

# Prediction of Abnormal Cardiac Rhythms with a 1D Dynamical Model

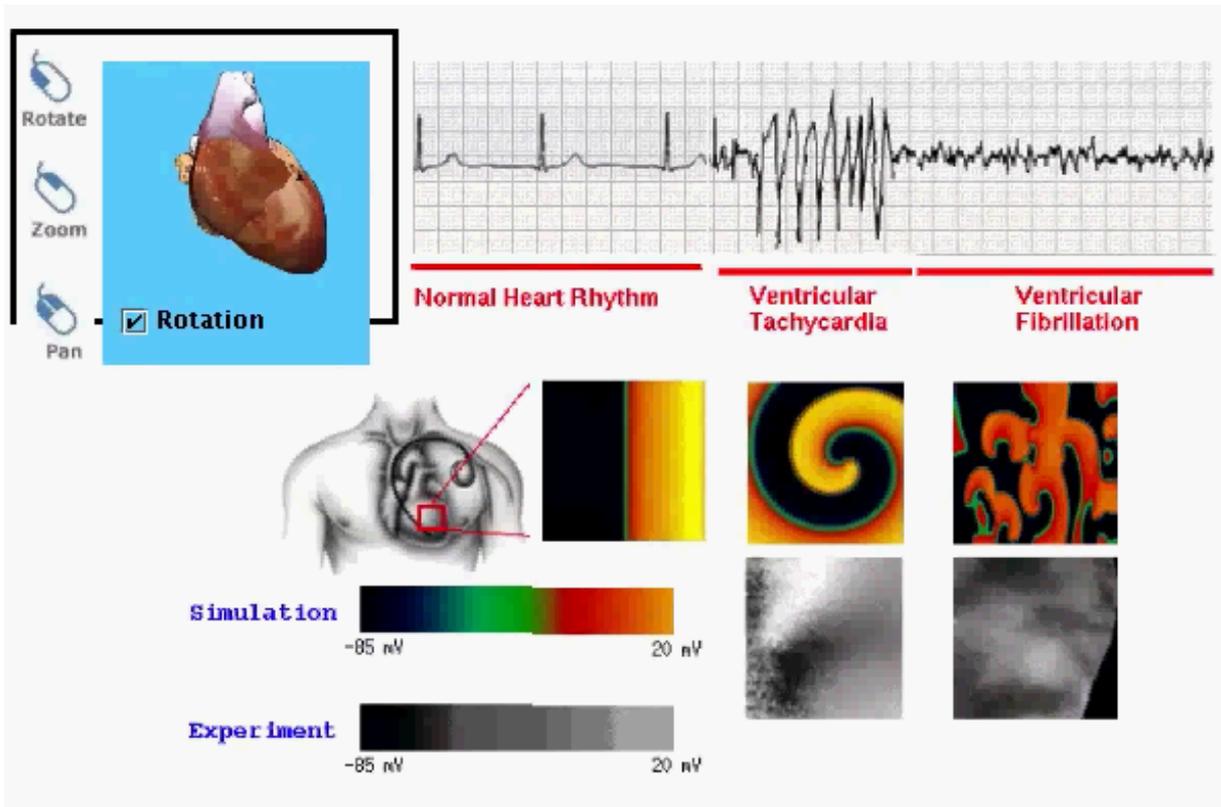
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Collaborators: Anna Gelzer (UPenn), Flavio Fenton (GA Tech), Wei Qian (UDel), Weiye Lin (BS, Cornell), Robert Gilmour, Jr. (UPEI), Niels Otani (RIT), Effiba Armah (BS, RIT)

