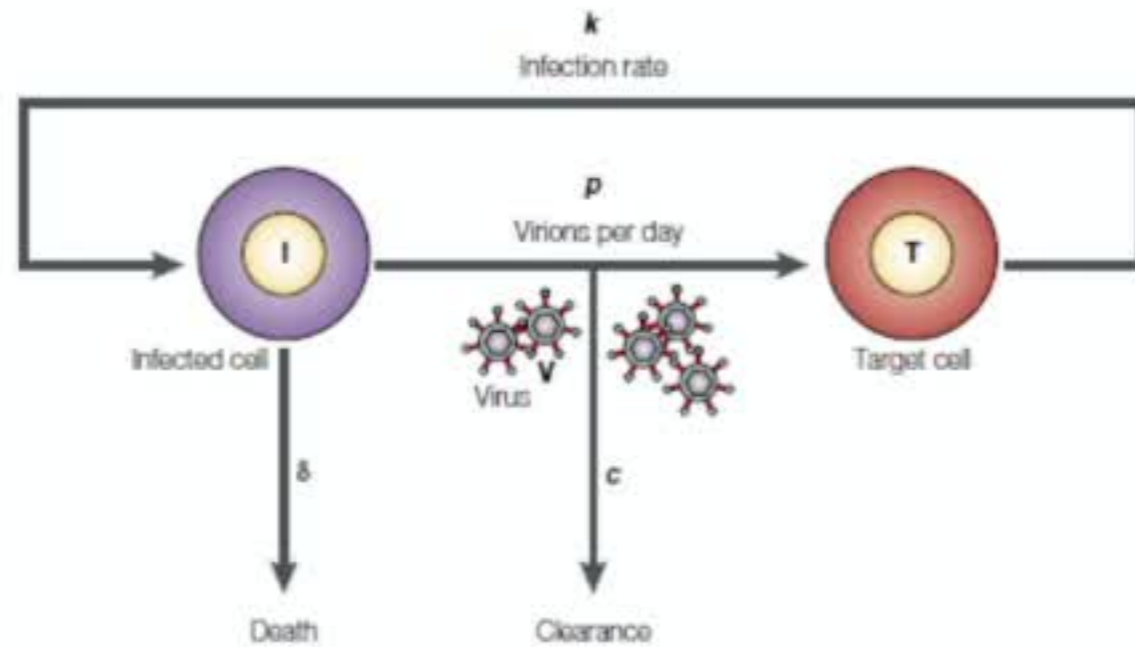




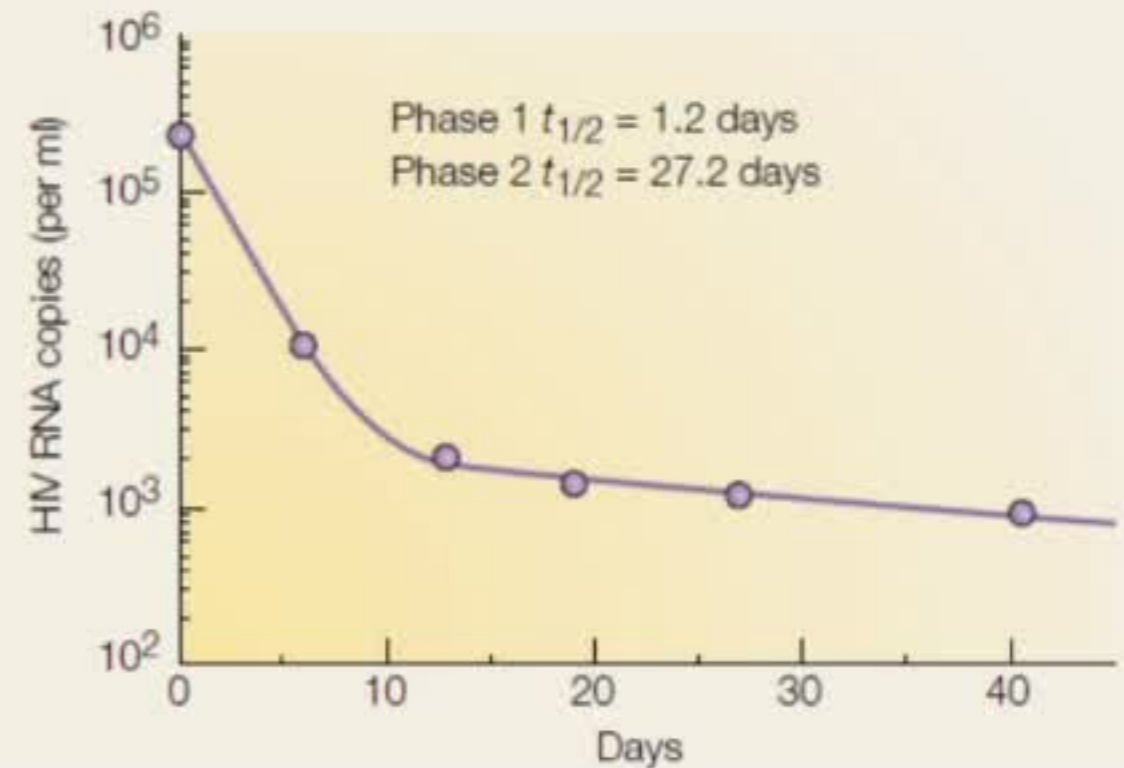
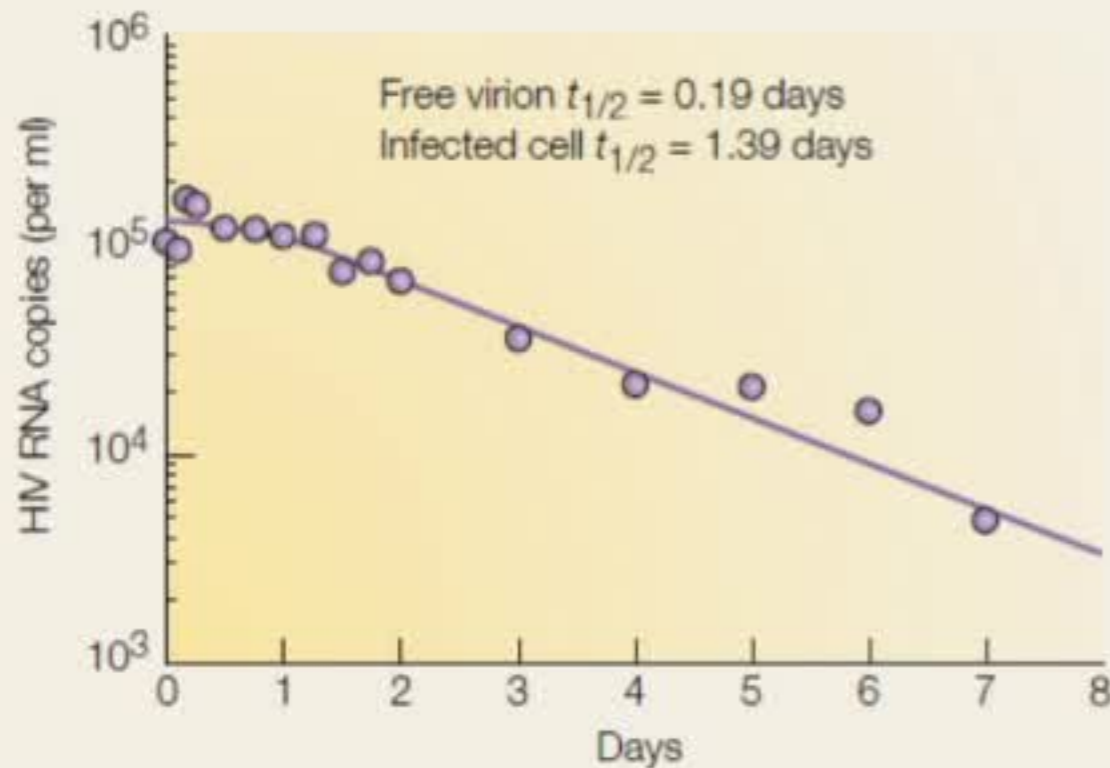
# Models with a well-mixed assumption often explain clinical data extremely well



$$\frac{dT}{dt} = \lambda - dT - kVT$$

$$\frac{dI}{dt} = kVT - \delta I$$

$$\frac{dV}{dt} = pI - cV$$



## Considering spatial structure is crucial to the understanding and prediction of the role of many biological processes

1. The frequency of co-infection/ the role of influenza semi-infectious particles.
2. The effectiveness of therapeutics, such as defective interfering particles.
3. The impact of the interferon response to virus infection (especially at the initial period of infection).

Ignoring spatial structure would lead to incorrect conclusions/predictions!

