

Computational Environments for Coupling Multiphase Flow, Transport, and Geomechanics in Modeling Carbon Sequestration in Saline Aquifers

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## Acknowledge

#### Collaborators:

- Algorithms: UT-Austin (T. Arbogast, M. Delshad, E. Gildin, G. Pencheva, S. Thomas, T. Wildey, G. Xue, C. Yuan): Pitt (I. Yotov); ConocoPhillips (H. Klie), Paris VI (V. Girault, M. Vohralik); Clemson (S. Sun)
- Parallel Computation: IBM (K. Jordan); Rutgers (M. Parashar)
- Closed Loop Optimization: NI (I. Alvarado, D. Schmidt)
- Phase Behaviour and Compositional Modeling : UT-Austin (M. Delshad); Yale (A. Firoozabadi)
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## Outline

### Motivation

- Why Carbon Capture and Storage (CCS)?
- Carbon Sequestration Storage Options
- Mathematical and Computational Models Objectives and Present Capabilities

### Mathematical and Computational Challenges

- Discretizations (see Pencheva, Thomas & Xue lectures)
- Solvers (see Wildey lecture)
- Multiscale and Uncertainty Quantification
- A Posteriori Error Estimates and Adaptivity
- Closed Loop Optimization
- Summary

## **World Primary Energy Demand**



From: Joan MacNaughton (Alstom Power Company)

World energy demand expands by 45% between now and 2030 – an average rate of increase of 1.6% per year – with coal accounting for more than a third of the overall rise

## **World Oil Production by Source**



From: Joan MacNaughton (Alstom Power Company)

Even if oil demand was to remain flat to 2030, 45 mb/d of gross capacity – roughly four times the capacity of Saudi Arabia – would be needed just to offset decline from existing oilfields

## **CO2 from Fossil/Fuel Combustion**



generation

# CO<sub>2</sub> Storage Options

#### Methods for storing CO2 in deep underground geological formations



SRCCS Figure TS-7



IPCC

INTERGOVERNMENTAL PANEL ON CLIMATE CHANGE

## **Global Experience in CO<sub>2</sub> Injection**



#### From: Peter Cook, CO2CRC

## **Planned Commercial Projects**

- Snohvit- Norway (2008) Aquifer
- Gorgon- Australia (2008-2010) Aquifer
- Miller-Peterhead UK (2009) EOR
- Carson US (2009) Oil/gas reservoirs
- ✓ Draugen Norway (2010) EOR

Total CO2 stored ~ 12.5 MT  $CO_2$ / yr





## Effect of Geology on CO<sub>2</sub> Migration



Sequestration performance depends on the geology of the proposed sequestration site. (a) In an aquifer with no shale layers, the CO<sub>2</sub> plume rises quickly to the aquifer caprock, where it migrates laterally beneath this impermeable seal. (b) When shale units are present, they effectively retard the plume's vertical migration while promoting its lateral extension, thus enhancing the effects of solubility and mineral trapping.

**GCEP: Stanford** 

## Key Issues in CO<sub>2</sub> Storage

- What is the likelihood and magnitude of CO<sub>2</sub> leakage and what are the environmental impacts?
- > How effective are different  $CO_2$  trapping mechanisms?
- > What physical, geochemical, and geomechanical processes are important for the next few centuries and how these processes impact the storage efficacy and security?
- What are the necessary models and modeling capabilities to assess the fate of injected CO<sub>2</sub>?
- What are the computational needs and capabilities to address these issues?
- How these tools can be made useful and accessible to regulators and industry?



# CO<sub>2</sub> Sequestration Modeling Approach

#### Numerical simulation

- Characterization (fault, fractures)
- Appropriate gridding
- Compositional EOS
- Parallel computing capability

#### Key processes

- ✓ CO₂/brine mass transfer
- ✓ Multiphase flow
  - During injection (pressure driven)
  - After injection (gravity driven)
- Geochemical reactions
- Geomechanical modeling





## **Compositional Modeling**



Figure 15 Comparison of CO<sub>2</sub> solubility data for a range of salinities.



Figure 3 Measured solubility of CO<sub>2</sub> in distilled de-ionised water at 8 MPa.







