rho = \bar{\rho}(1 + \epsilon a)$
- ▶ Chemical: $c = \bar{c}(1 + \epsilon b)$

where a, b are functions.

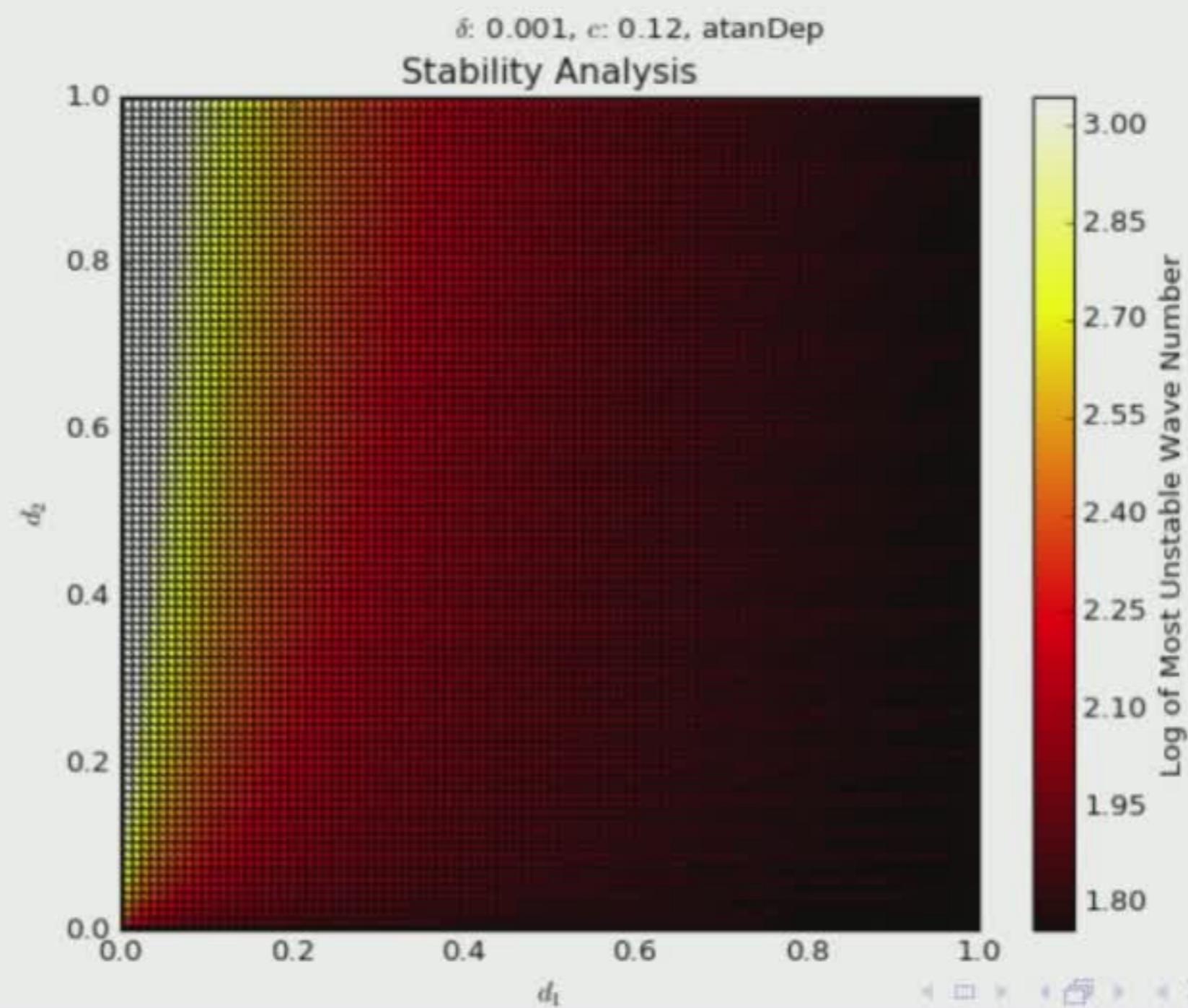
Characteristic Equation (n is the wave number):

$$\begin{aligned} r^3 + [d_1 n^2 - d_3 + 1] r^2 + [(d_1 + 1)n^2 - d_3] r \\ + n^2 \left(d_1 n^2 - d_3 - \frac{\bar{c} d_2}{\delta} \right) = 0 \end{aligned}$$

