

# Parkinsonian oscillations: a computational view

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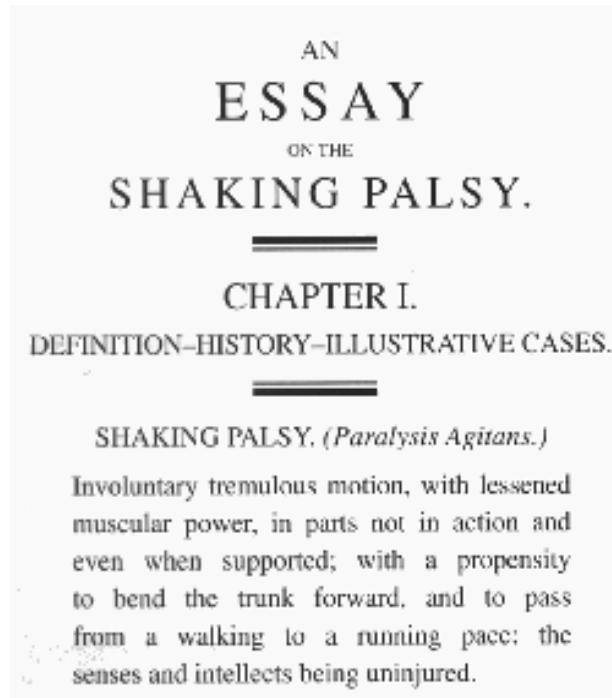
**SIAM Life Sciences**  
July 14, 2016



# Parkinson's disease: historical origin in medicine



James Parkinson



Parkinson, 1817

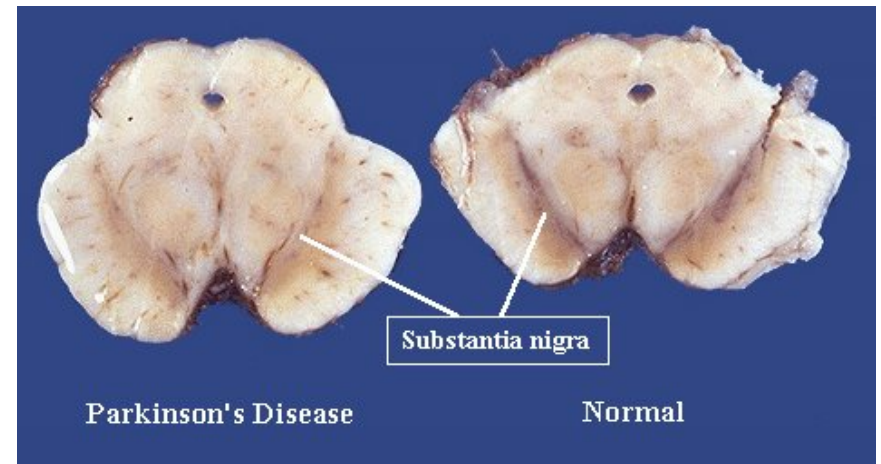
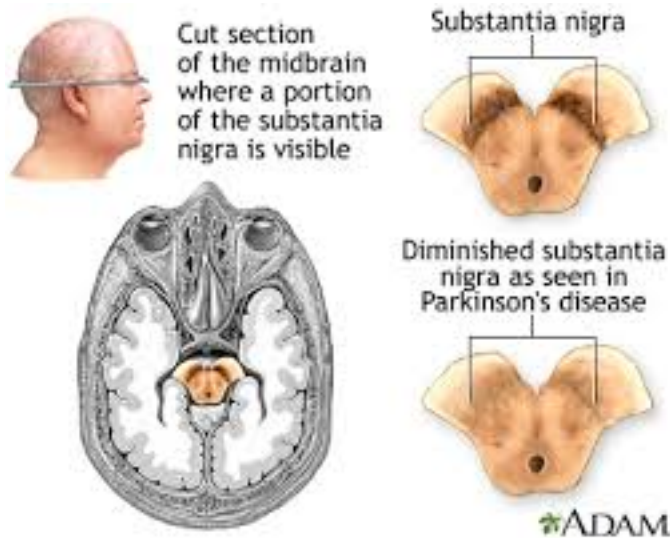


William Gowers, 1886

# Parkinson's disease: immediate cause

death of dopaminergic neurons in substantia nigra pars compacta:

Hassler et al., pre-1940; Carlsson & Hornykiewicz, 1950-1970



NIH Medline

CNS Pathology

**OP: Why do these cells die? Why don't other cells die?**





# Parkinson's disease: summary

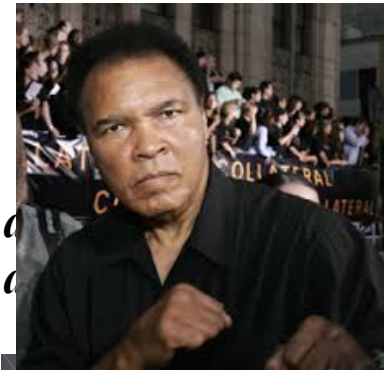
**what:** akinesia (difficulty initiating movement), bradykinesia (slowed movement), posture issues, rigidity, tremor

**how:** dopamine loss: death of dopamine-secreting cells in the substantia nigra pars compacta (SNc) of the *basal ganglia*

**who:** “8-18 cases per 100,000 person-years”; 1% of those over 60 and 4% of those over 80; 5-10% of cases are early onset (age 20-50)

**why:** occasionally but not usually genetic; risks linked to pesticides (e.g., rotenone!), toxins (MPTP -- *The Case of the Frozen Addicts*), heavy metals; possibly protection from caffeine, smoking, anti-inflammatories, estrogens, exercise, (clean) apple skin...

Wikipedia; de Lau et al., *Lancet Neurol.*, 2006; O. Bandmann



# altered basal ganglia neuronal activity patterns in parkinsonism

- *changes in firing rates*
- *increased burstiness*
- *increased oscillations*

Normal

Parkinsonism

GPe

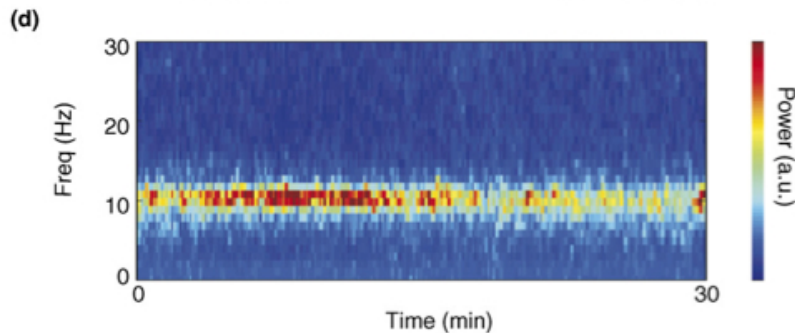
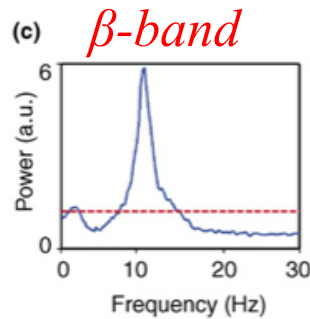
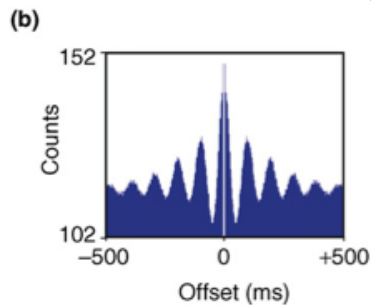
STN