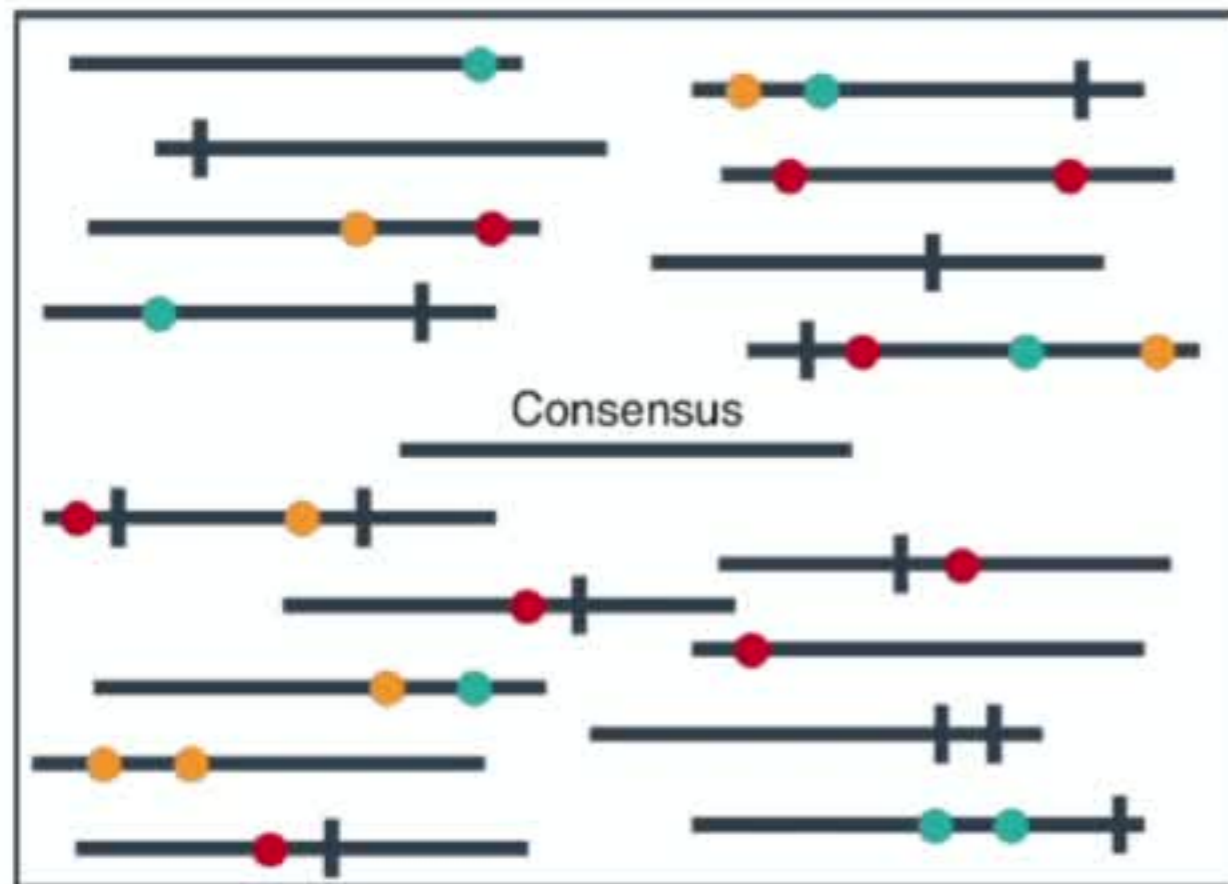
Understanding influenza co-infection  
dynamics and the role of semi-infectious  
particles (SIPs) and defective interfering  
particles (DIPs)

• • •

with Alex Farrell, Chris Brooke and Katia Koelle

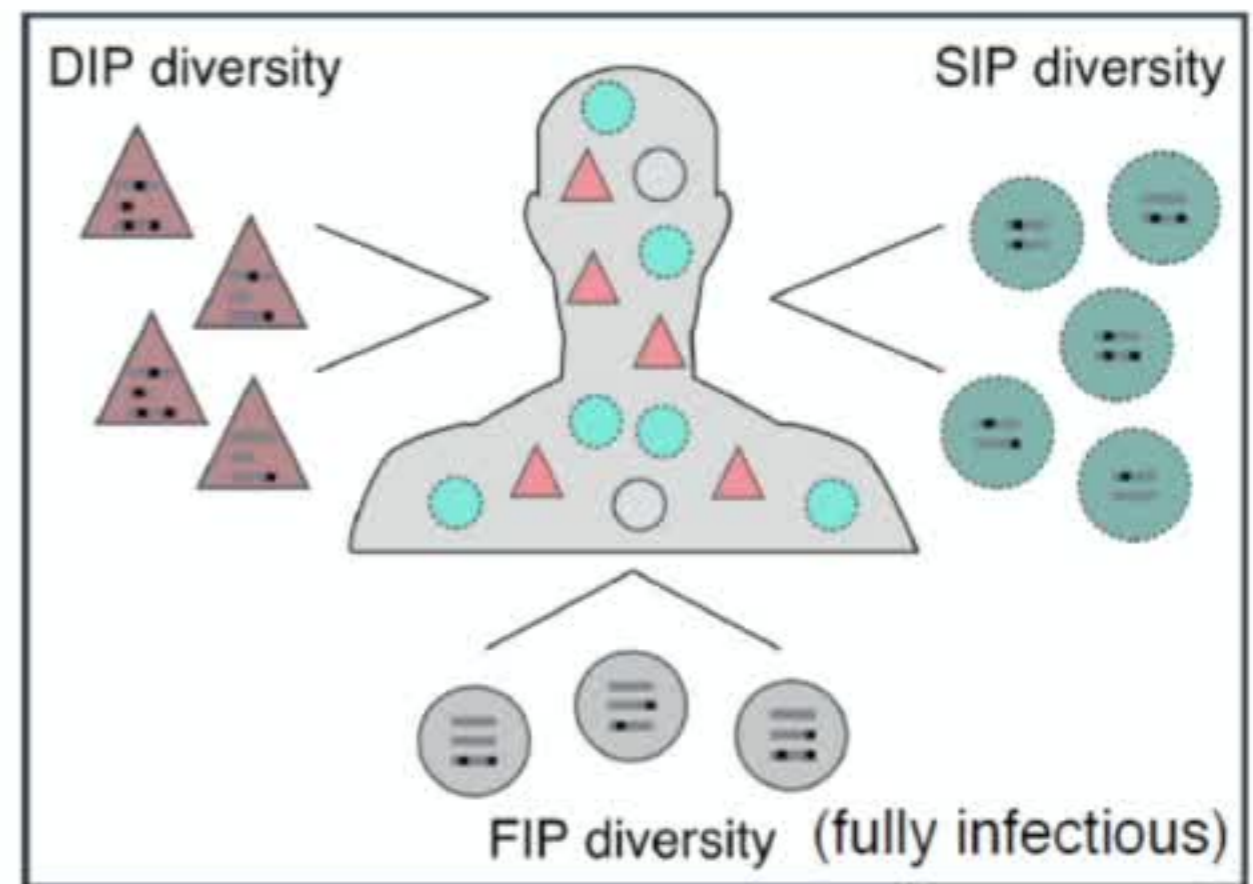
# IAV diversity

## Genetic Diversity



Sequence variation generated by the high mutation rate of the viral polymerase

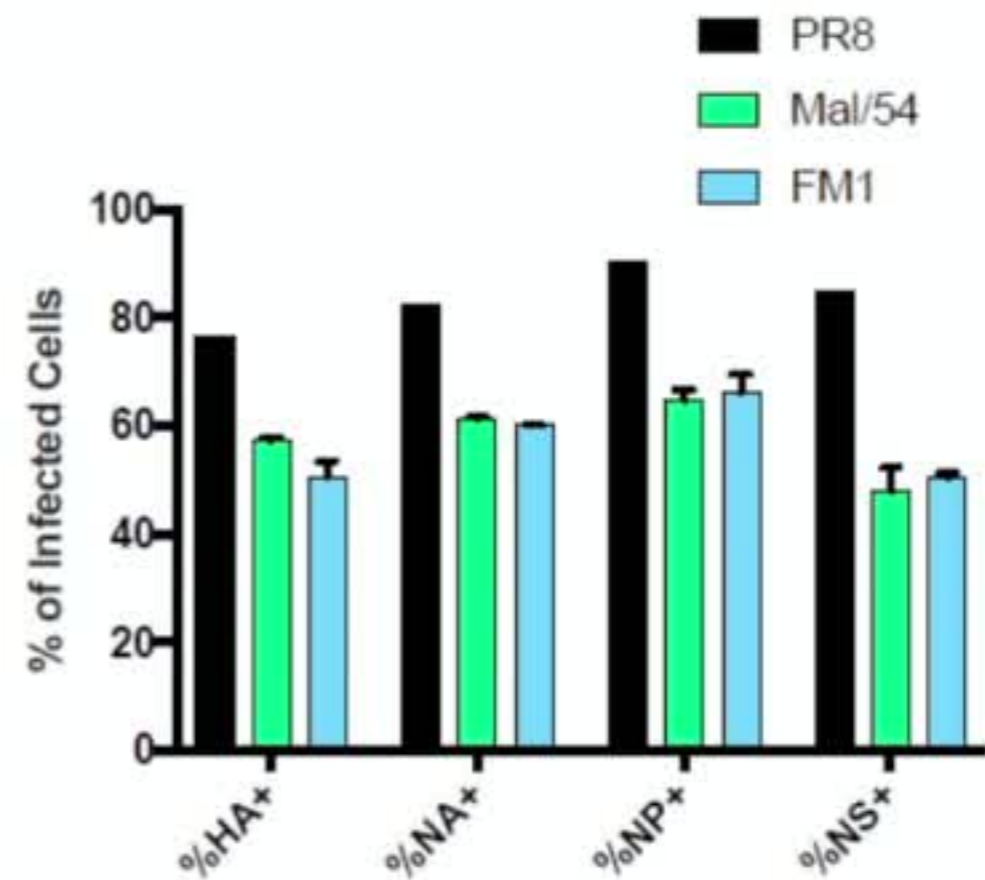
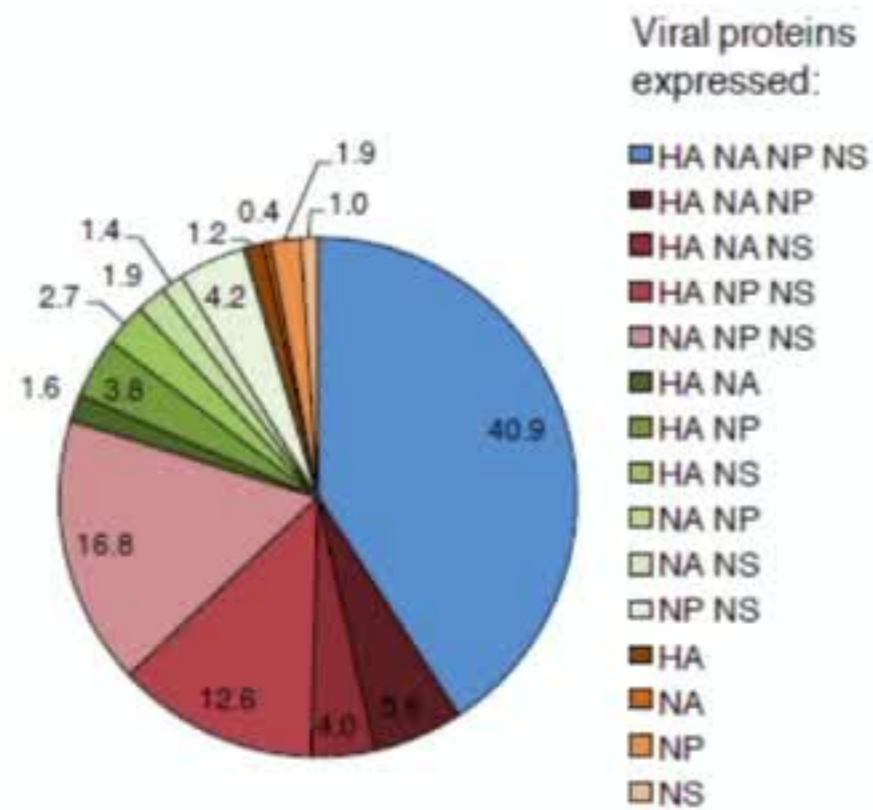
## Genomic Diversity