# Motivation

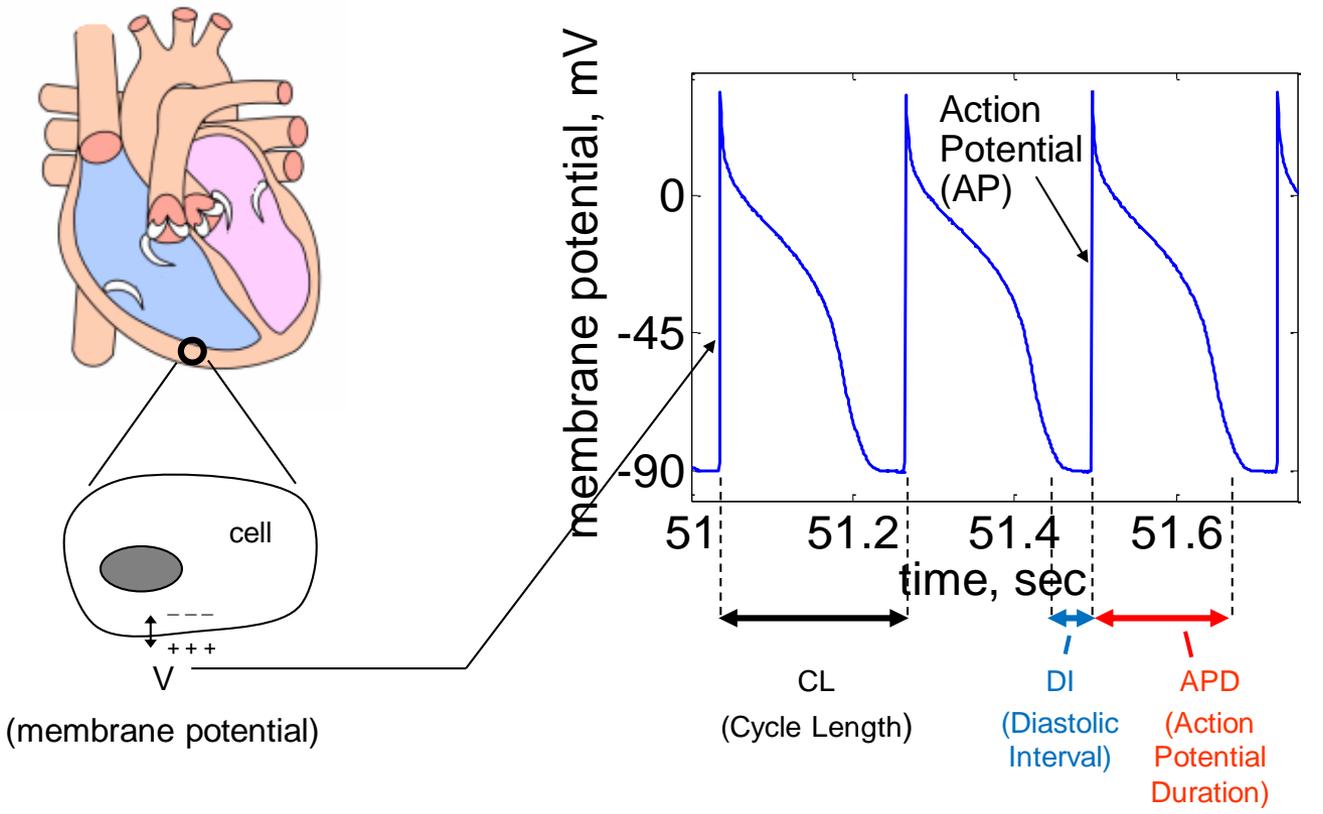
- Ventricular fibrillation (VF) is an uncoordinated heart rhythm that results in loss of effective blood pumping
- Sudden cardiac death (SCD) is a leading cause of death in the industrialized world, responsible for approx. 180000--450000 deaths in US annually
- A substantial proportion of SCDs are thought to be due to VF
- SCDs are rare, in that they affect up to  $\sim 0.1\%$  of the US population each year
- VF is often preceded by a sequence of premature beats

# Ventricular Fibrillation



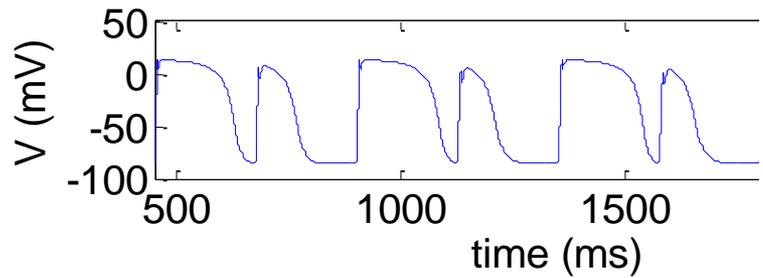
c/o Flavio Fenton and Elizabeth Cherry, <http://thevirtualheart.org>

# Terminology



(membrane potential)