GPi



Galvan & Wichmann, *Clin. Neuro.*, 2008

1 s



Magnin et al., *Neuroscience*, 2000



Hammond et al., *TINS*, 2007; GPi

# some past comput. models w/parkinsonian activity

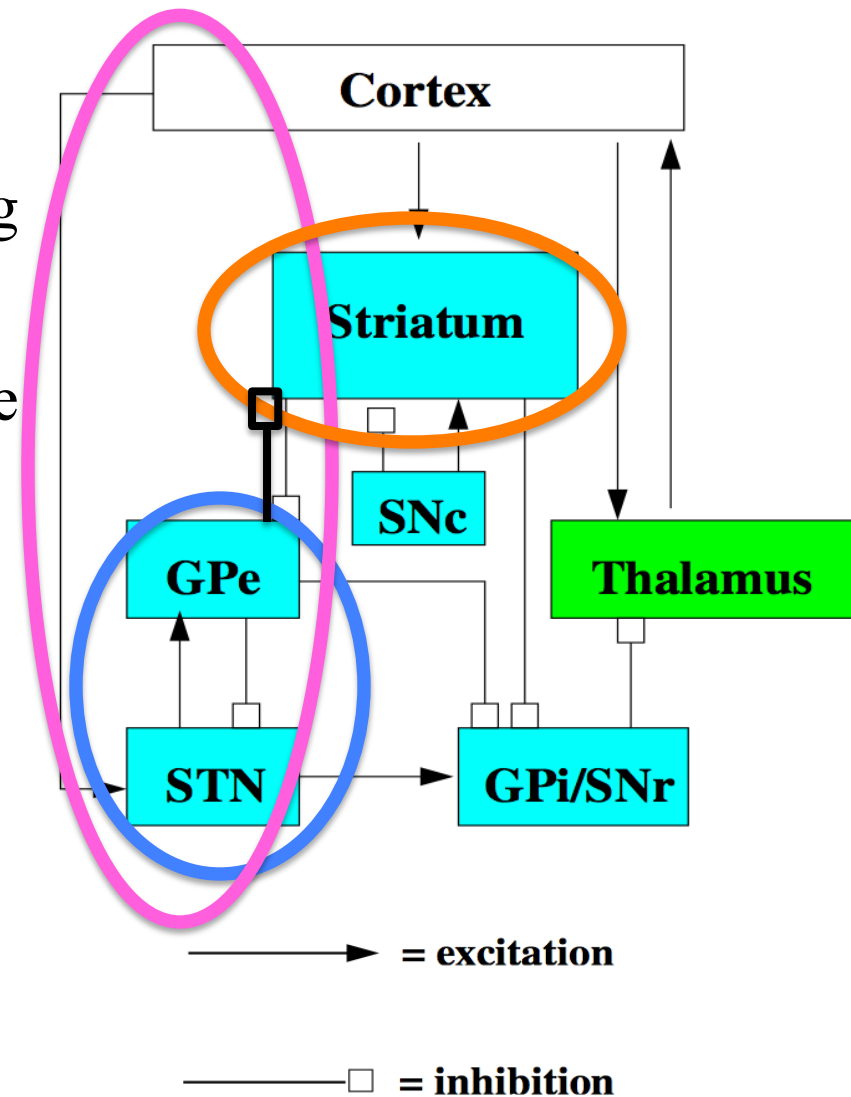
[Terman et al., 2002](#): STN-GPe (E-I loop); cf. Park & Rubchinsky

[Leblois et al., 2006](#): symmetry-breaking in full BG activity-based model

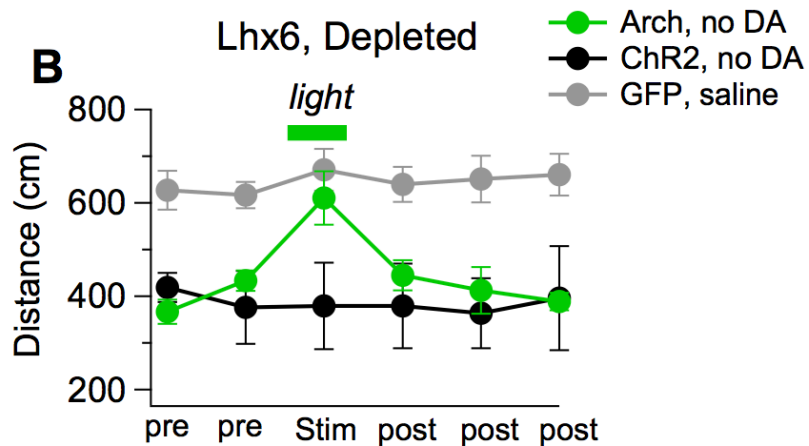
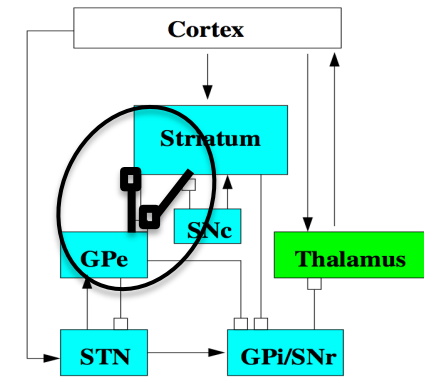
[Nevado-Holgado et al., 2010](#): STN-GPe firing rate model;  $\beta$  oscillations require cortical excitation to STN and synaptic delays

[McCarthy et al., 2011](#): inhibitory interactions in striatal medium spiny neurons (MSNs) sufficient for  $\beta$

