

# Mathematical Modeling of Cell Density in Diffusion Weighted Imaging (DWI) - Clinical Application in Crossed Cerebellar Diaschisis

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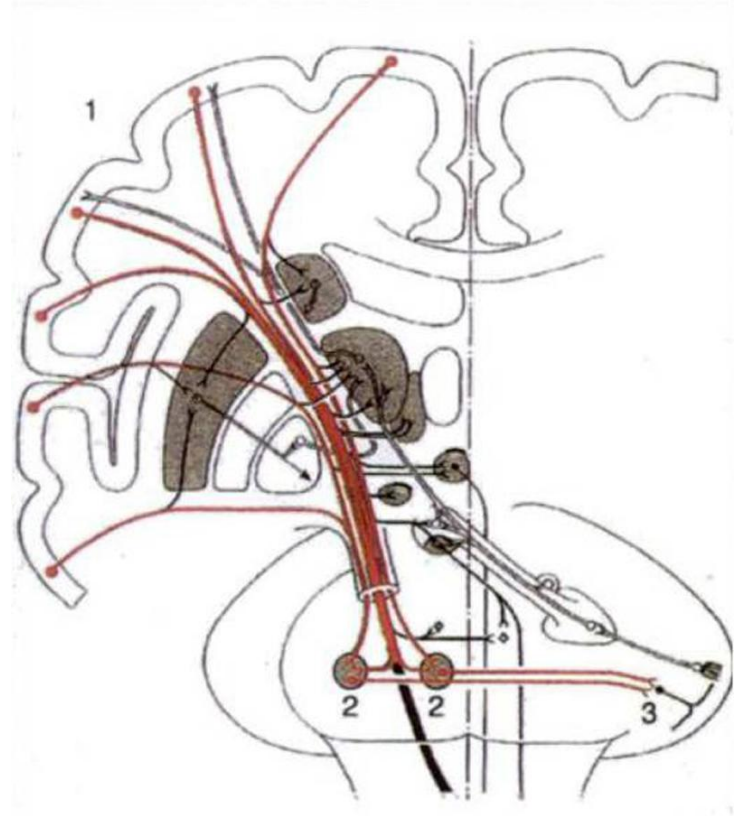
# Outline

- [Introduction](#)
- [Purpose](#)
- [Methods](#)
- [Results](#)
- [Discussion](#)
- [References](#)



# Introduction

- Crossed cerebellar diaschisis (CCD) refers to transneuronal degeneration in the cerebellum as a result of contralateral cortical pathology and disruption of the corticopontocerebellar pathway.
- Stroke patients with CCD have been found to have a worse prognosis in multiple studies (e.g., Sobesky et al., 2005).
- Our aim in this study is to propose a modeling approach for accurate detection of CCD on routine MRI scans with DWI.



Rabin et al., 1998.