Variation in the genomic content and gene coding capabilities of individual virions

# Vast majority of IAV particles (70-99%) are “non-infectious”

**Semi-infectious particles (SIPs)** – virions that express a limited subset of essential viral genes

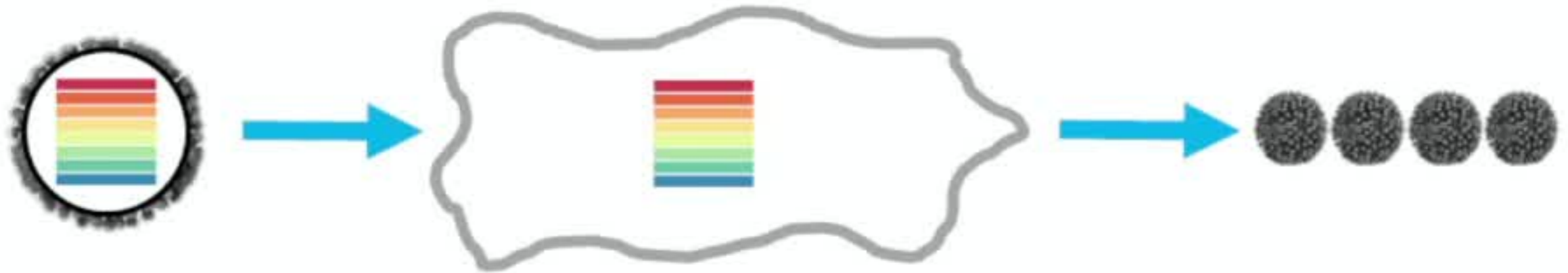


Brooke et al. (2013) *JVI*

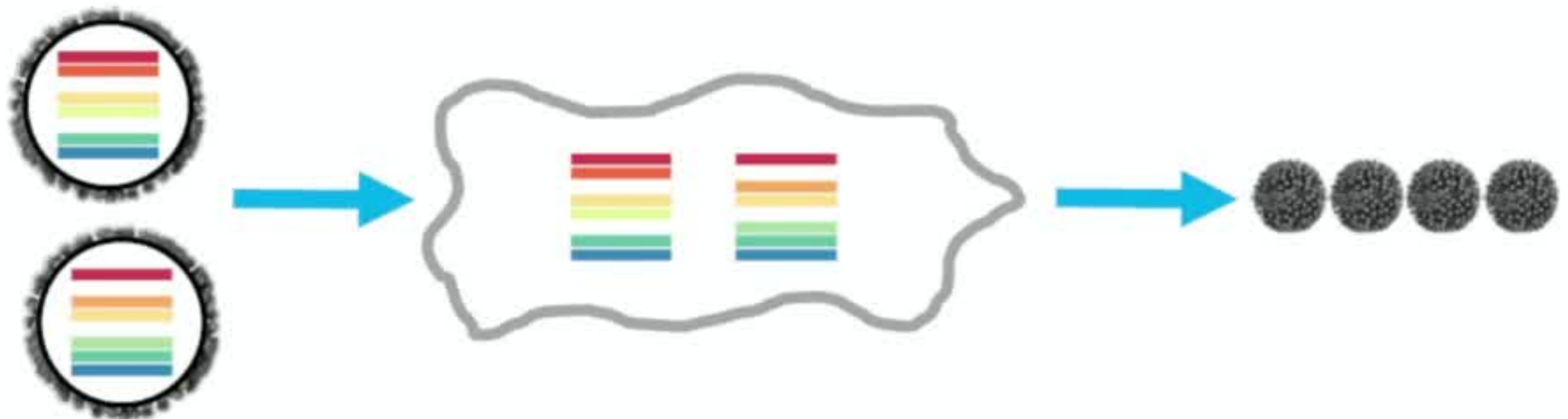
# Ways of generating a productive infection

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I. Infection of a cell with a fully infectious particle (FIP)



II. Infection of a cell with multiple semi-infectious particles (SIPs)



Cellular co-infection and viral complementation are critical for productive IAV infection

# Questions

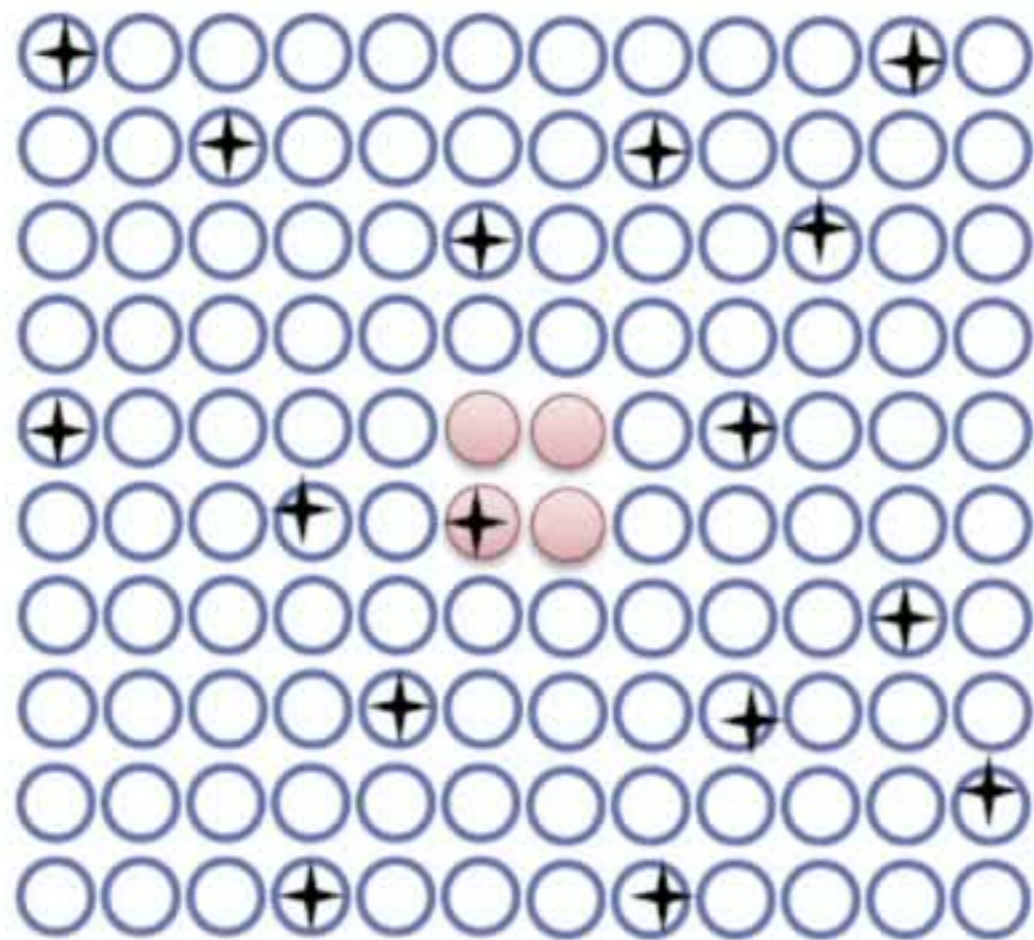
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- To what extent SIPs contribute to viral load?
- What is the appropriate model to describe coinfection in a host?
- Is there an advantage/disadvantage in producing large fraction of SIPs?