[Kumar et al., 2011](#): large scale (LIF) STN-GPe model

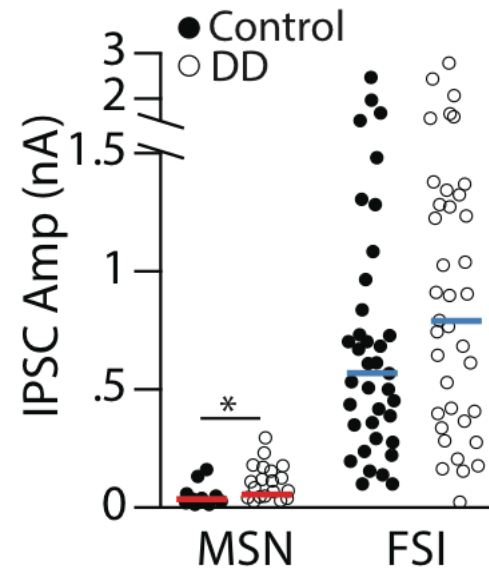
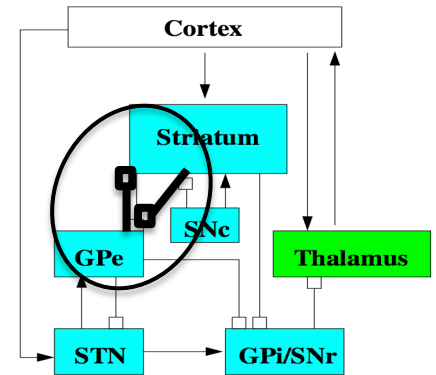
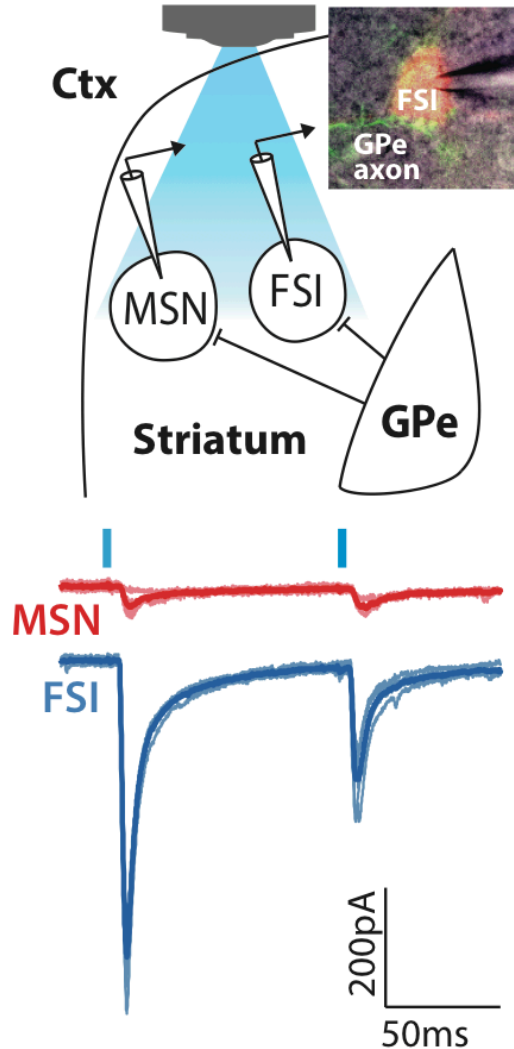


# new suspect: pallidostriatal circuit



Gittis lab, CMU; unpublished

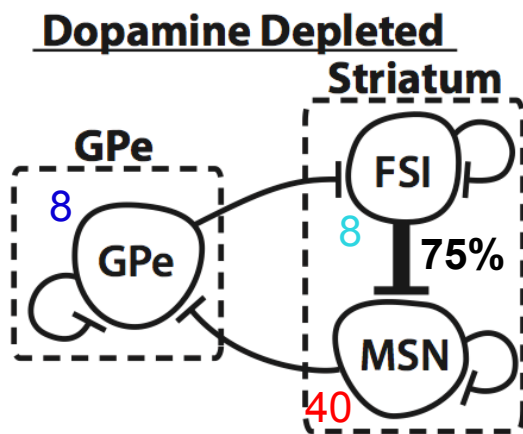
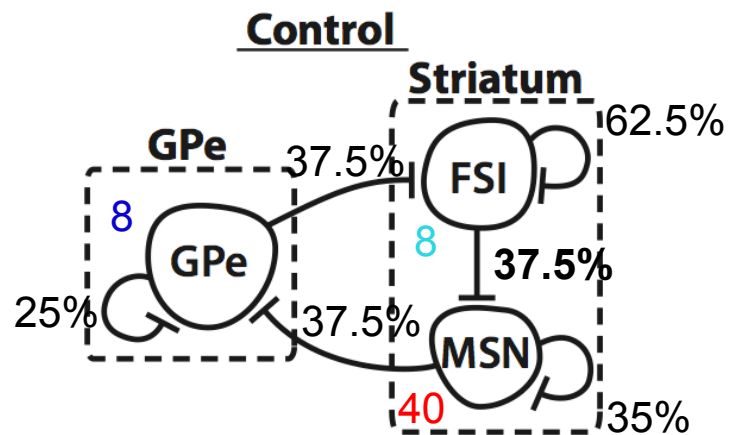
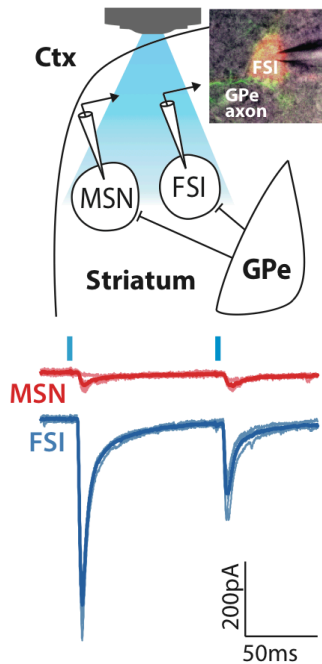
# defining the pallidostriatal circuit