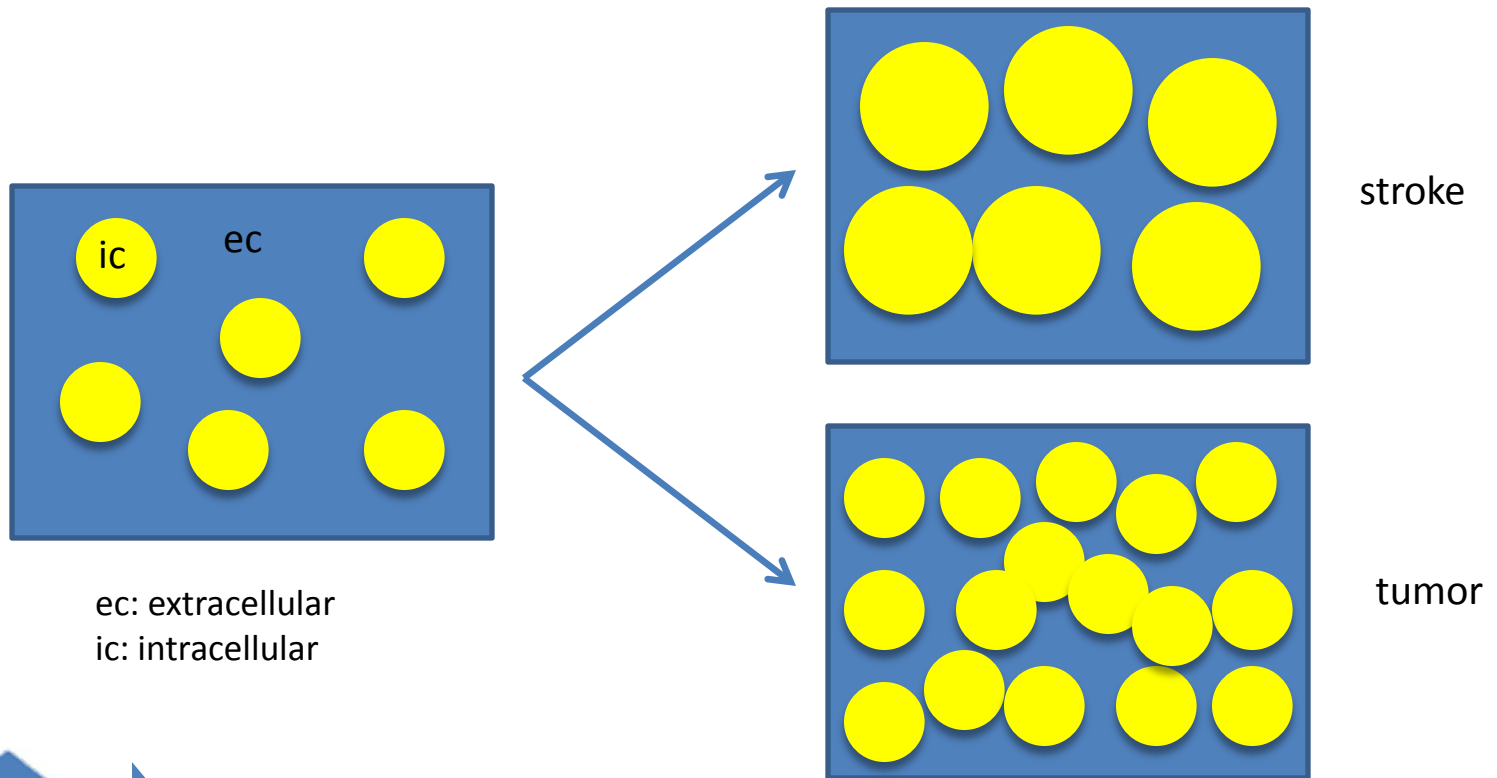
# Purpose

- Diffusion weighted imaging (DWI) has become increasingly popular in clinical neuroimaging for evaluation of stroke, tumors, infection and neurodegeneration.
- Apparent Diffusion Coefficient (ADC) maps are typically generated from  $b$  values based on a presumed, mono-exponential relationship.
- We aim to apply a bi-exponential model, where the DWI signal is presumed to be explained by intracellular and extracellular compartments.