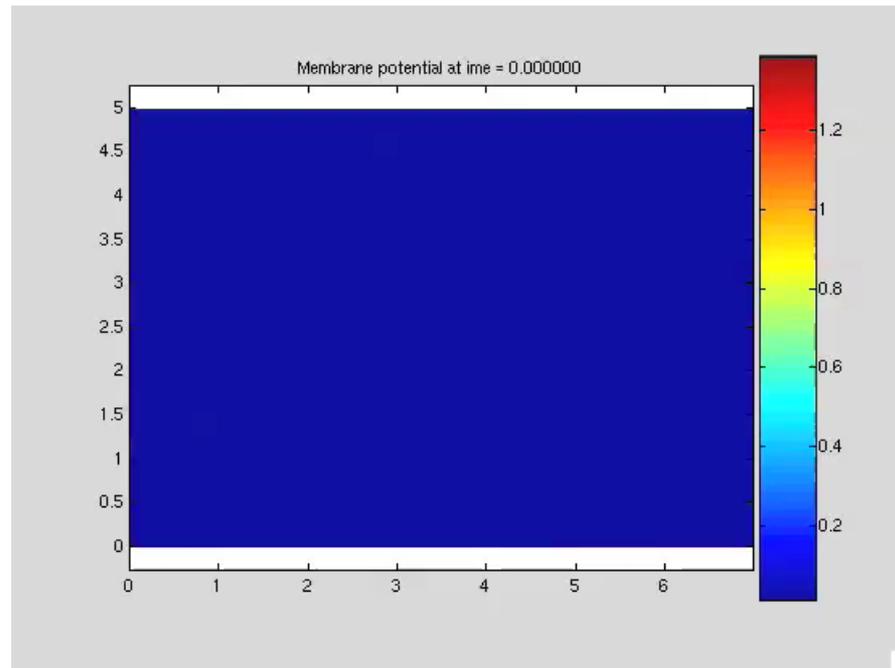
Alternans: beat-to-beat alternation in APD



# Progression to VF

- Proposed mechanism: Premature beats induce alternans, conduction block, leading to reentry and VF

Simulated  
ventricular  
tissue  
(2D sheet)



c/o Niels Otani

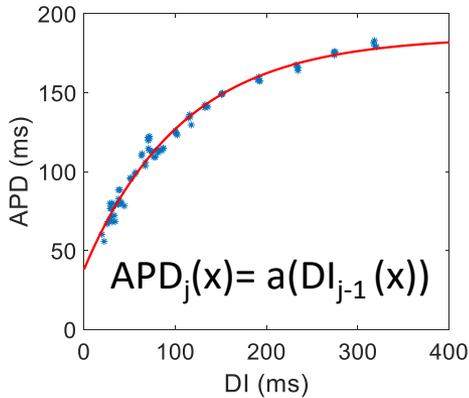
# Background

- Many models of cardiac electrical activity have been developed
  - ODE, PDE, difference equations, cellular automata, etc.
  - Phenomenological: lower dimensional, e.g. Noble model (1962), 4 variables per cell
  - Detailed: higher dimensional, e.g. Iyer-Mazhari-Winslow model (2004), 67 variables per cell
- Our approach
  - Use simple nonlinear 1D model to predict alternans, block, VF, following premature beats *in vitro* (Muñoz, et al., 2018)
  - Advantages of simple model: few parameters, and can quickly simulate large numbers of different premature beat sequences

# Coupled Maps Model

(Fox *et al.*, 2003, Otani, 2007)

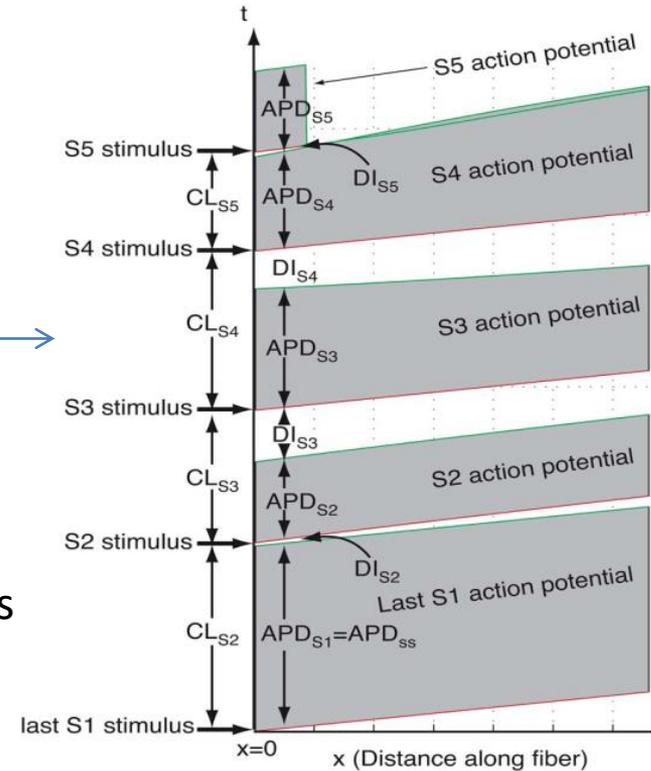
action potential duration  
(APD) restitution function