# Model assumptions

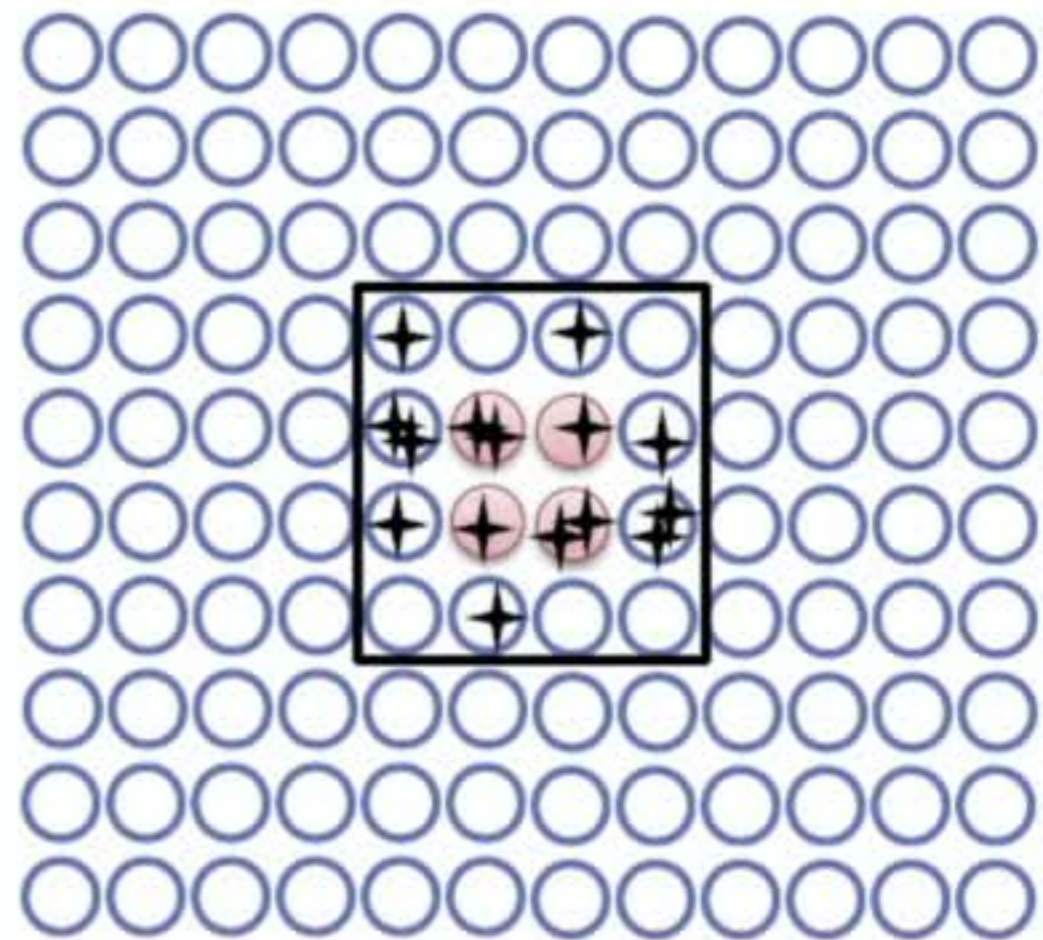
Homogeneous mixing – low frequency of coinfection



Infection in a host

○ Target cells    ● Infected cells    ✦ Virus

Target cell saturation – high frequency of coinfection

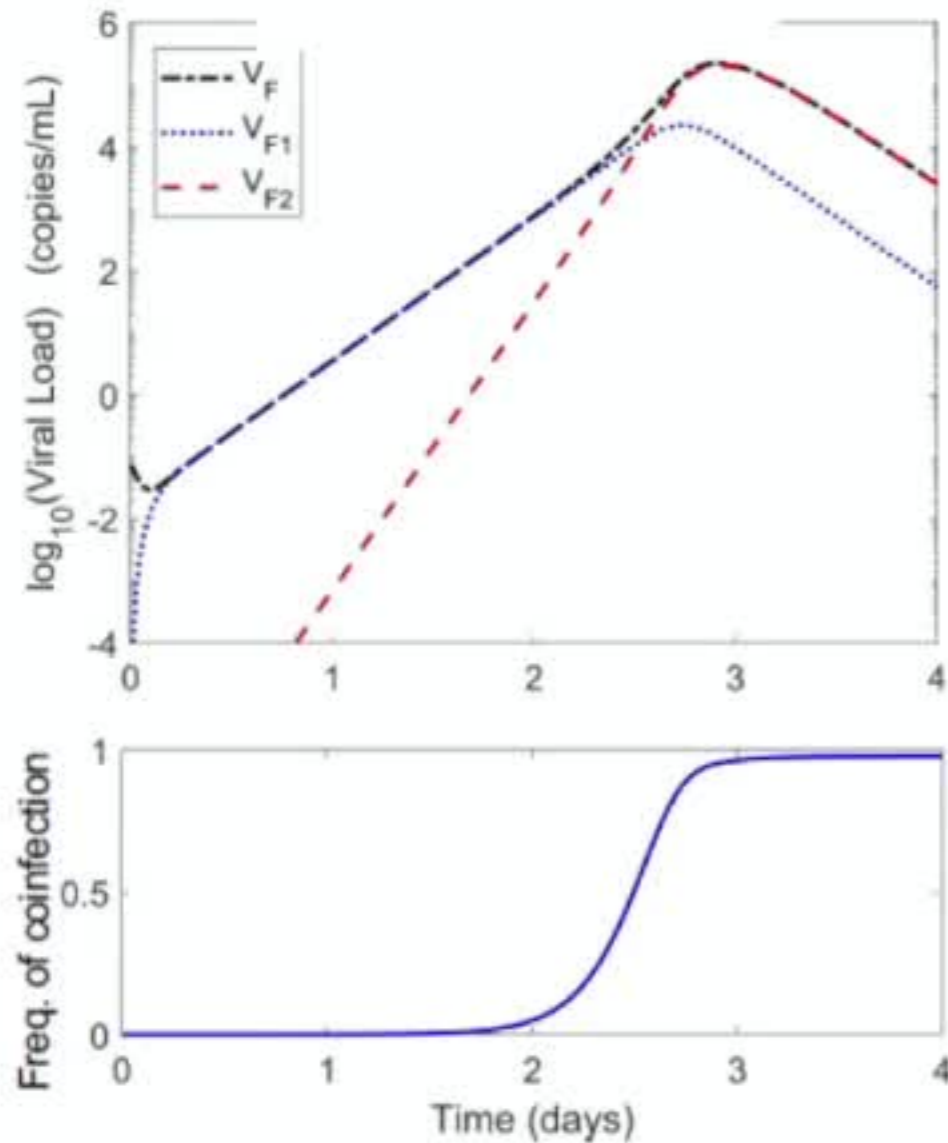


Infection in a host

□ Range of infection

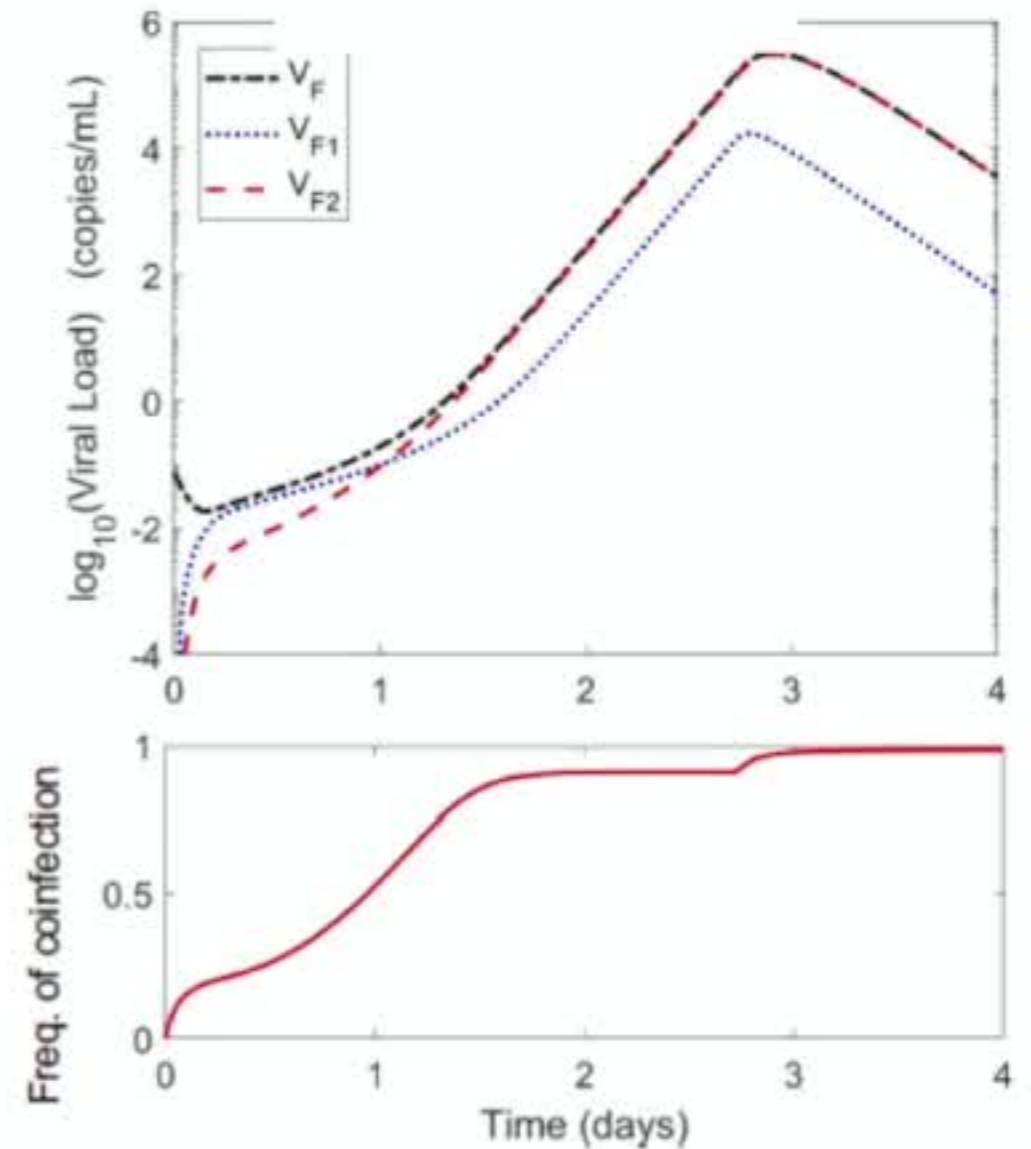
# Model results

Homogeneous mixing – low frequency of coinfection



- Freq. of coinfection is low until viral peak
- Viral load is mostly driven by (10-30%) fully-infectious particles (FIPs).