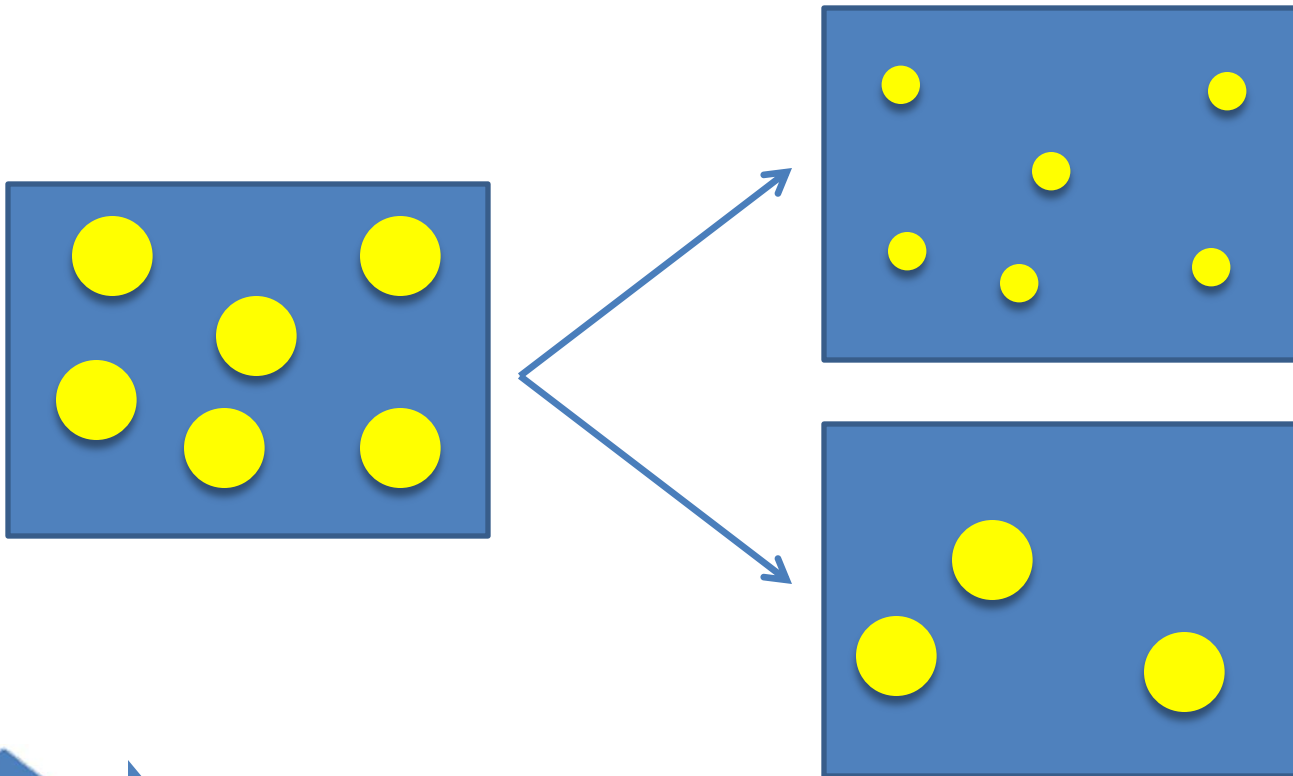
# Purpose

In acute stroke and malignancy, one would expect a higher intracellular to extracellular ratio secondary to cytotoxic edema and increased cellularity, respectively.



# Purpose

Conversely, in the case of CCD, we hypothesize that there will be a higher extracellular contribution to the DWI signal in the abnormal cerebellar hemisphere, secondary to neuronal atrophy and/or decreased number of neurons secondary to cell death.



# Purpose

- Our main hypothesis is that we find a higher extracellular contribution (or alternatively, lower intracellular contribution) to the DWI signal in the cerebellar hemisphere contralateral to cortical pathology, i.e., affected by CCD.
- Bi-exponential models have been previously proposed in experimental DWI studies with multiple  $b$  values to provide better fits for the DWI signal (e.g., Mulkern et al., 1999; Maier et al., 2001).
- Here, we aim to numerically solve for a biexponential model using three, typically clinically accessible  $b$  values (i.e., 0, 500, and 1000).



# Methods

- We study DWI images of six patients with cortical encephalomalacia, predominantly secondary to old infarction in the middle cerebral artery territory.
- Semi-automatic segmentation of the cerebellum is performed on Matlab (MathWorks, Natick, MA).



# Methods

We numerically solve a bi-exponential model at a voxel-by-voxel basis to obtain intracellular and extracellular contributions for each cerebellar hemisphere. Histograms of  $f$ , the intracellular component coefficient, are then obtained for each cerebellar hemisphere.

$$\frac{S_j}{S_0} = f * e^{-b_j D_i} + (1 - f) * e^{-b_j D_e}$$

Diagram illustrating the bi-exponential model equation with parameter labels and arrows pointing to the corresponding terms:

- signal (purple) points to  $S_j$
- intracellular fraction (blue) points to  $f$
- intracellular diffusion coefficient (blue) points to  $D_i$
- extracellular fraction (blue) points to  $(1 - f)$
- extracellular diffusion coefficient (blue) points to  $D_e$

Set of two equations with  $b_j$ : {500, 1000}



# Methods

- We additionally select regions of interest in normal-appearing basal ganglia (presumed to be rich in gray matter) and in normal-appearing centrum semiovale (presumed to be rich in white matter).
- Similarly to our analysis of the cerebellum, we solve a voxelwise, bi-exponential model to compare the intracellular and extracellular coefficients between each region of interest and acquire  $f$  histograms.
- As proof of principle, we expect that the basal ganglia region of interest demonstrates higher  $f$  (intracellular coefficient) than the centrum semiovale region.