where $d_3 = \bar{\rho}f'(\bar{c}) - d_2$

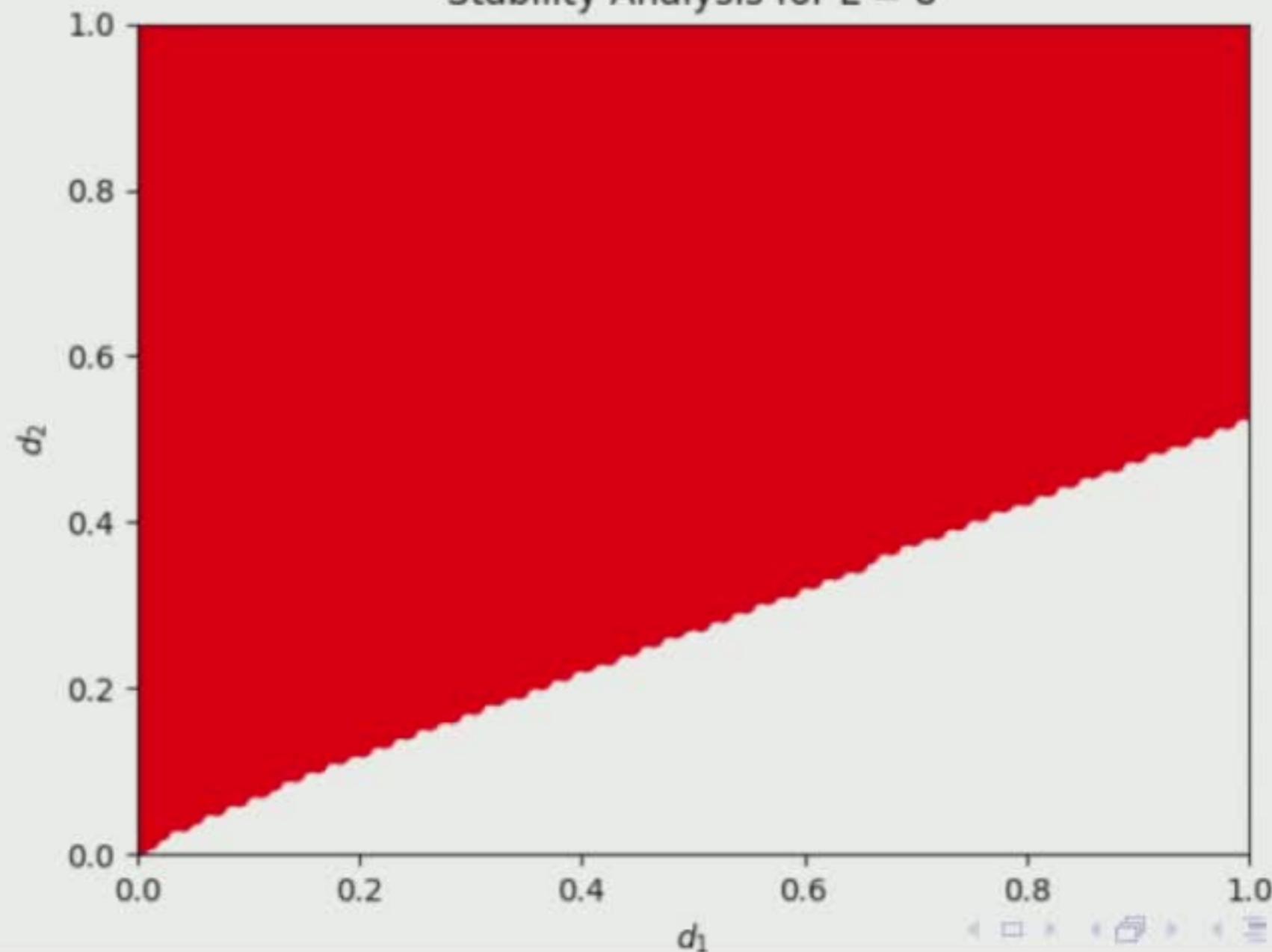
- ▶ $\text{Re}(r) > 0 \implies \text{Instability}$
- ▶ $\text{Re}(r) < 0 \implies \text{Stability}$