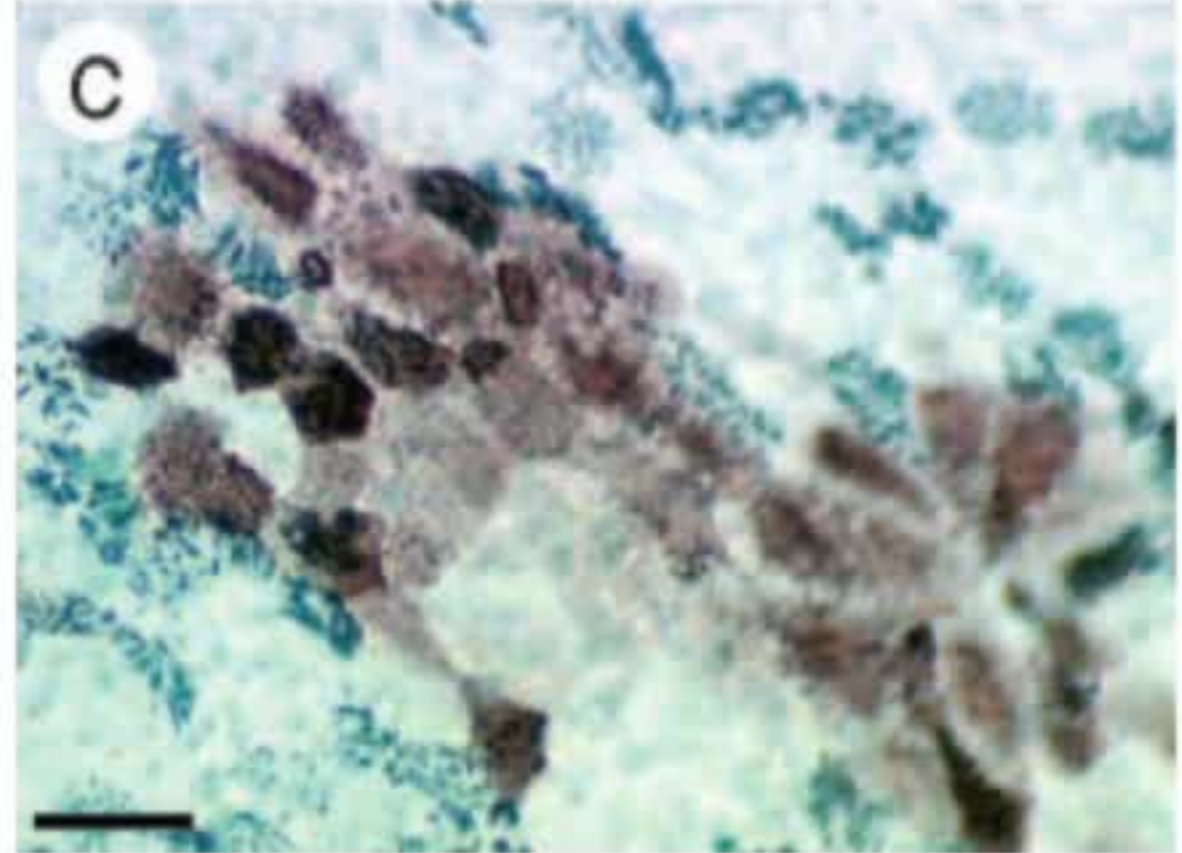
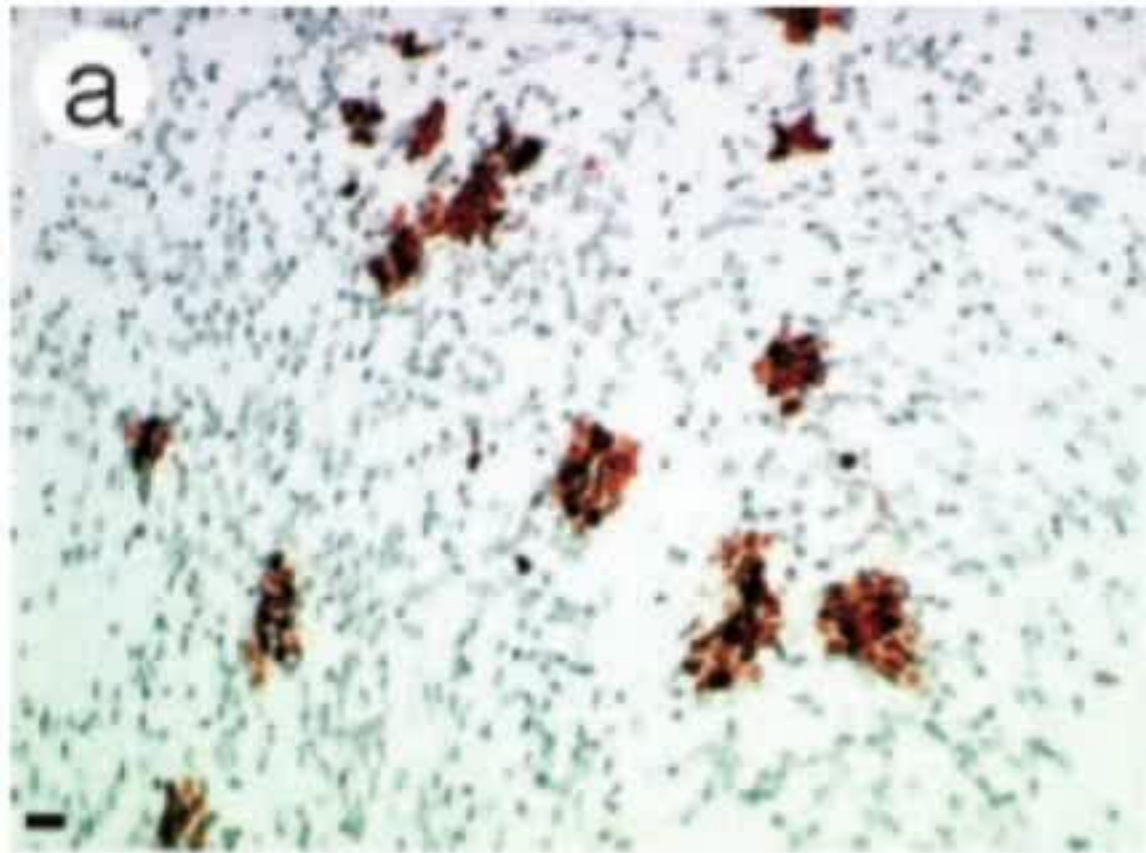
Target cell saturation – high frequency of coinfection



- Freq. of coinfection is high throughout the infection
- Viral load is mostly driven by (70-90%) semi-infectious particles (SIPs).