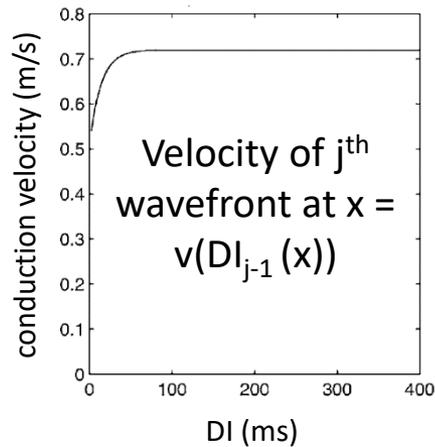
$x$  = distance along fiber  
 $j$  = cycle index

Coupled  
Maps Model

space-time plot



conduction velocity (CV)  
restitution function



Inter-stimulus intervals  
( $CL_2, CL_3, CL_4, CL_5$ )

# Coupled Maps Model

(Fox *et al.*, 2003, Otani, 2007)

$x$  = distance along fiber (7cm,  $\Delta x = 0.025$ cm)

$j$  = cycle index

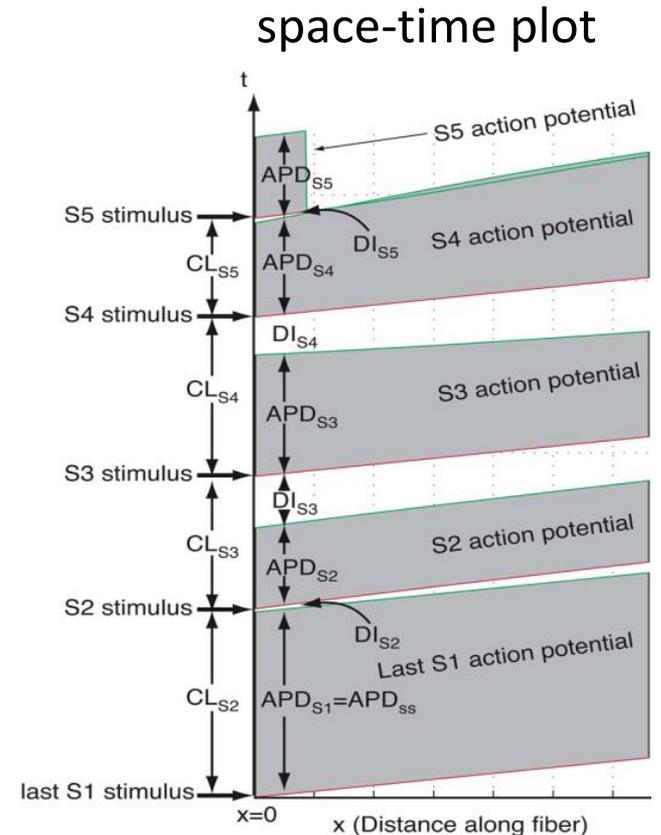
$i$  = cell index

$$APD_j(x_i) = a(DI_{j-1}(x_i))$$

$$CL_j(x_i) = CL_j(x_0) + \sum_{k=1}^{i-1} \Delta x / v(DI_j(x_k))$$

$$- \sum_{k=1}^{i-1} \Delta x / v(DI_{j-1}(x_k))$$

$$DI_j(x_i) = CL_j(x_i) - APD_j(x_i)$$



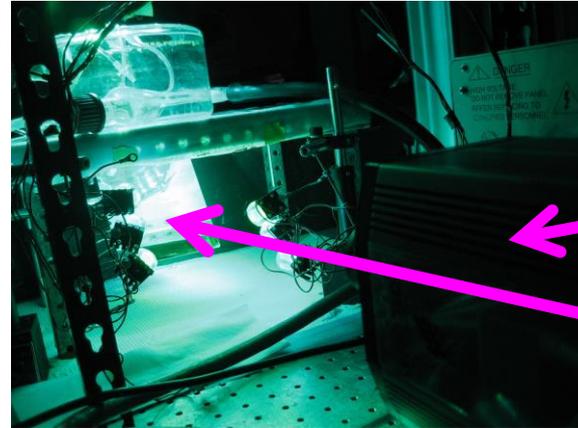
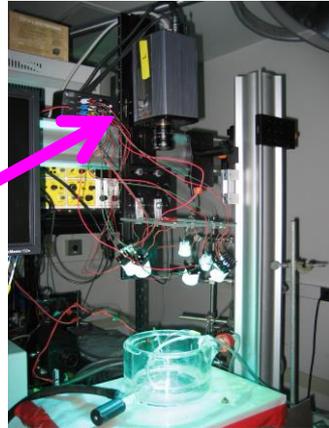
**Premature stimulus sequences that caused distal block in the model were found to be likely to induce VF *in vivo* (Gelzer, *et al.* 2008, 2009)**