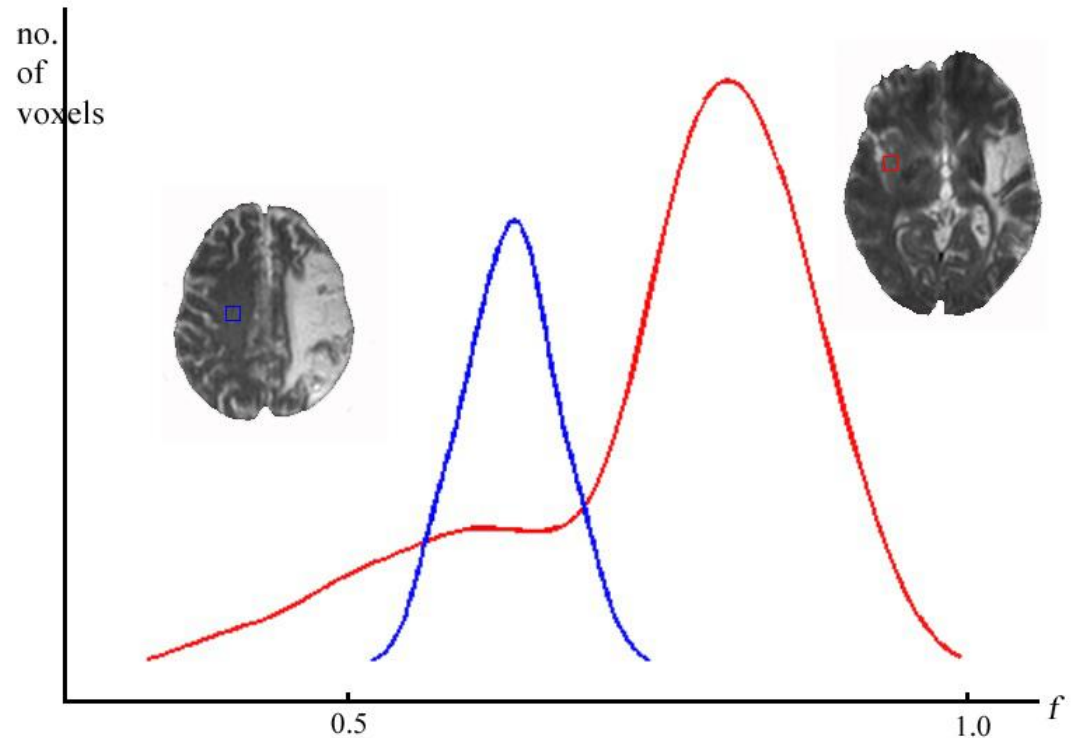
# Methods

- After obtaining histograms for intracellular coefficients,  $f$ , in each cerebellar hemisphere, we compare the distributions via a Mann-Whitney U test and obtain  $p$  values.
- Our null hypothesis is that two regions being compared result in the same distribution of intracellular coefficients.



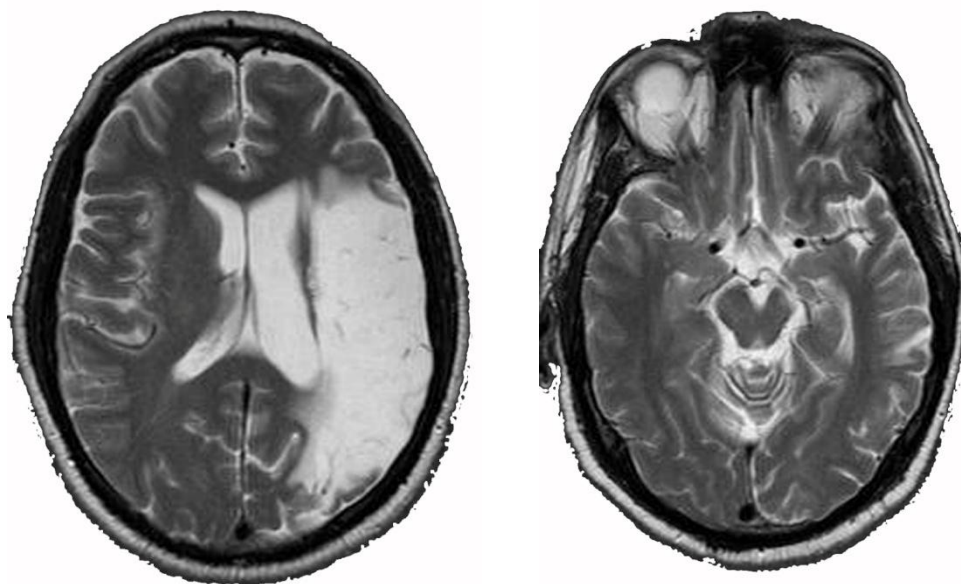
# Results

As expected, the basal ganglia region of interest (shown here in red) has a significantly higher  $f$ , i.e., contribution of the intracellular compartment, when compared to the centrum semiovale (shown here in blue;  $p \ll 0.001$ ).