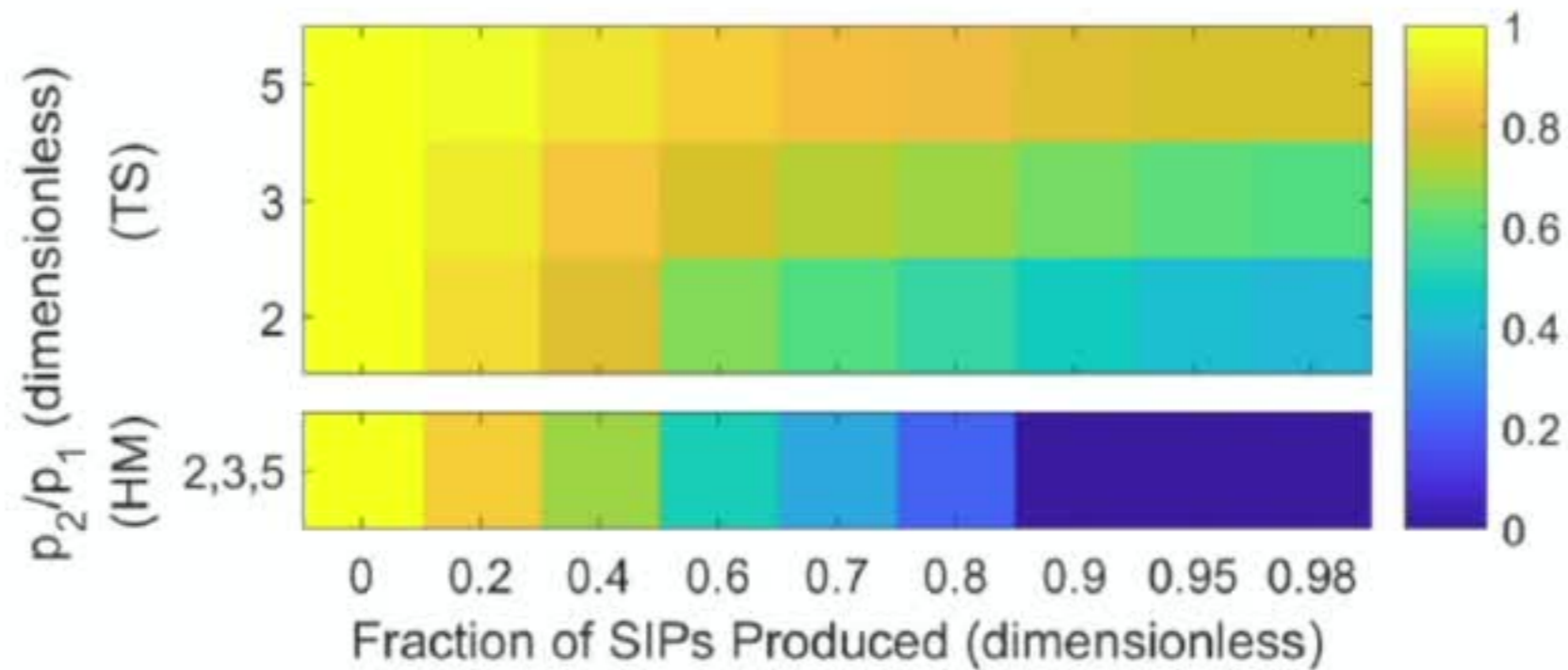
# IAV spreads in a spatial manner

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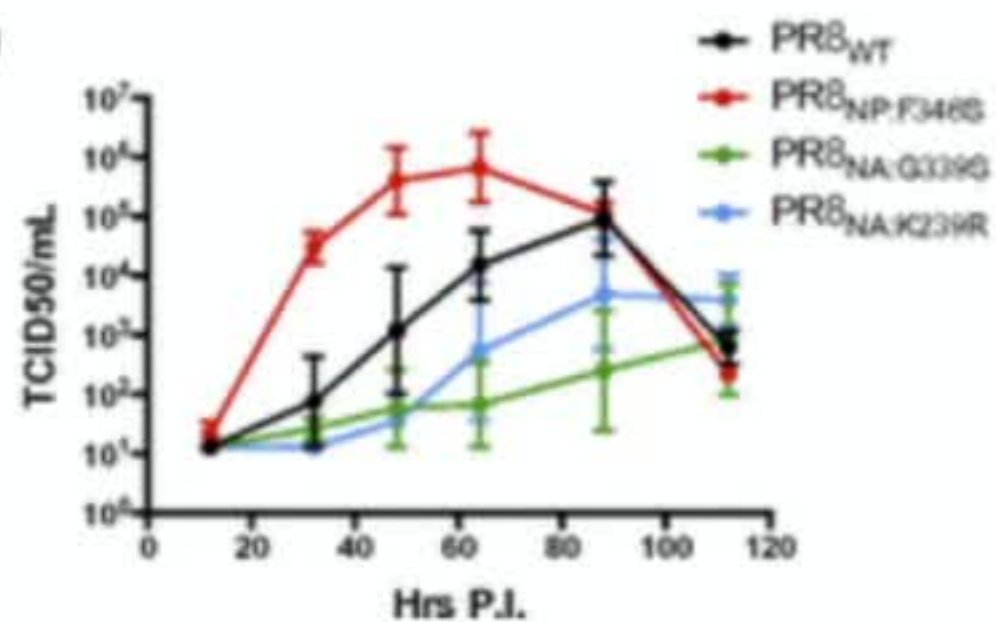


Matrosovich et al. (2004) *PNAS*

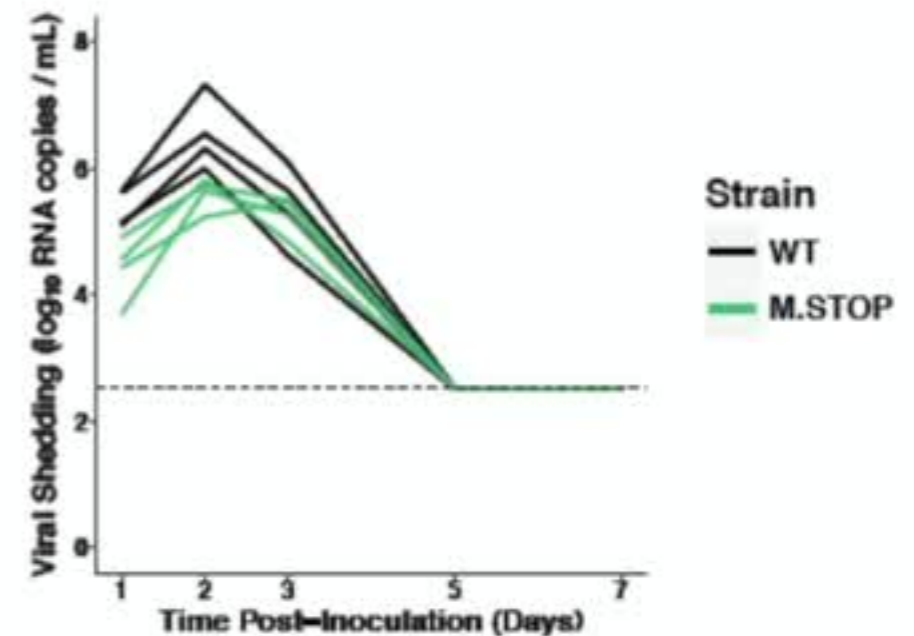
The model with a spatial structure predicts that large SIP production can have a minimal impact on viral fitness



D



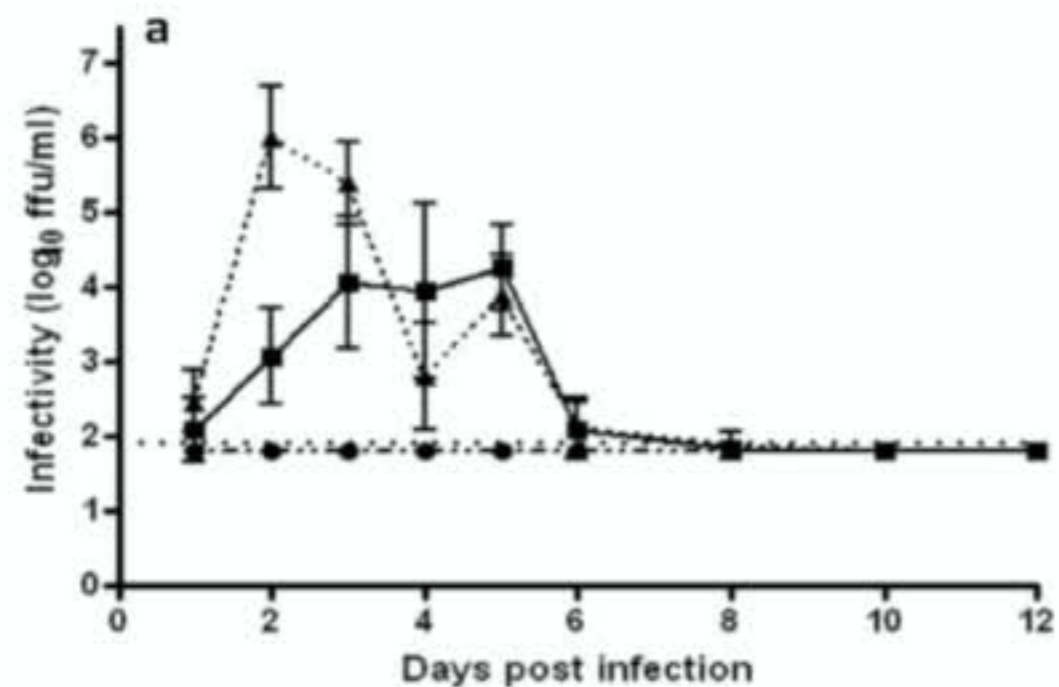
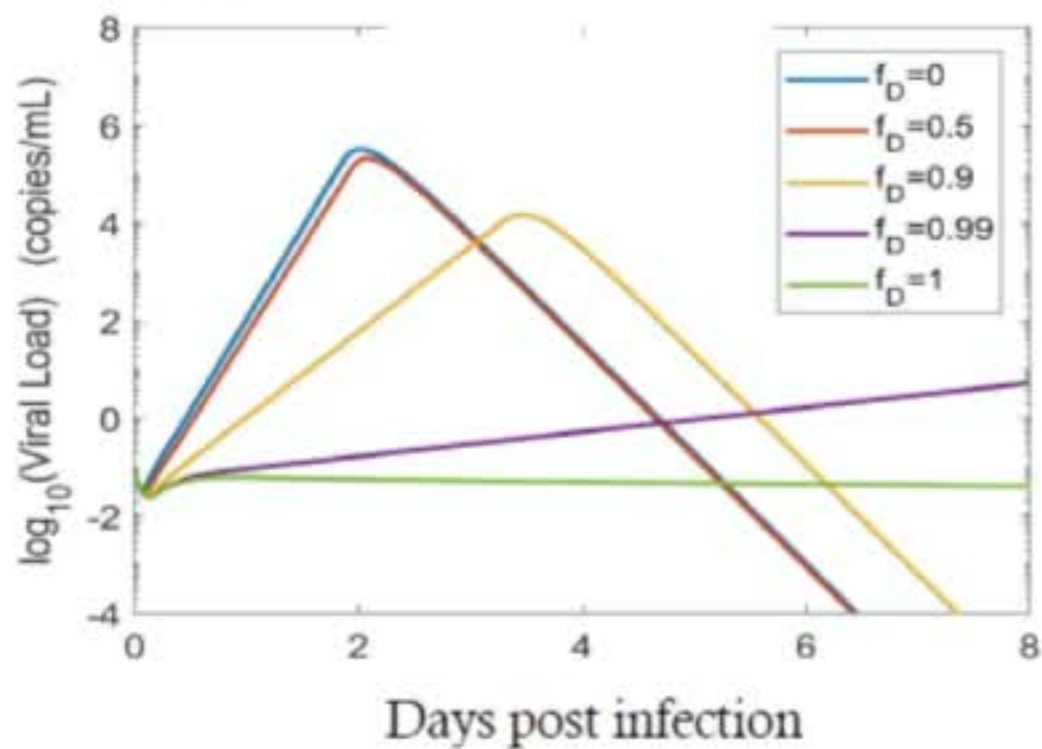
Brooke et al. (2014) PNAS