Most Unstable Wave Number

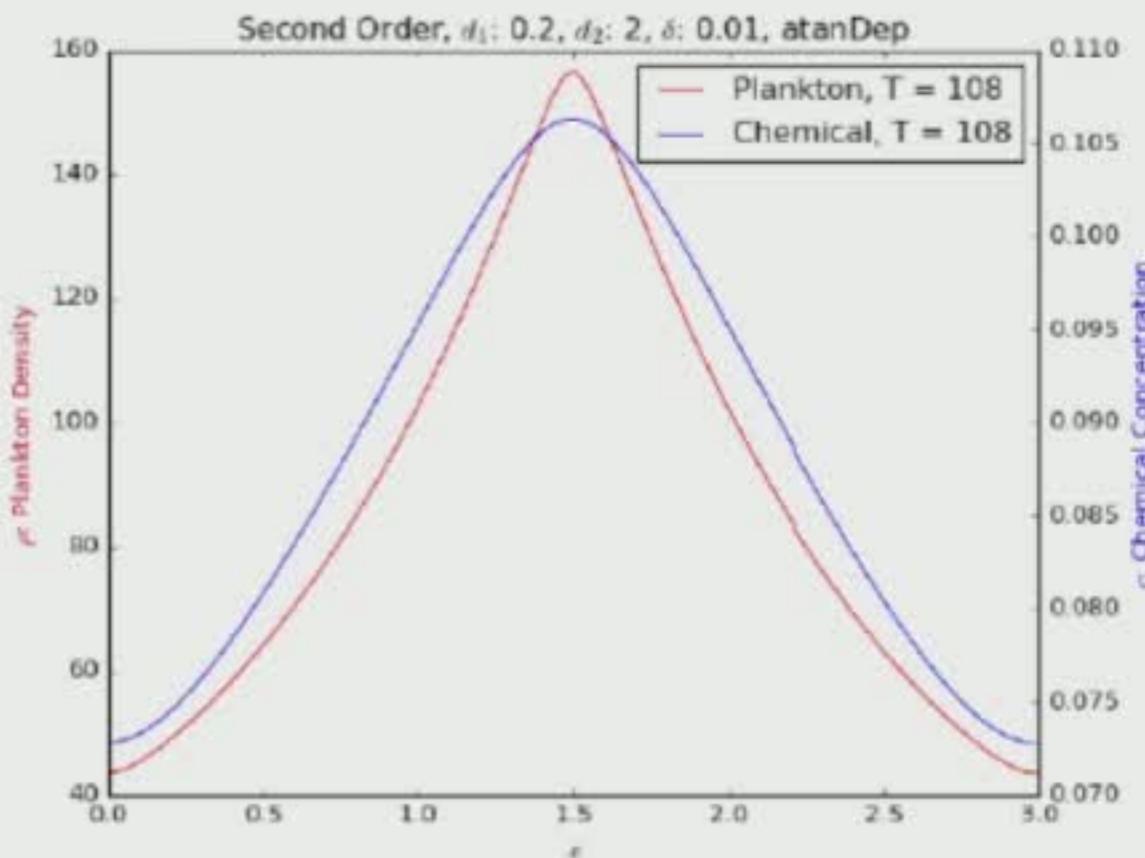
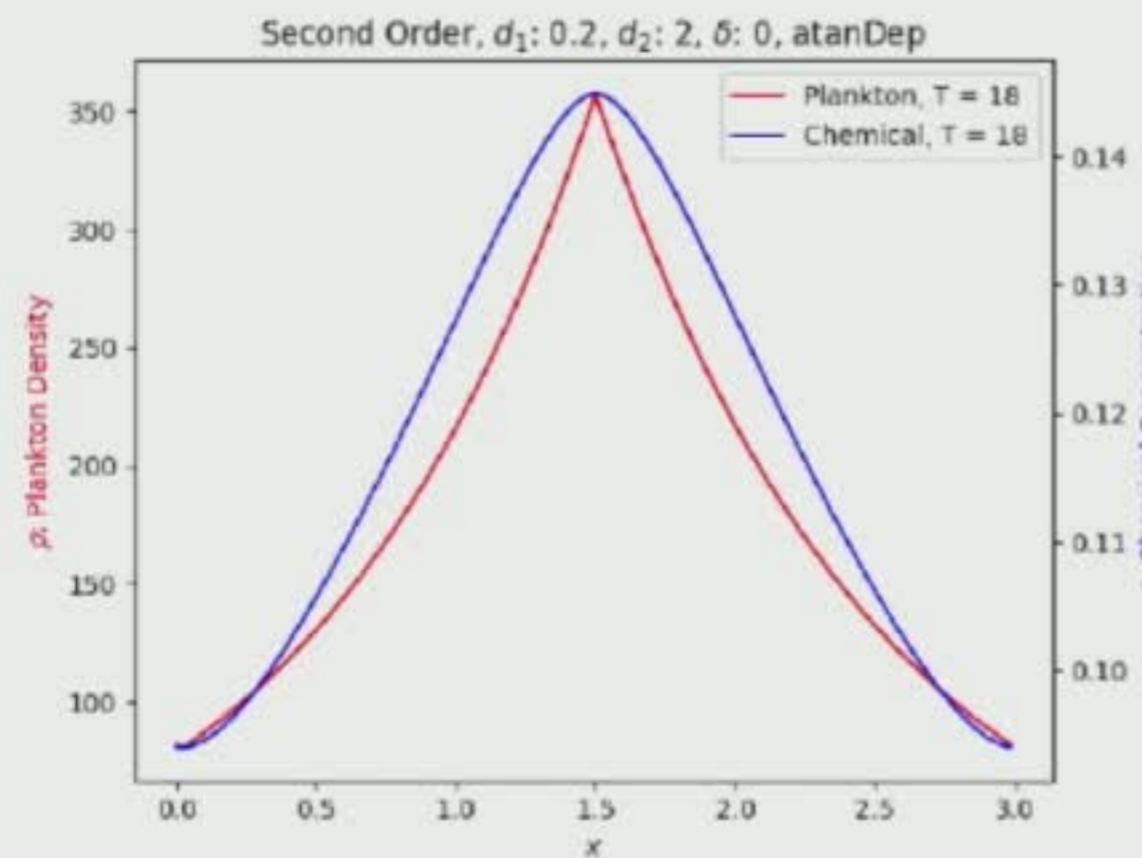