- Accurate physic-based simulation of CO<sub>2</sub> storage
- Incorporate realistic phase behavior and physical property model enhancements
- Include geochemical, geomechanical, and geobiological couplings with flow to investigate their impact at different time scales
- Implementation of efficient and accurate parallel multiscale and multiphysics algorithms based on accurate adaptive error estimators
- Train students and postdocs on above collaborative projects

## **IPARS-COMP Flow Equations**

Mass Balance Equation

$$\frac{\partial \left(\phi N_{i}\right)}{\partial t} + \nabla . \left(\sum_{\alpha} \rho_{\alpha} \xi_{i}^{\alpha} u_{\alpha} - \phi \rho_{\alpha} S_{\alpha} D_{i}^{\alpha} \nabla \xi_{i}^{\alpha}\right) = q_{i}$$

#### **Pressure Equation**

$$\frac{\partial S_T}{\partial p}\delta p + \sum_i \frac{\partial S_T}{\partial N_i}\delta N_i + \sum_i \frac{\partial S_T}{\partial \ln K_i}\delta(\ln K_i) = 1 - S_T^k.$$

#### **Solution Method**

 Iteratively coupled until a volume balance convergence criterion is met or a maximum number of iterations exceeded.

### **Thermal & Chemistry Equations**

#### Energy Balance

- Solved using a time-split scheme (operator splitting)
- Higher-order Godunov for advection

 Fully implicit/explicit in time and Mixed FEM in space for thermal conduction

$$\frac{\partial (\mathbf{M}_{\mathrm{T}}\mathbf{T})}{\partial t} + \nabla \cdot \left(\sum_{\alpha} \rho_{\alpha} \mathbf{C}_{p\alpha} \mathbf{u}_{\alpha} \mathbf{T} - \lambda \nabla \mathbf{T}\right) = \mathbf{q}_{\mathrm{H}}$$

 $M_{\rm T} = (1 - \phi) \rho_{\rm s} C_{\rm vs} + \phi \sum_{\alpha} \rho_{\alpha} C_{\rm v\alpha} S_{\alpha}$ 

Internal energy :  $M_T$ 

#### <u>Chemistry</u>

 System of (non-linear) ODEs
 Solved using a higher order integration schemes such as Runge-Kutta methods

$$\frac{\mathrm{d}\mathbf{c}}{\mathrm{d}t} = \mathbf{r}\left(\mathbf{c}\right).$$

$$\mathbf{k}_{1,i} = \Delta \tau^{l} \mathbf{r}_{i} \left( \mathbf{c} \right)$$
$$\mathbf{k}_{2,i} = \Delta \tau^{l} \mathbf{r}_{i} \left( \mathbf{c} + \frac{1}{2} \mathbf{k}_{1} \right)$$
$$\hat{\mathbf{c}} = \mathbf{c} + \mathbf{k}_{2}.$$

### **EOS Model**

#### **Peng-Robinson EOS**



## Coupled Flow-Thermal-Chemistry Algorithm



# **CO2 EOR Simulations**

### Verification

SPE5 -- A quarter of 5 spot benchmark WAG problem 3-phase, 6 components C1, C3, C6, C10, C15, C20









## Verification

### CO<sub>2</sub> pattern flood injection 3-phase, 10 components CO<sub>2</sub>, N<sub>2</sub>, C<sub>1</sub>, C<sub>3</sub>, C<sub>4</sub>, C<sub>5</sub>, C<sub>6</sub>, C<sub>15</sub>, C<sub>20</sub>

### **IPARS-COMP vs CMG-GEM**



## **Parallel Simulations**





#### Texas Advanced Computing Center The University of Texas at Austin



## **Parallel Scalability**

#### Hardware

Lonestar: Linux cluster system	Blue GeneP: CNK system, Linux I/O
1,300 Nodes / 5,200 cores	262,144 Nodes / 1,048,576 cores
Processor Arch: 2.66GHz, Dual core, Intel Xeon 5100, Peak: 55 TFlops/s	Processor Arch: 850MHz, IBM CU-08, Peak: ~1 PFlop/s
8 GB/node	2 GB/node
Network: nfiniBand, 1GB/s	Network: 10Gb Eth,1.7GB/s

### Software

GMRES, BCGS, LSOR, Multigrid.