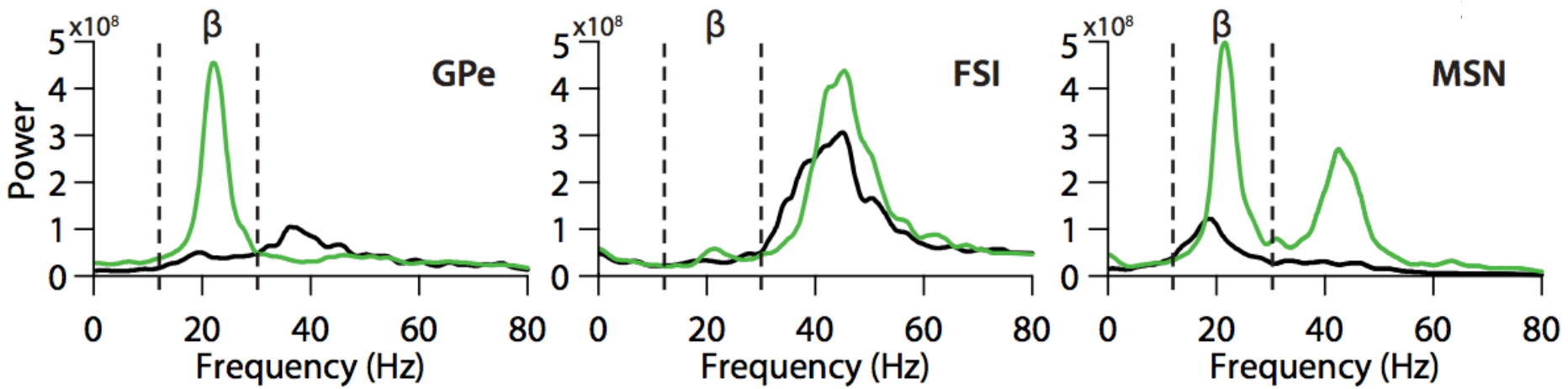
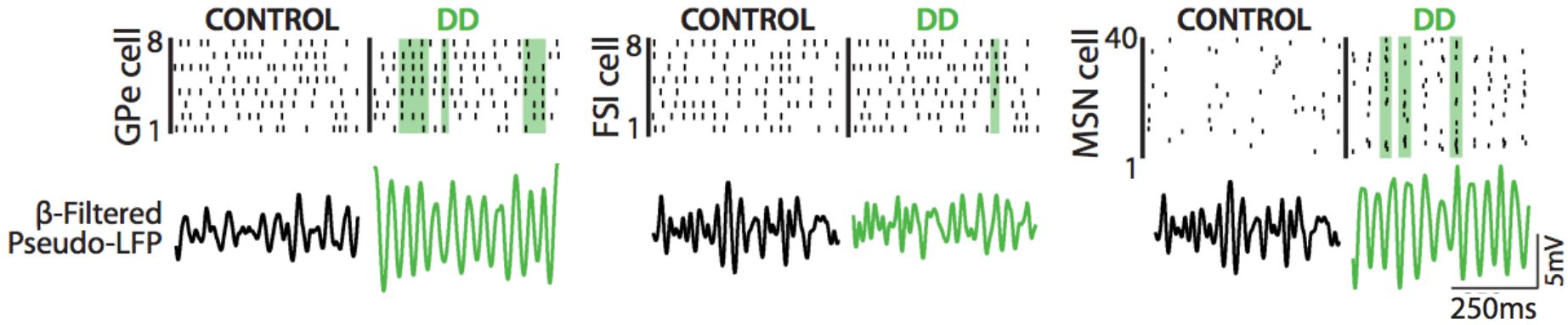
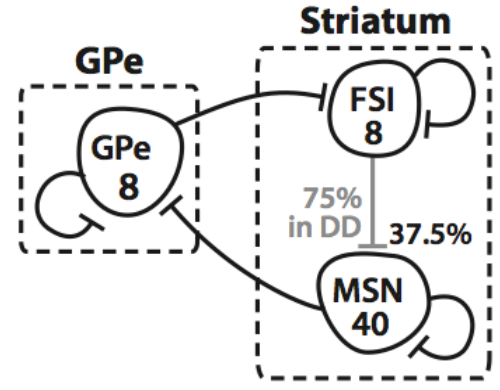
Corbit\*, Whalen\* et al., *J. Neurosci.*, 2016