# Background

- Gelzer et al. (2008, 2009): premature beat sequences that caused block in the coupled maps model were found likely to induce VF in canine hearts in vivo
- Shortcoming of in vivo setup: can only take measurements at two locations. Can detect VF, but not alternans or block
- Solution: use optical mapping in vitro (n=9 right ventricles), allows detection of alternans, block, VF

# Optical Mapping Setup

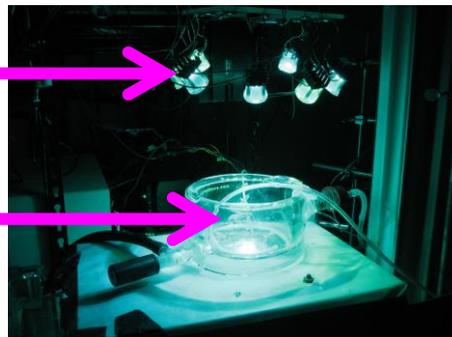
Cascade 128+ camera



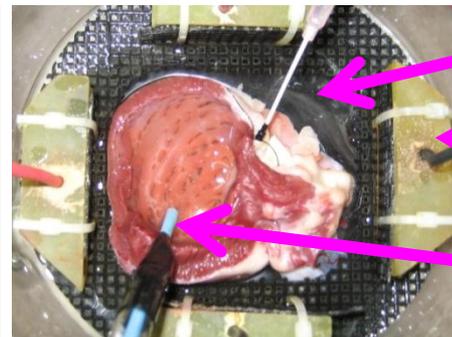
Cascade 128+ camera

mirror

LED units



heat bath including optical-grade bottom



perfusion inflow