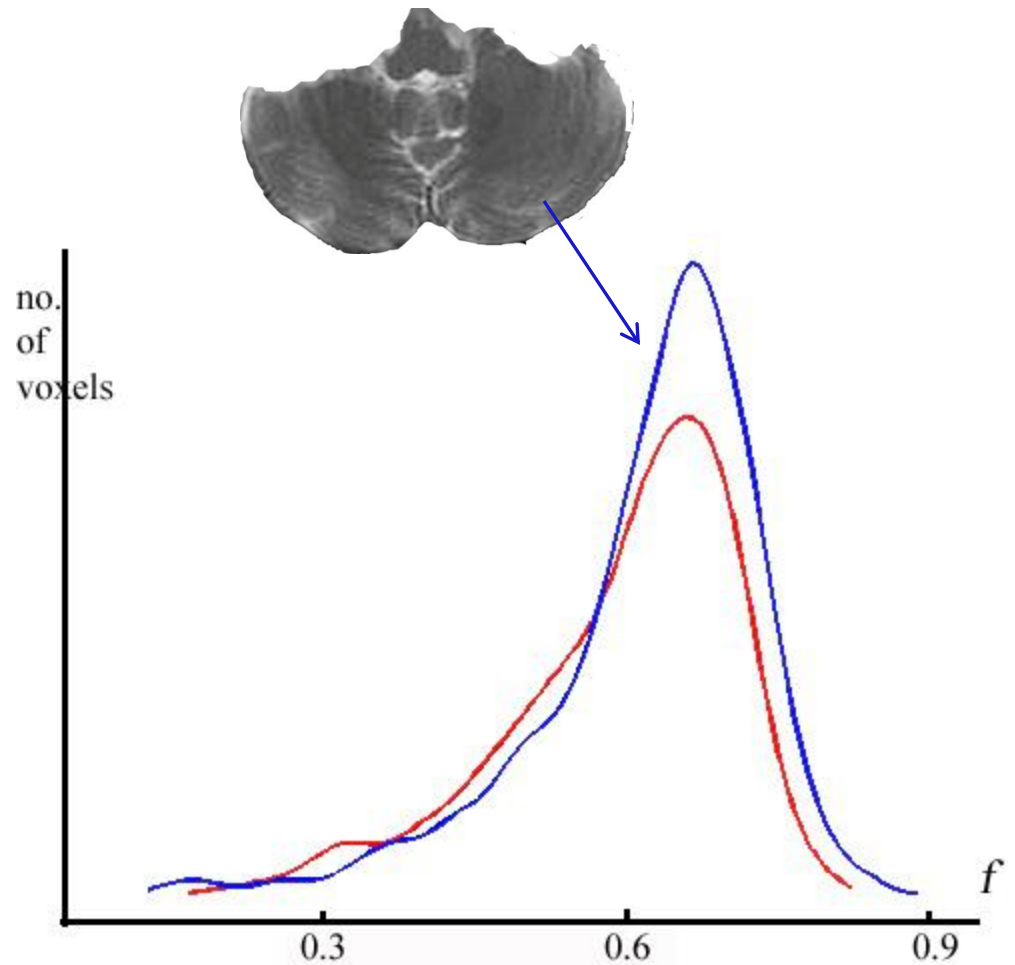
# Results

- Axial T2 weighted MRI images are shown for one of our six cases, demonstrating a large, old left MCA territory infarct and Wallerian degeneration of the ipsilateral cerebral peduncle.
- Histograms of the intracellular coefficients for each cerebellar hemisphere are shown in the next slide.