# pallidostriatal circuit model

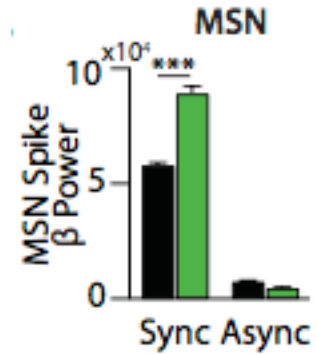
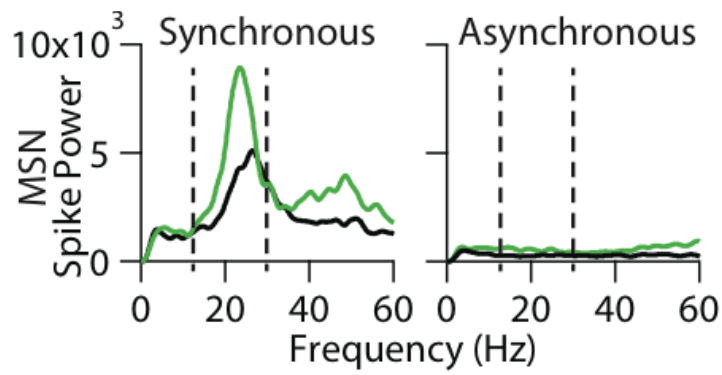
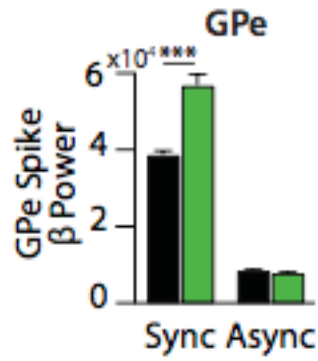
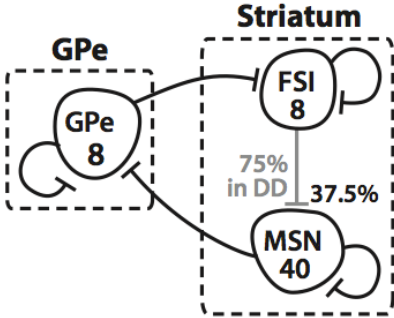
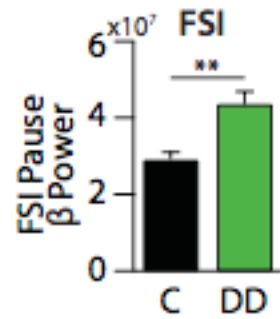
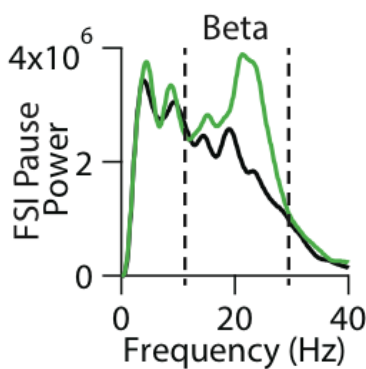
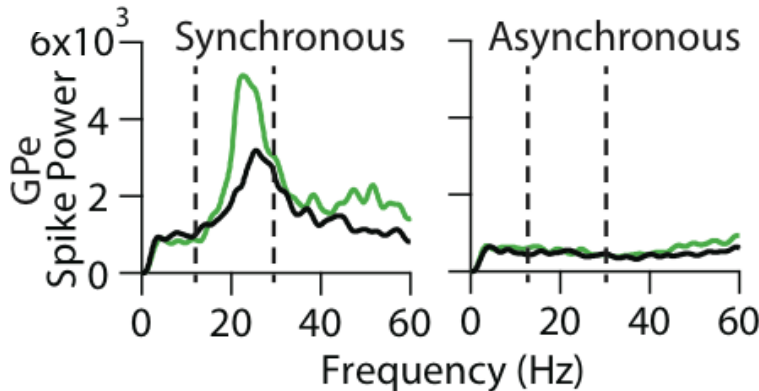