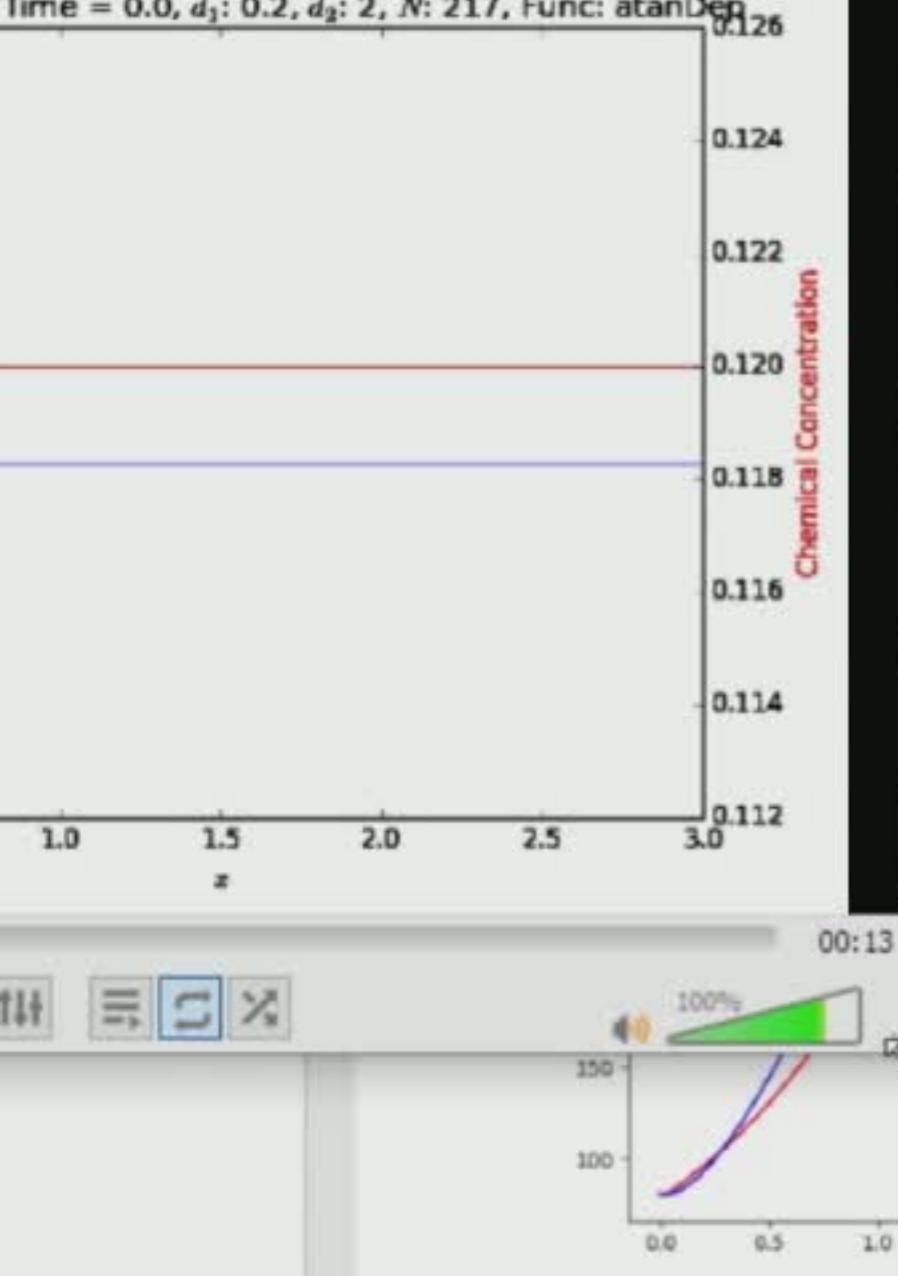
Stability Regions

$\delta: 0.01, c: 0.12, \text{atanDep}$
Stability Analysis for $L = 8$



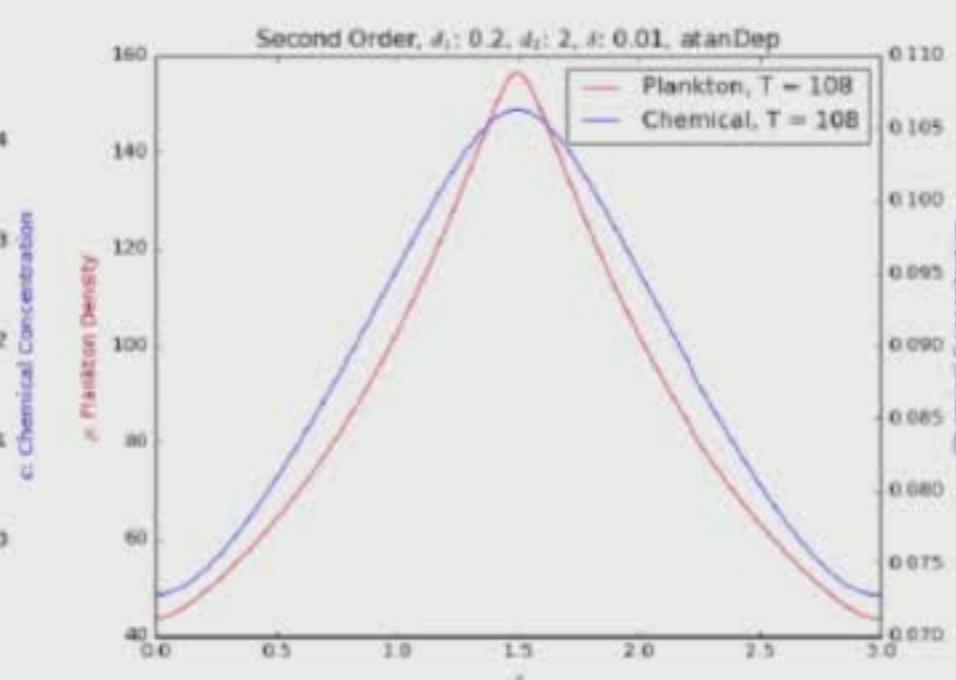
Steady States for Different Delta



Time = 0.0, d_1 : 0.2, d_2 : 2, N: 217, Func: atanDepModel and Results
ooooooooooooooAnalysis of the 1D Model
oooooo•