MPI: MVAPICH2 library for parallel communication

## Scalability On Ranger (TACC) & Blue Gene P

GMRES solver with Multigrid Preconditioner 3500ft, 3500 ft, 100ft reservoir 40x160x160=1,024,000 elements CPUs: 32, 64, 128, 256, 512, 1024



# Speedup on Blue Gene (Watson-Shaheen)





# Frio Brine Pilot Site

- Injection interval: 24-m-thick, mineralogically complex fluvial sandstone, porosity 24%, Permeability 2.5 D
- Unusually homogeneous
- Steeply dipping 16 degrees
- 7m perforated zone
- Seals numerous thick shales, small fault block
- Depth 1,500 m
- Brine-rock, no hydrocarbons
- 150 bar, 53 C, supercritical CO<sub>2</sub>



## **Frio Modeling using IPARS**

Stair stepped approximation on a 50x100x100 grid (~70,000 active elements) has been generated from the given data.



## **Modeling Temperature for Frio Test**



# REALISTIC CO2 STUDIES WAG HYSTERESIS

## CO<sub>2</sub> Injection Scenarios

Continuous CO<sub>2</sub> injection
 CO<sub>2</sub>-Water injection (2:1 Cycle)
 CO<sub>2</sub> injection/Shut in (2:1 cycle)
 One injector at the bottom layer

# Inject CO<sub>2</sub> in the bottom 30 ft layer





## CO<sub>2</sub> Plume at the end of Injection



# CO<sub>2</sub> plume at the end of Injection (Vertical Profile)



## **Frio Pilot Test**



#### Permeability (md)





#### Ghomian et al., 2006

### Effect of Gas Relative Permeability – Hysteresis

#### End of 12 day injection



### **Simulation of Frio Pilot Test**

#### Ghomian et al., 2006



✓ 1500 m deep, 6 m thick
✓ 30 m inj – monitoring wells
✓ T = 57 C
✓ 5- 25 dip angle
✓ K = f (\$)
✓ S<sub>wir</sub> and s<sub>gr</sub> = f (k, \$)

At 10 yrs: 55% as residual CO<sub>2</sub> 45% dissolved in brine

83 x 62 x 26 (212,366 cells) 10' x 10' x 2.5' local mesh refinement No temperature modeling No geomechanics No geochemistry

1 – 3 hrs cpu per run

## On Prediction of Realistic CO<sub>2</sub> Tests

- Fluid properties as a function of pressure, temperature, composition
  - ✓ Viscosity, density, interfacial tension, phase behavior
- Rock dependent relative permeability and capillary pressure as a function of
  - ✓ Saturation, composition, saturation history (hysteresis), IFT
- Rock reaction to pressure changes and subsequent impact on pore volumes and permeability (geomechanics)
- Reactions of rock minerals and injected CO2 (geochemistry)
- Model estimators that include upscaling and downscaling for property manipulations for coarse/fine grid
- > Upscale strategy for  $CO_2$  storage (if needed)
- Increase grid resolution to improve the quality of model results
  - ✓ Increase CPU and memory requirements
  - ✓ Faster numerical methods dynamic grid refinement based on a posteriori error estimators that include upscaling and down scaling, efficient solvers
  - ✓ Efficient parallelization methods
  - Optimization and Uncertainty analysis

### **Computational Components**

- High Fidelity Algorithms for Treating Relevant Physics --Complex Nonlinear Systems (coupled near hyperbolic & parabolic/ elliptic systems with possible discrete models)
  - Locally Conservative Discretizations (mixed fem, control volume and/or discontinuous Galerkin)
- Multiscale (spatial & temporal multiple scales)
- Multiphysics (Darcy flow, biogeochemistry, thermal, geomechanics)
- Robust Efficient Physics-based Solvers (ESSENTIAL)
- A Posteriori Error Estimators
- Decision Theory: Closed Loop Optimization
- Parameter Estimation (history matching) and Uncertainty Quantification (Impt. monitoring leakage)
- Computationally intense:
- Distributed Computing
- Dynamic Steering

## **Motivation**

- Both DG and MFE are locally mass-conservative
- Real world heterogeneities such as thin faults, fractures and pinchouts, internal boundaries, geological layers can be computationally expensive



- Multiphysics applications necessitate coupling of DG and Mixed FEM
- Local mesh refinement

Eolian sandstone of the Weber Formation, Whiskey Gap, Wyoming

(photo taken from Wayne Narr, David W. Schechter, and Laird B. Thompson. Naturally Fractured Reservoir Characterization. Society of Petroleum Engineers, 2006.)