# how does $\beta$ emerge in GPe/MSN result of $\beta$ in FSI? you in $\beta$ ? (dopamine-depleted)



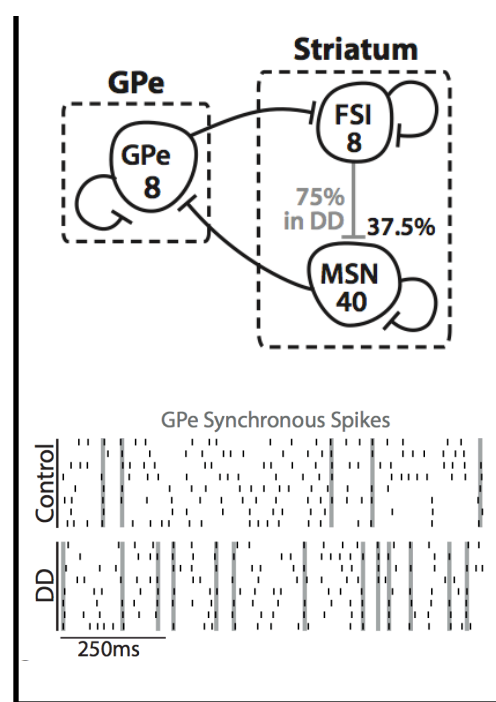
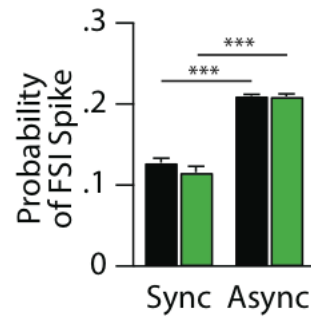
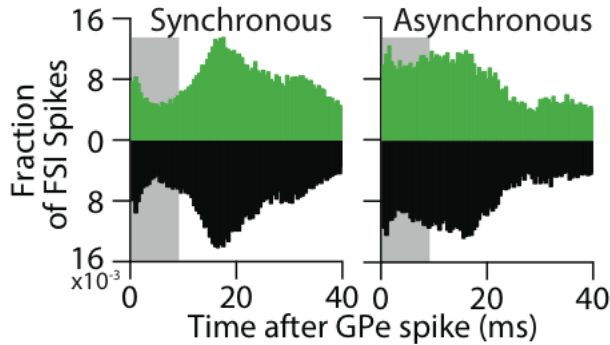


**key point: *synchronous events* exhibit  $\beta$  rhythmicity, enhanced in dopamine-depleted**

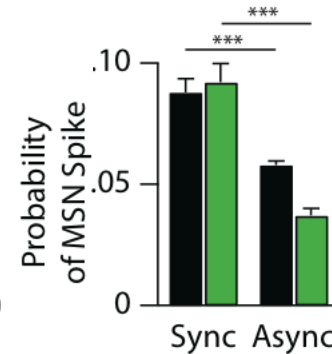
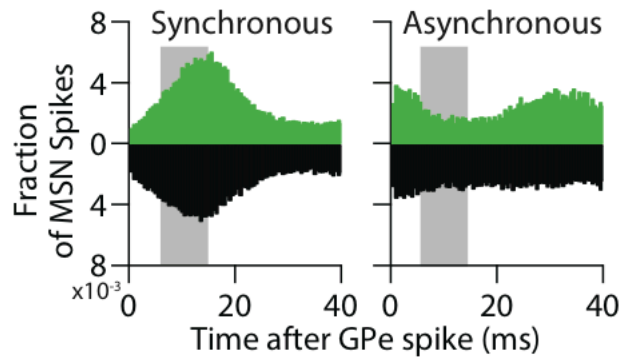


# thrown for a loop

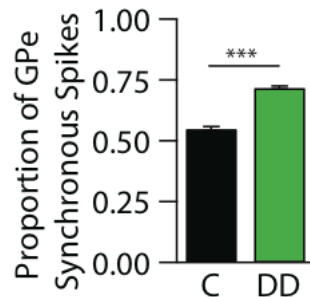
*synchronous spikes in GPe pause FSI...*