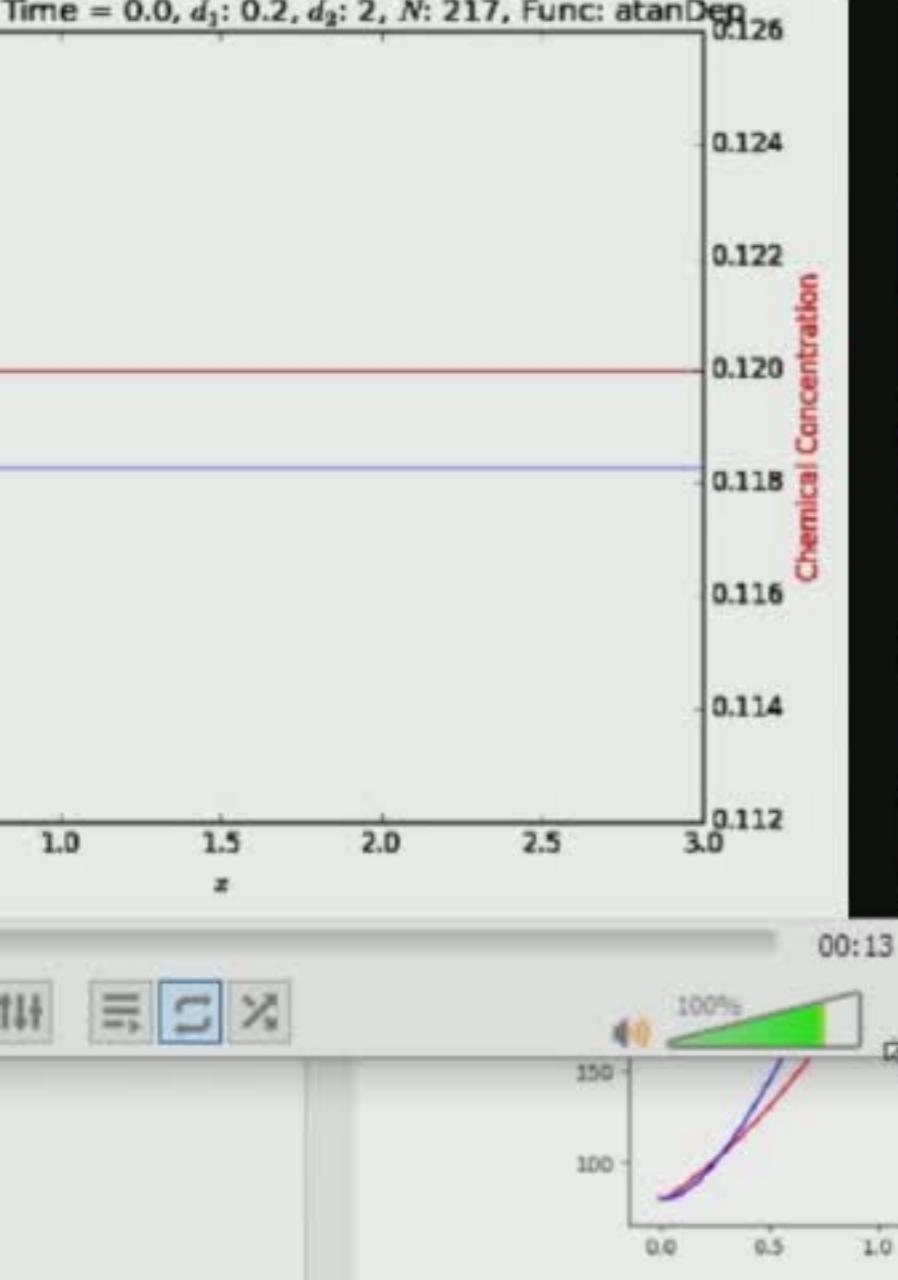
Future Goals

for Different Delta



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Heterosigma Akashiwo

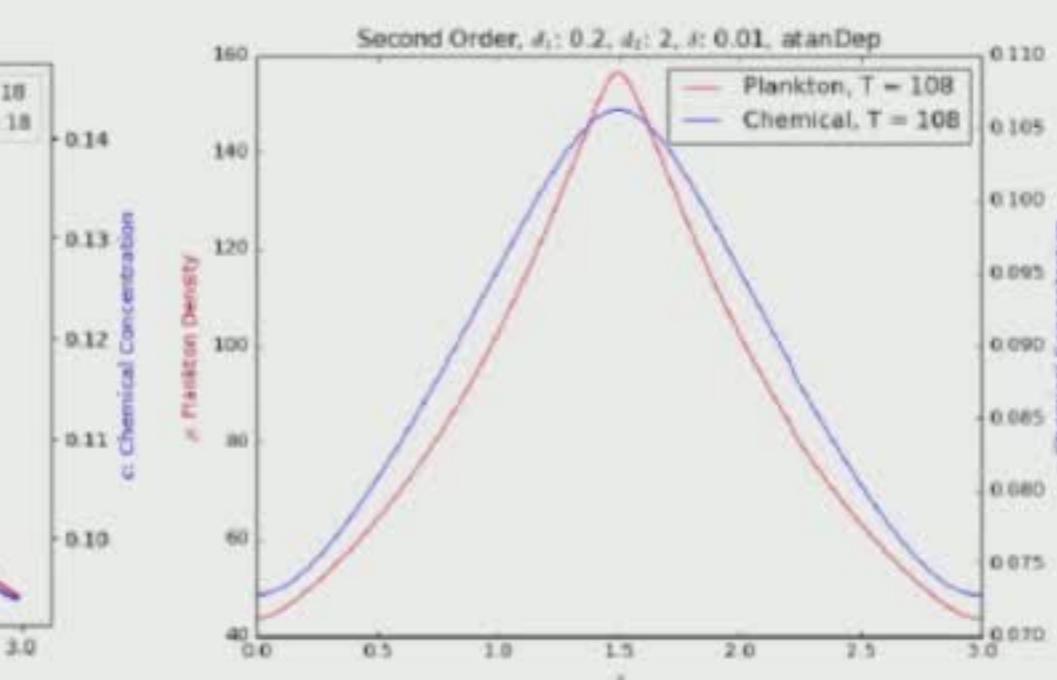
Time = 0.0, d_1 : 0.2, d_2 : 2, N: 217, Func: atanDep