# Why Multiscale?

 Subsurface properties vary on the scale of millimeters Computational grids can be refined 3.5 to the scale of meters or kilometers Multiscale methods are designed to 2.5 allow fine scale features to impact a coarse scale solution Variational multiscale finite elements Hughes et al 1998 Upscale Hou, Wu 1997 Efendiev, Hou, Ginting et al 2004 3.8 Mixed multiscale finite elements 3.6 3.4 Arbogast 2002 3.2 Aarnes 2004 3 Mortar multiscale finite elements 2.8 Arbogast, Pencheva, Wheeler, 2.6 Yotov 2004 Yotov, Ganis 2008

## Basic Idea of the Multiscale Mixed Mortar Method

- 1. Localization. Divide  $\Omega$  into many small subdomains (or coarse elements of scale H), over which the original PDE is imposed.
- 2. Fine-scale effects. The subdomains are given Dirichlet boundary conditions  $p = \lambda$  on  $\Gamma$  and solved on the fine scale h to define the local solution.
- 3. Global coarse-grid problem. The weakly defined flux mismatch (jump in  $\mathbf{u} \cdot \nu$ ) on  $\Gamma$  is used to define a better  $\lambda$  on scale H > h, and we iterate the previous step until convergence is attained.
- 4. Fine-grid (re)construction. We obtain a fully resolved and fully coupled approximate solution if  $\lambda$  is approximated in a higher order space.

By using a higher order mortar approximation, we compensate for the coarseness of the grid and maintain good (fine scale) overall accuracy.



## Multiscale Mortar Mixed Finite Element Method

Key idea. On the interface

- Use only a few degrees of freedom (manage the linear algebra).
- Use higher order approximation (maintain accuracy).



#### Finite element spaces.

- Subdomain.  $V_{h,i} \times W_{h,i}$  is usual mixed space with polynomials of degree k-1 on mesh of spacing h > 0 on  $\Omega_i$ .
- Mortar.  $M_{H,ij}$  is continuous or discontinuous polynomials of degree m-1 on mesh of spacing H > h on  $\Gamma_{ij}$ .

*Mortar method.* Find  $\mathbf{u}_h \in \mathbf{V}_h$ ,  $p_h \in W_h$ ,  $\lambda_H \in M_H$  such that

$$\begin{array}{ll} (K^{-1}\mathbf{u}_{h},\mathbf{v})_{\Omega_{i}} = (p_{h},\nabla\cdot\mathbf{v})_{\Omega_{i}} - \langle\lambda_{H},\mathbf{v}\cdot\nu_{i}\rangle_{\Gamma_{i}} & \forall \mathbf{v}\in\mathbf{V}_{h,i} \\ (\nabla\cdot\mathbf{u}_{h},w)_{\Omega_{i}} = (f,w)_{\Omega_{i}} & \forall w\in W_{h,i} \\ \sum_{i}\langle\mathbf{u}_{h}\cdot\nu_{i},\mu\rangle_{\Gamma_{i}} = 0 & \forall \mu\in M_{H} \end{array}$$

*Remark.* The last equation enforces weak continuity of flux on  $\Gamma$ .

## **Construction of a Multiscale Basis**



### **Domain Decomposition and Multiscale**



# **Example: Uncertainty Quantification**

- > 360x360 grid
- > 25 subdomains of equal size
- 129,600 degrees of freedom
- Continuous quadratic mortars
- Karhunen-Loéve expansion of the permeability truncated at 9 terms
- Second order stochastic collocation
  - 512 realizations
- Training operator based on mean permeability



#### Mean Permeability Number of Interface Iterations



Inverfacer Sostuce Time

## **Example: IMPES for Two Phase Flow**

- 360x360 grid
- 25 subdomains of equal size
- 129,600 degrees of freedom
- Continuous quadratic mortars
- 50 implicit pressure solves
- 100 explicit saturation time steps per pressure solve
- Training operator based on initial saturation