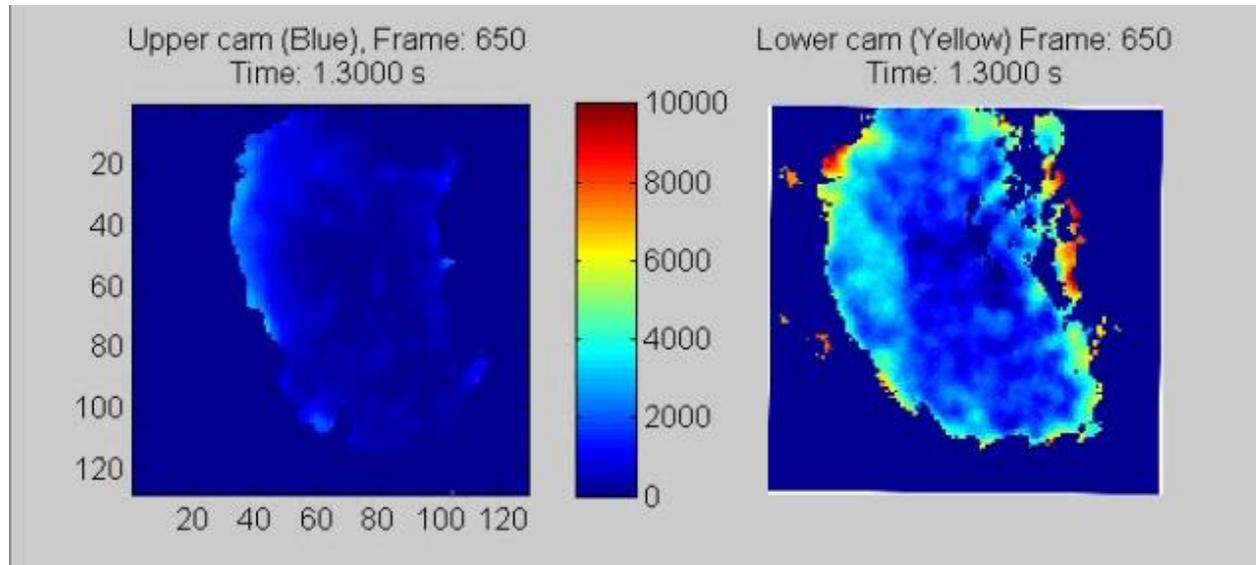
far-field stimulation electrode

bipolar stimulation electrode

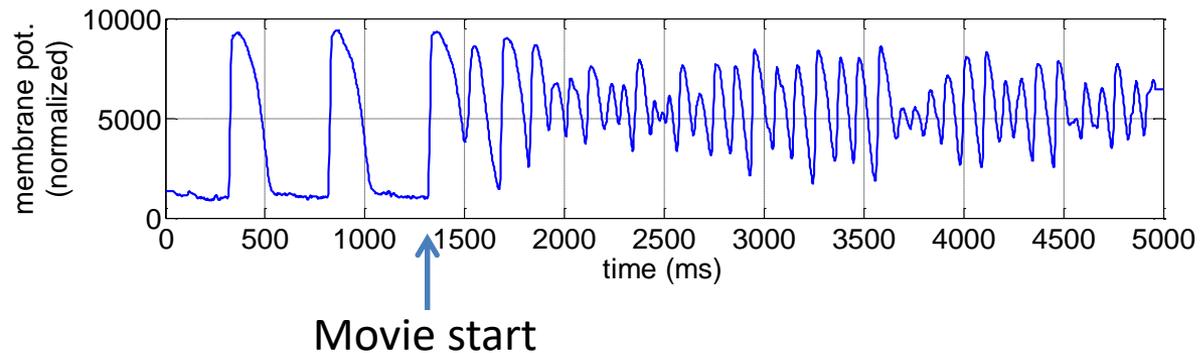
# Optical Data Example

Endo

Epi



2011-08-09\_Exp000\_Rec084  
horiz = 80 vert = 90



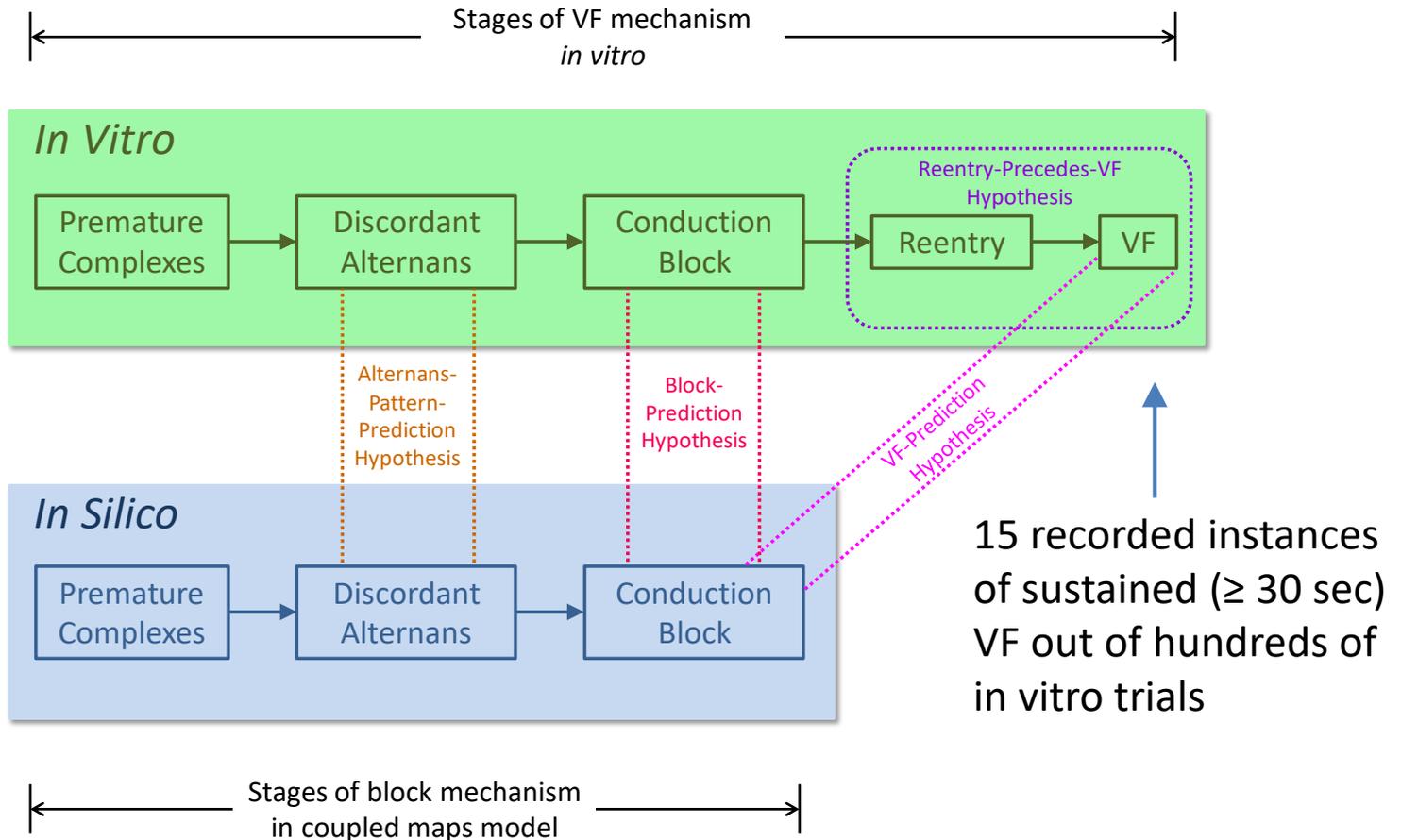
# Methods

- For purposes of comparison, use same methods as in past *in vivo* studies
- Collect APD restitution data from *in vitro* preps
- Use historical CV restitution data (Riccio et al., 2009)
- Test different combinations of premature stimulus timings *in vitro*
- Compare model simulation results with *in vitro* measurements