Model and Results

Analysis of the 1D Model

Future Goals

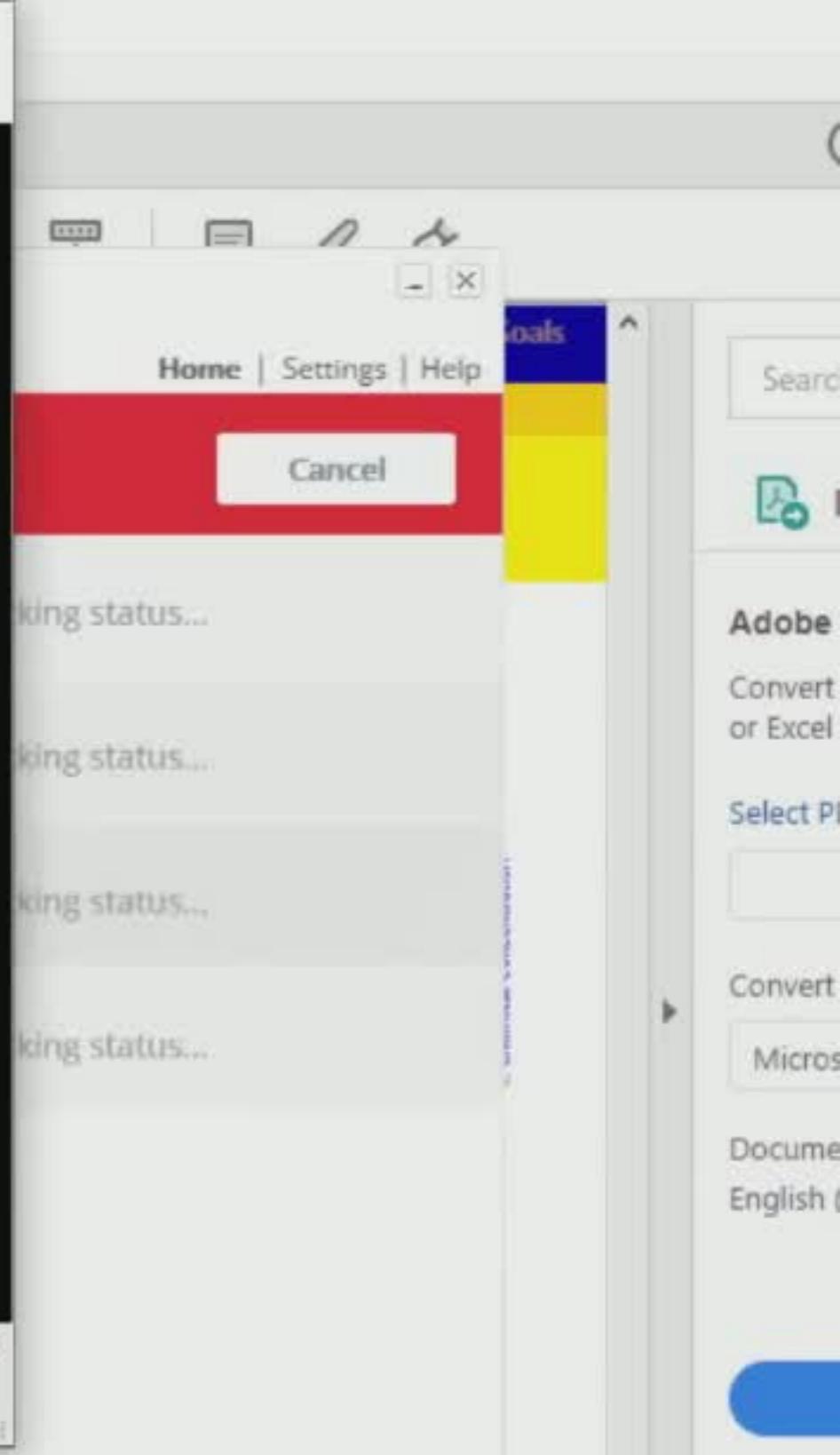