Jacobs et al. (2019) BioRxiv

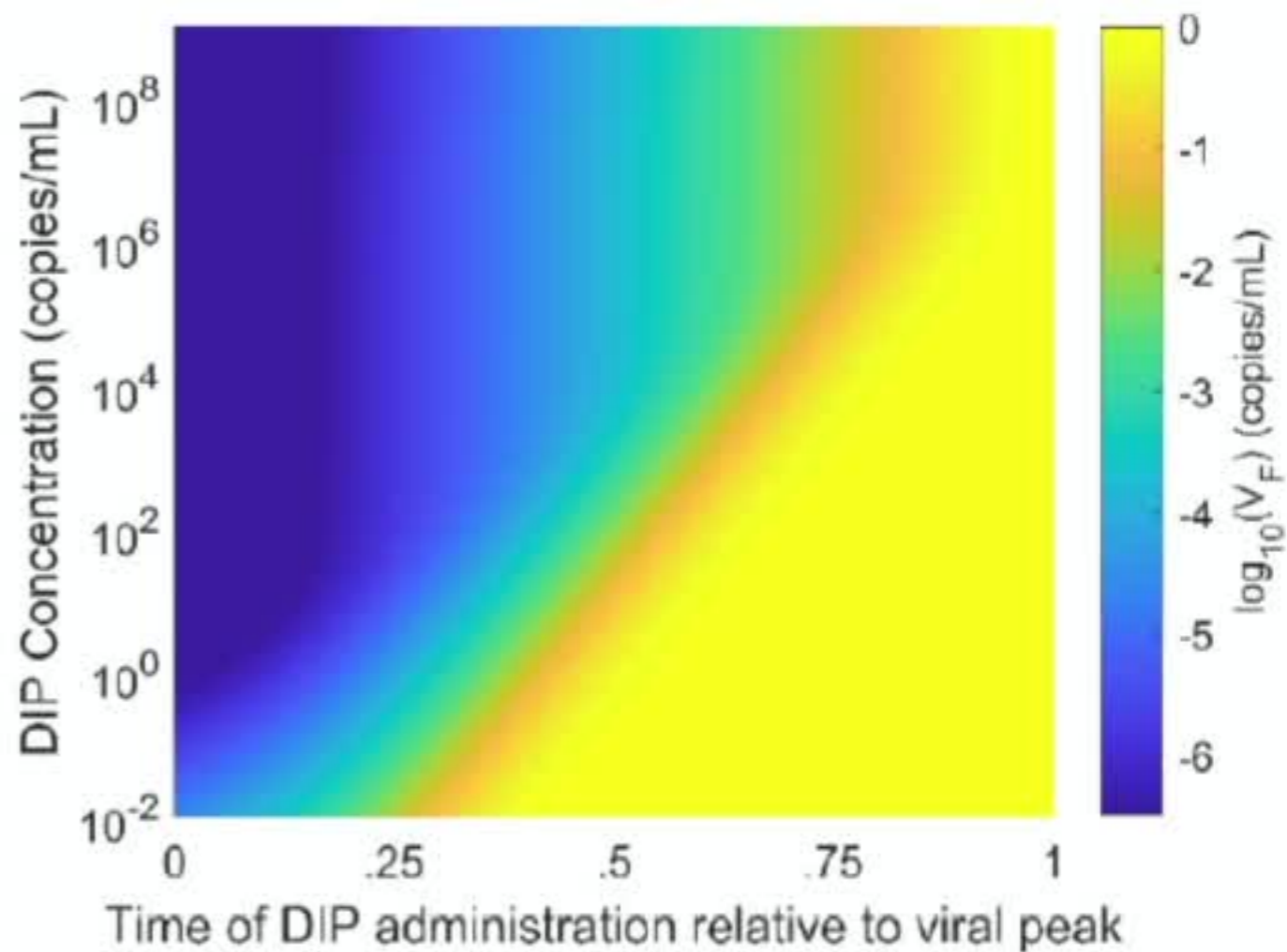


## Model predictions consistent with published experiments in ferrets

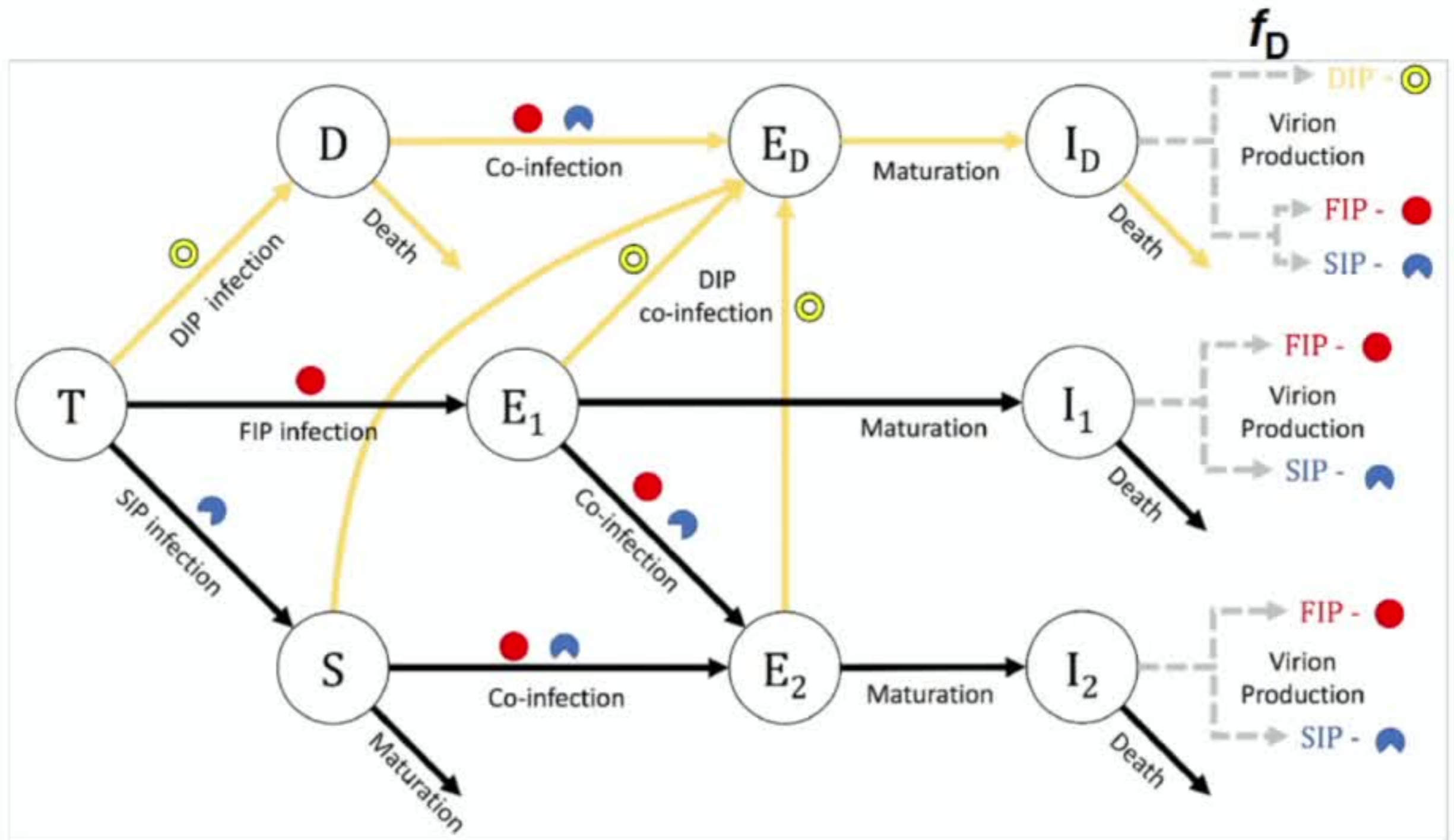


Dimmock et al. (2012) PLoS One

There exists only **a narrow window period before viral peak** for effective treatment of acute infections using DIPs.