# Methods

- Alternans Prediction
  - Compare model predictions with observations for randomly-selected trials
  - Use Bayesian approach to compute posterior probabilities that measured APs followed any given pattern
- Block Prediction
  - Compare model predictions with observations for randomly-selected trials
  - Use generalized estimating equation (GEE) logistic-regression approach
  - GEE model: dependent variable is measured block, explanatory variable is model-predicted block, with clustering by dog
- VF Prediction:
  - Run >100000 simulations and partition premature beat sequence space into blocking/non-blocking categories. Compare blocking/non-blocking predictions with VF/no-VF observations
  - A GEE logistic regression approach was used here as well

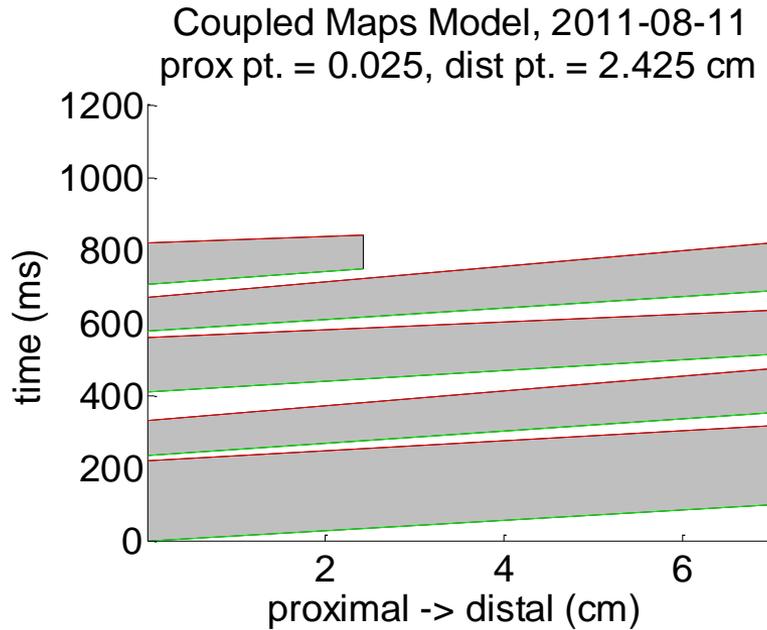
# Model vs. Experiment



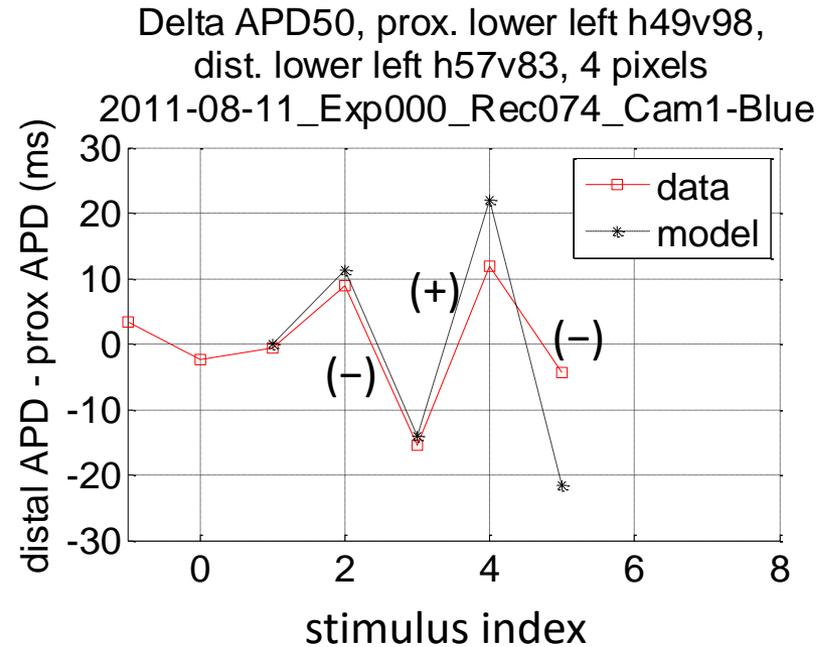
Muñoz, et al., Discordant Alternans as a Mechanism for Initiation of Ventricular Fibrillation In Vitro, *Journal of the American Heart Association*, 2018