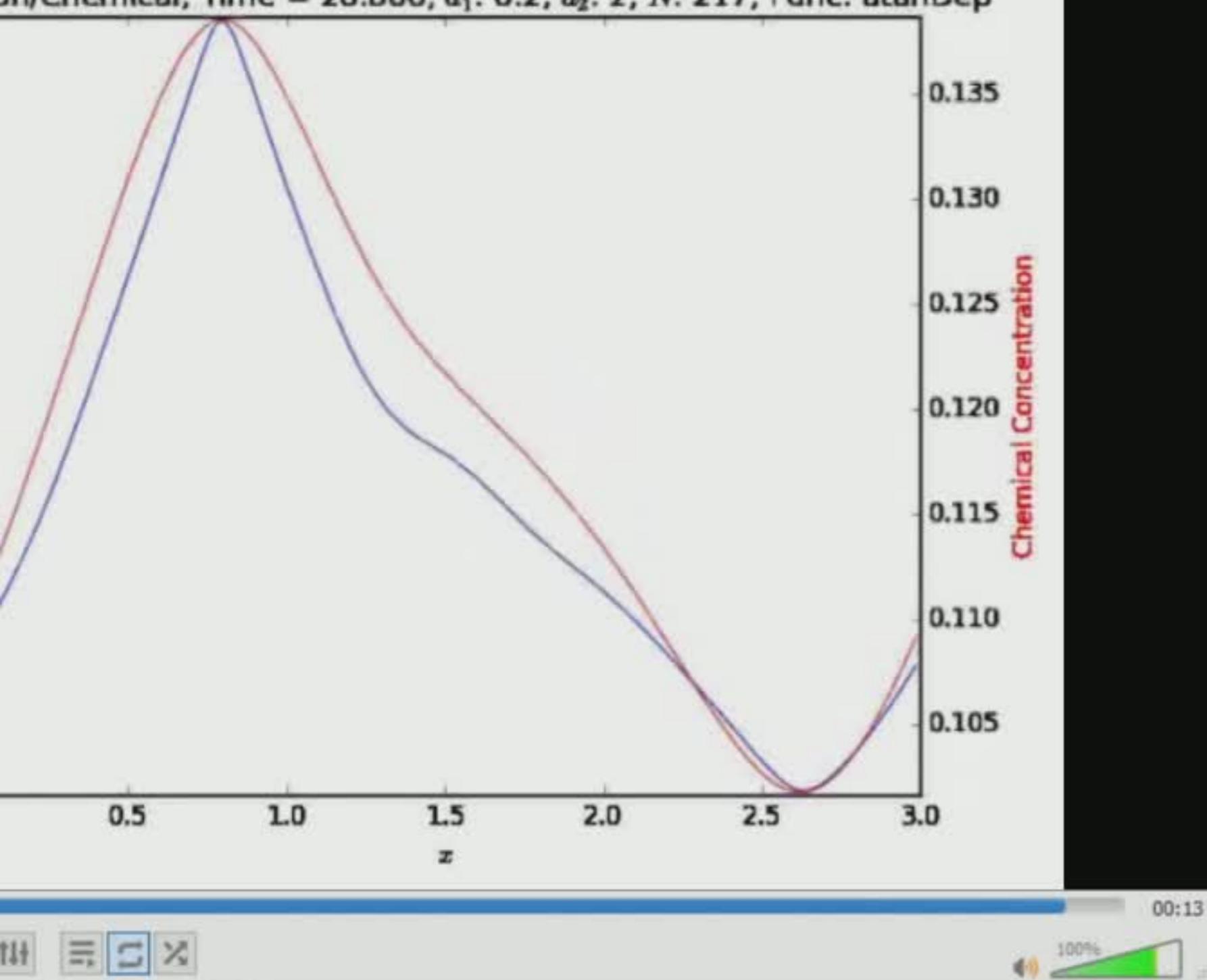
for Different Delta