# A within-host model incorporating FIPs, SIPs and DIPs

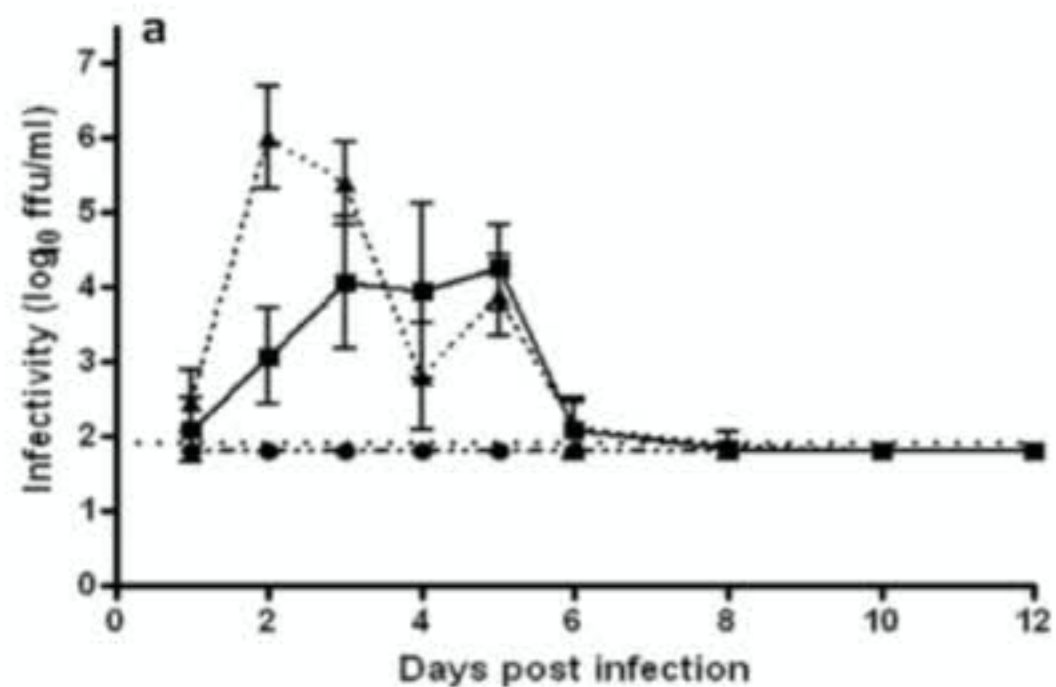
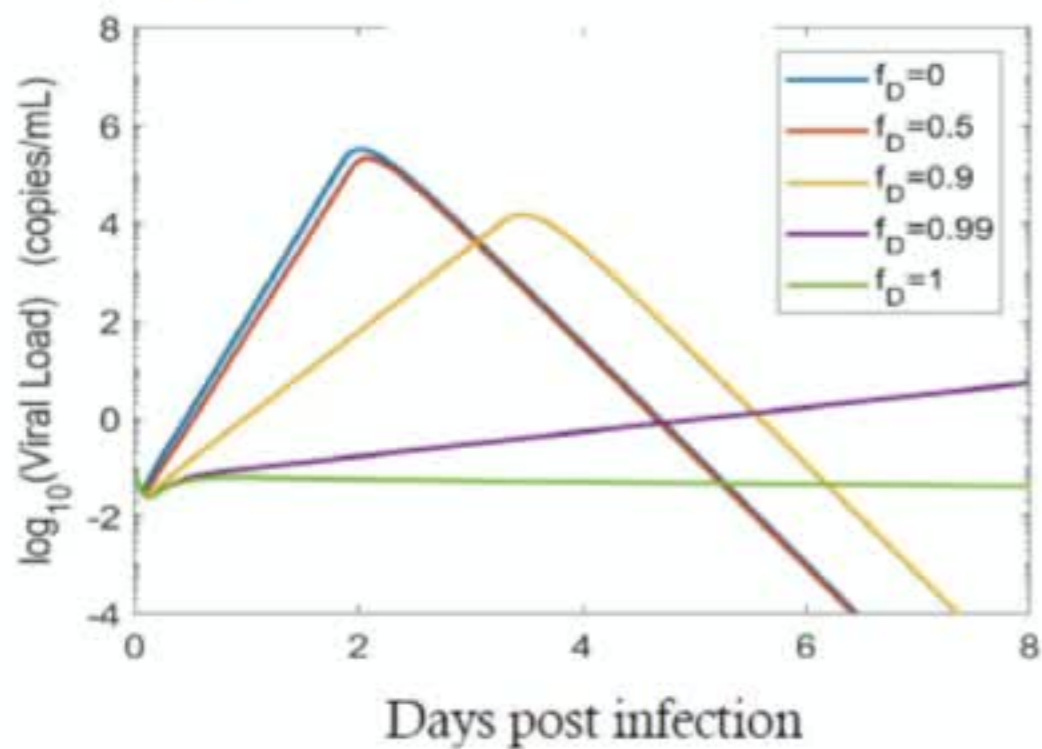


D: DIP infected cells  
 T: Target cells  
 S: SIP infected cells

$E_D$ : DIP co-infected cells in the eclipse phase  
 $E_1$ : FIP infected cells in the eclipse phase  
 $E_2$ : co-infected cells in the eclipse phase

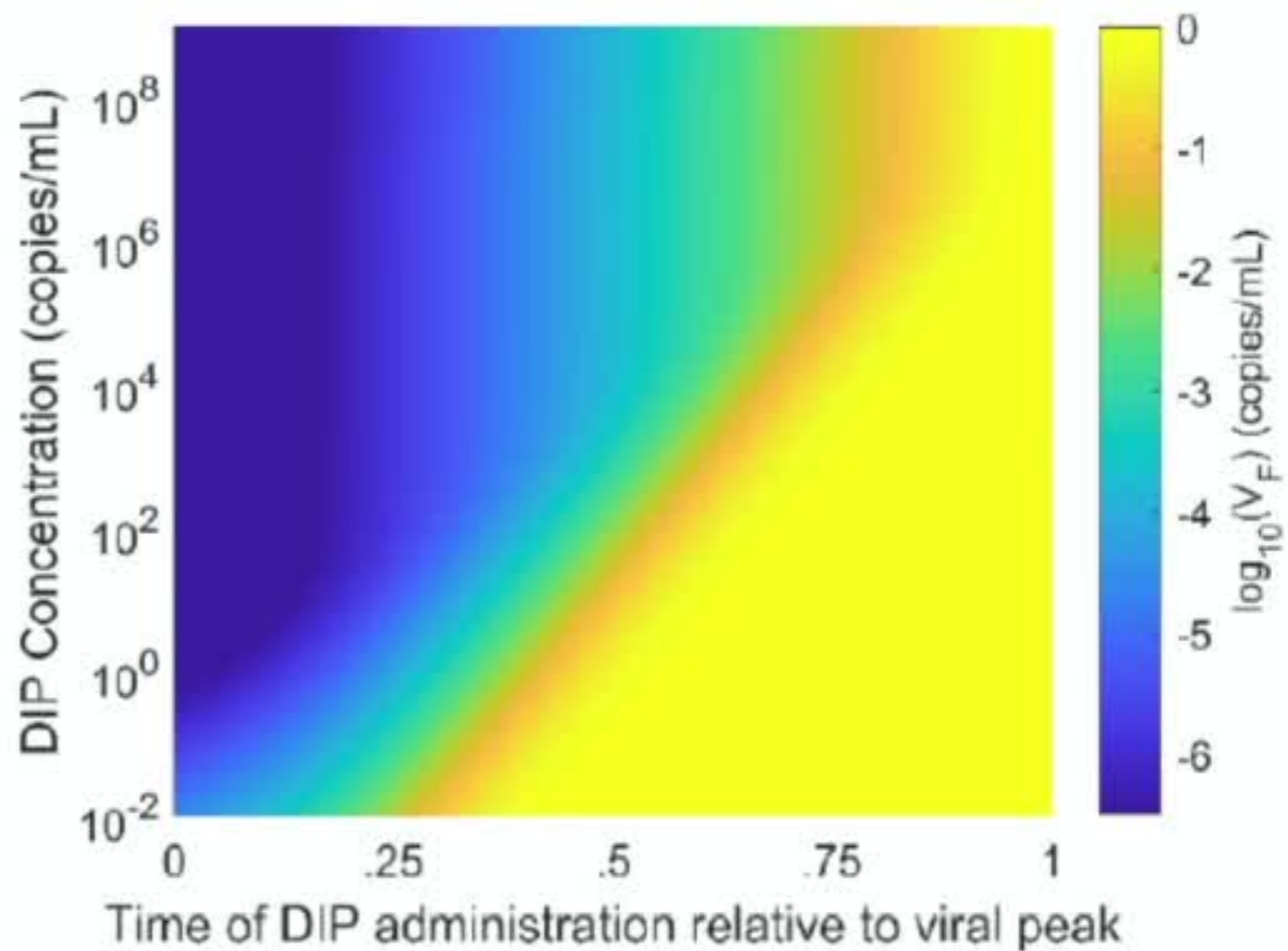
$I_D$ : productively DIP co-infected cells  
 $I_1$ : productively FIP infected cells  
 $I_2$ : productively co-infected cells

## Model predictions consistent with published experiments in ferrets



Dimmock et al. (2012) PLoS One

There exists only **a narrow window period before viral peak** for effective treatment of acute infections using DIPs.





Considering spatial structure is crucial to the understanding and prediction of the role of many biological processes

1. The role of co-infection and semi-infectious particles (SIPs) during IAV infection.
2. The effectiveness of therapeutics, such as DIPs.



*viruses*



*Review*

## **Causes and Consequences of Spatial Within-Host Viral Spread**

Molly E. Gallagher<sup>1</sup>, Christopher B. Brooke<sup>2,3</sup>, Ruian Ke<sup>4</sup> and Katia Koelle<sup>1,\*</sup>

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  - **Alex Farrell**
  - G. Michael Lavigne
  - Hayley Russell
  - Yufan Huang



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## Multiscale dynamics of infectious diseases, immune responses and therapeutics

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### Call for Papers Announcement

Infectious diseases infection involves spatial and temporal dynamics of entry, replication, spread and evolution of pathogens. These dynamics occur at spatial and temporal scales and at multiple levels of biological organization, i.e. the cellular level and the in-host level. Mathematical modeling has been critical to quantify the rates at which these processes occur, the role of immune responses and make precise predictions of the efficacy and the impact of therapeutics. This special issue collects recent advances of a broad range of mathematical/statistical modeling studies of infection disease dynamics, immune responses and/or the impact therapeutics.

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