#### Number of Interface Iterations



## **Multipoint Flux Mixed Finite Element**



## MFMFE on Quadrilaterals and Hexahedra



## **Convergence of MFMFE**

Find 
$$u_h \in V_h$$
 and  $p_h \in W_h$   

$$(K^{-1}u_h, v)_Q = (p_h, \nabla \cdot v), \quad v \in V_h$$

$$(\nabla \cdot u_h, w) = (f, w), \quad q \in W_h$$
Numerical Quadrature:  $(K^{-1}v, q)_{Q,E} = (\kappa^{-1}\hat{q}, \hat{v})_{Q,\hat{E}} = \frac{|\hat{E}|}{4} \sum_{i=1}^{4} \kappa^{-1}(\hat{r}_i)\hat{q}(\hat{r}_i) \cdot \hat{v}(\hat{r}_i)$ 

$$\kappa = JDF^{-1}\hat{K}(DF^{-1})^T$$

This quadrature rule reduces saddle point problem into cell-centered pressure equation.

Theorem: (Wheeler and Yotov 2005, Ingram and Wheeler and Yotov 2009) On simplicial and  $h^2$ -parallelogram grids,  $h^2$ -parallel pipebeds

$$\left\| u - u_h \right\|_V + \left\| p - p_h \right\|_W \le Ch$$
$$\left\| Q_h p - p_h \right\|_W \le Ch^2$$

## **PHYSICS BASED SOLVERS**



## **A Posteriori Error Estimates**

- Bound computations without knowing the solution:
- Choose norm equivalent to residual
  - Standard for linear problems on conforming spaces (Ainsworth, Babuska, Estep, Johnson, Oden, Rannacher, Verfurth, ...)
  - Extensions to non-conforming and computable bounds (W & Yotov; Arbogast, Pencheva, W & Yotov; Ainsworth; Vohralik; Vohralik & Ern; Pencheva, W, Wildey & Vohralik;
- Estimators need to be
  - Computable
  - Locally efficient for adaptivity
  - Robust (correct and apply to realistic problems, e.g. nonlinear and possibly singular)
  - Incorporate upscaling and downscaling of models ; solver tolerance related to mesh

# Ex. – A Highly Oscillating Permeability (Arbogast, Pencheva, W, & Yotov)

Permeability is highly oscillating

$$K = \begin{cases} 105 - 100 \sin(20\pi x) \sin(20\pi y), \\ 105 - 100 \sin(2\pi x) \sin(2\pi y), \end{cases}$$

We test AMR with K = I.

- $6 \times 6$  subdomains.
- Initial subdomain grid  $2 \times 2$ .
- Single mortar element on each interface.

 $x, y \in [0, 1/2]$  or  $x, y \in [1/2, 1]$ , otherwise.

# Ex. – A Highly Oscillating Permeability

#### Magnitude of the velocity after four refinements



Continuous quadratic mortars



Continuous linear mortars.

#### Conclusions.

- The highly oscillating velocity is well resolved.
- Refinement along x = 1/2 is due to the large jump-flux term  $\omega_{\tau}$ .
- Linear mortars produce finer grids, especially in the two regions of high oscillation.

# Continuous Measurement and Data Analysis for Reservoir Model Estimation



# Continuous Measurement and Data Analysis for Reservoir Model Estimation



## **Parameter Estimation Using SPSA**







Center for Frontiers of Subsurface Energy Security The University of Texas

**Summary statement**: Our goal is scientific understanding of subsurface physical, chemical and biological processes from the very small scale to the very large scale so that we can predict the behavior of CO2 and other byproducts of energy production that may need to be stored in the subsurface.



#### **RESEARCH PLAN AND DIRECTIONS**

- Challenges and approaches: Integrate and expand our knowledge of subsurface phenomena across scientific disciplines using both experimental and modeling approaches to better understand and quantify behavior far from equilibrium.
- Unique aspects The uncertainty and complexity of fluids in geologic media from the molecular scale to the basin scale.
- Outcome Predict long term behavior of subsurface storage.





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### Conclusions

- Computational Science and Mathematics Essential in Addressing Problems Impacting Energy and the Environment
  - Computation Required for Understanding and Developing Strategies for Energy Production, Carbon Capture and Storage, Storage of Nuclear Wastes and Renewables
  - Challenges Include MPP Modeling of Multiphysics, Multiscale Problems Accurately and Efficiently, and Incorporating Model Reduction, V&V and QU