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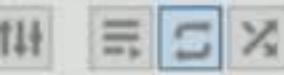
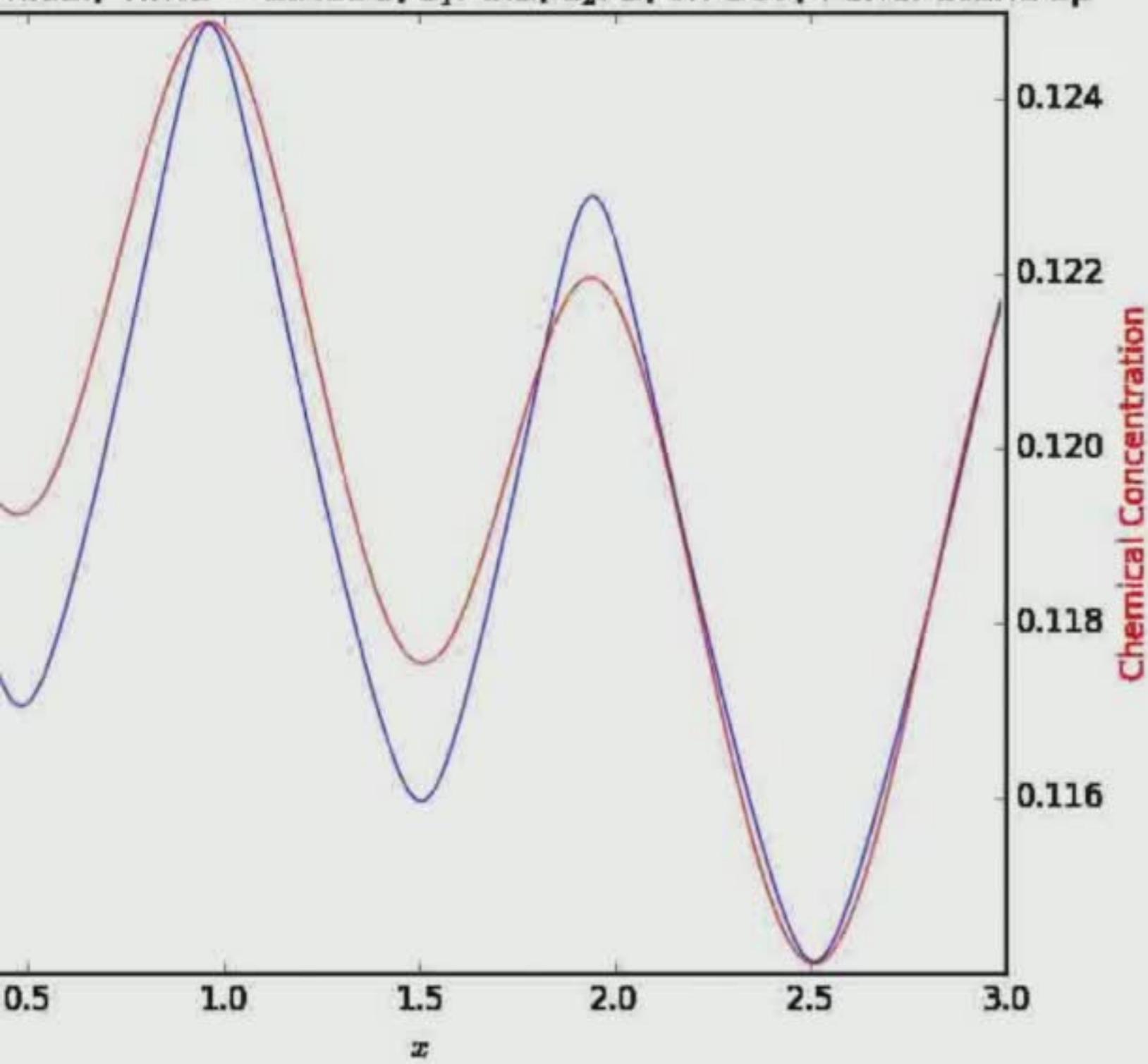
Video Subtitle Tools View Help

on/Chemical, Time = 26.866, d_1 : 0.2, d_2 : 2, N: 217, Func: atanDep

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Video Subtitle Tools View Help

Chemical, Time = 25.156, d_1 : 0.2, d_2 : 2, N: 217, Func: atanDep

Heterosigma Akashiwo