# Simulated vs. Measured $\Delta$ APDs

## Space-time plot



## $\Delta$ APD plot



# Report Card for Model

- Alternans:
  - Sign patterns for APD and DI spatial gradients were more likely to follow model-predicted pattern (posterior probs. of **91%** and **82%**) than would be expected if none of the possible patterns were preferred ( $1/8 = 12.5\%$ )
- Block:
  - Wald test applied to GEE model: effect of coupled maps model prediction was significant ( $p < 1 \times 10^{-15}$ , **coeff. 44.36**)
  - Accuracy = (# correct predictions)/(# total events) = **72%**
  - Model predicted fewer instances of block (50%) than actually occurred (78%)
- VF:
  - Wald test applied to GEE model: effect of coupled maps model prediction was significant ( $p = .0046$ , **coeff. 1.63**)
  - Accuracy = (# correct predictions)/(# total events) = **79%** in vitro (compare with 90% in vivo)
  - Model predicted more instances of VF (21%) than actually occurred (8%)

# Possible Improvements to Model

- Calibrate APD restitution (APDR) parameters from location closer to electrode
- Calibrate CV restitution (CVR) parameters from in vitro data. Main obstacle: only have 2D imaging of 3D CV quantity
- Allow spatial variation in APDR and/or CVR parameters
- Include electrotonic effects

# Parameter Sensitivity Ratios

- Determine which parameters or settings have larger impacts on predicted values

- For quantity  $q$  and parameter  $p$ , sensitivity ratio is

$$\frac{\delta q}{\delta p} = \frac{q - q_0}{q_0} \frac{p_0}{p - p_0} = \frac{\Delta q}{\Delta p} \frac{p_0}{q_0}$$

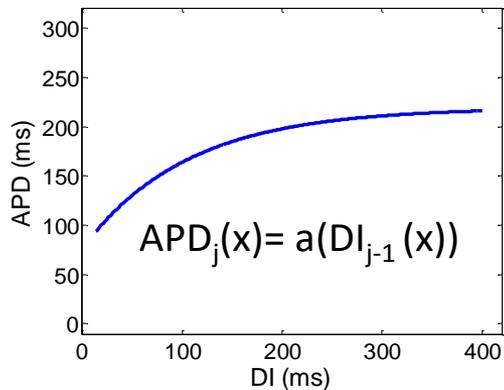
- Let  $q$  = mean magnitude of alternans gradient;  $N=4$  premature stimuli

$$q = \frac{1}{N-1} \sum_{i=2}^N \left| \frac{\Delta APD_i}{\Delta x} \right|$$

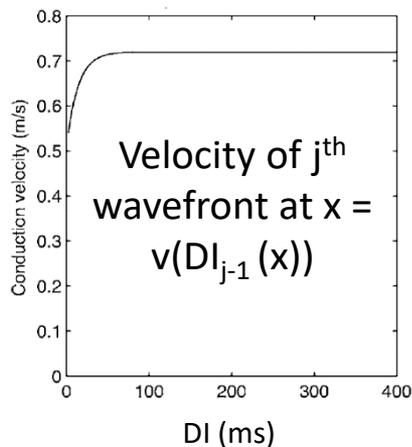
- Larger  $q$  means more severe alternation

# Parameter Sensitivity Ratios

action potential duration  
(APD) restitution function



conduction velocity (CV)  
restitution function



- $APD = a(DI) = A + Be^{-DI/C}$
- $CV = v(DI) = \alpha (1 - e^{-(DI-\beta)/\gamma})$
- Rest. params.  $A, B, C, \alpha, \beta, \gamma$
- Example: sensitivity ratios for one trial, +5% parameter perturbation

$\delta q/\delta A$	$\delta q/\delta B$	$\delta q/\delta C$	$\delta q/\delta \alpha$	$\delta q/\delta \beta$	$\delta q/\delta \gamma$
0.0	2.7	-1.5	-0.9	-0.6	1.8

# Conclusions and Future Work

- Model is a significant predictor of VF
- Predicts measured alternans but under-predicts conduction block
- Possible application: improved stimulus algorithms for anti-arrhythmic devices
- Future work: compute parametric sensitivities over a wider range of conditions

# Acknowledgments

## Collaborators

- Students:
  - Effiba Armah (BS, RIT)
  - Weiye Lin (BS, Cornell)
  - Min Chul Shin (BS, Cornell)
- Faculty:
  - Anna Gelzer (UPenn)
  - Flavio Fenton (GA Tech)
  - Robert Gilmour, Jr. (UPEI)
  - Niels Otani (RIT)
  - Wei Qian (UDel)

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- Thank you for attending!
- Questions?