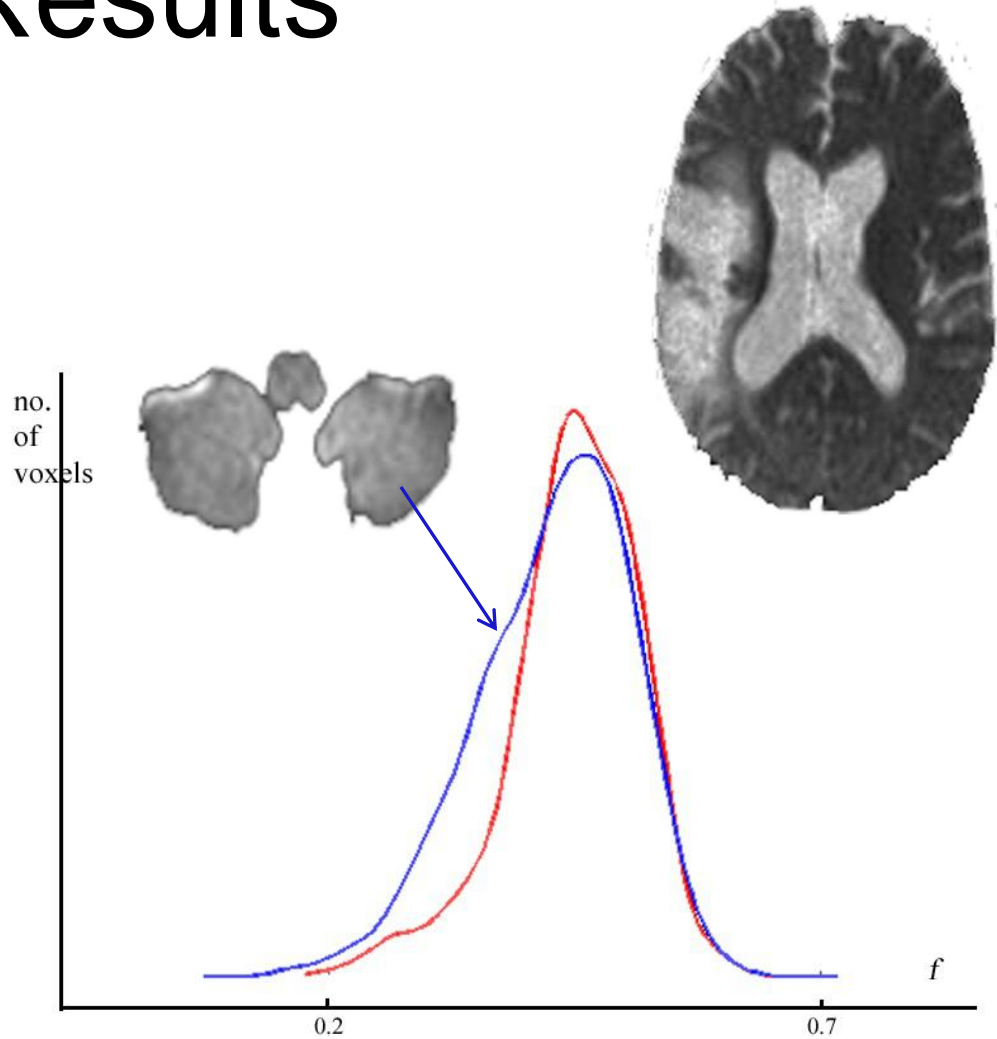
# Results

We find a significantly lower intracellular contribution to the DWI signal in the contralateral, right cerebellar hemisphere (red), compared to the left (blue;  $p < 0.01$ ).



# Results

- Another case is shown with right-sided cortical encephalomalacia.
- There is significantly lower intracellular contribution in the contralateral, left cerebellar hemisphere (blue), compared to the right (red;  $p < 0.01$ ).



# Results

- All six cases similarly showed significantly lower intracellular coefficients in the cerebellar hemisphere contralateral to the side of cortical pathology.
- This corroborates our hypothesis in that CCD leads to a lower intracellular to extracellular compartment ratio, presumably as a result of decreased neuronal density.



# Discussion

- We apply a bi-exponential model composed of intracellular and extracellular compartments to aid in detection of crossed cerebellar diaschisis on DWI.
- We numerically solve for the contribution of each compartment to the DWI signal. Our method only utilizes three, typically clinically available  $b$  values.
- Our approach may thus offer promise for detection of sub-threshold signal differences in a variety of clinical scenarios.



# Discussion

- CCD has traditionally been diagnosed on PET as asymmetric hypometabolism.
- Asymmetric atrophy on MRI is often subtle and difficult to detect.
- New studies have provided promising results with arterial spin-labeling MRI for detection of CCD (e.g., Kang et al., 2015; Strother et al., 2016).
- We provide a promising, quantitative approach to detection of DWI signal alterations in CCD with the advantage of applicability to clinical cases.



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