*...allowing MSN to fire, esp. in DD...*

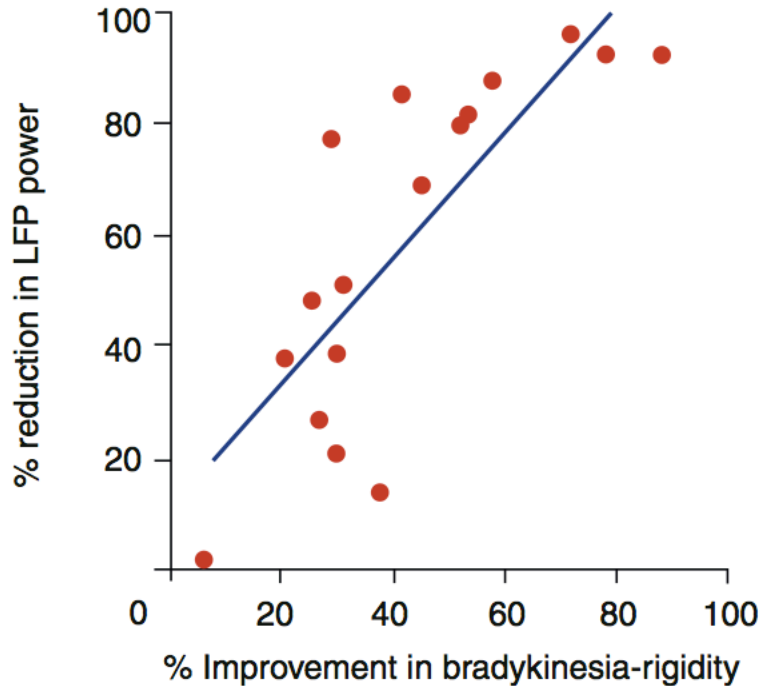


*...enhancing GPe synchrony in DD*

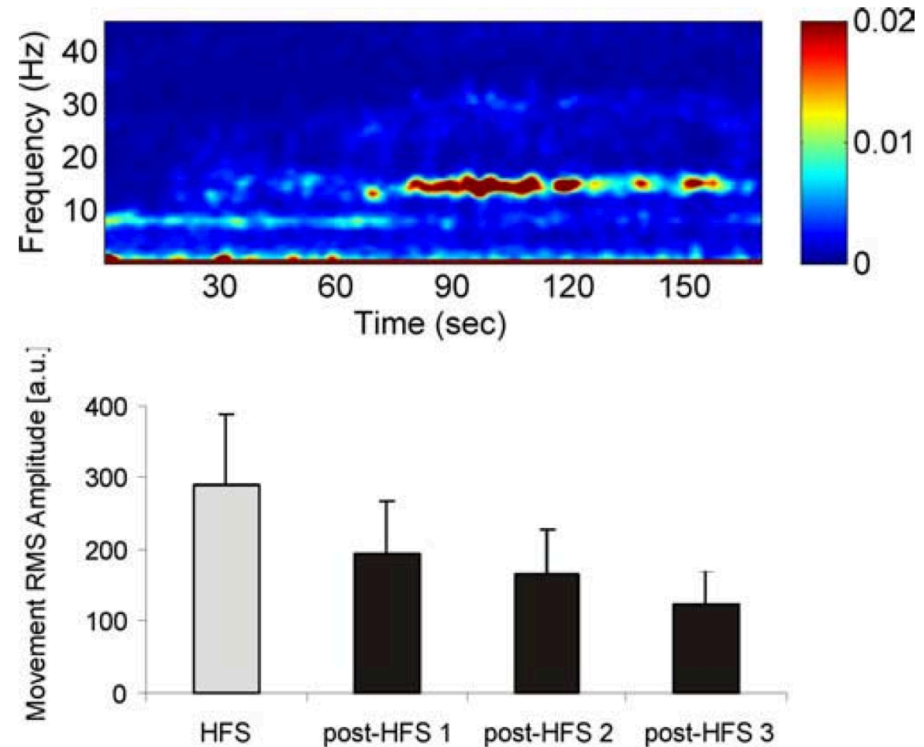


# why are $\beta$ oscillations significant?

$\beta$  strength correlates with PD severity; re-emergence/  
introduction of  $\beta$  can cause PD-like signs



Jenkinson & Brown, TINS, 2011  
(cf. Kuhn et al., *EJN*, 2006; *Exp. Neurol.*, 2009)

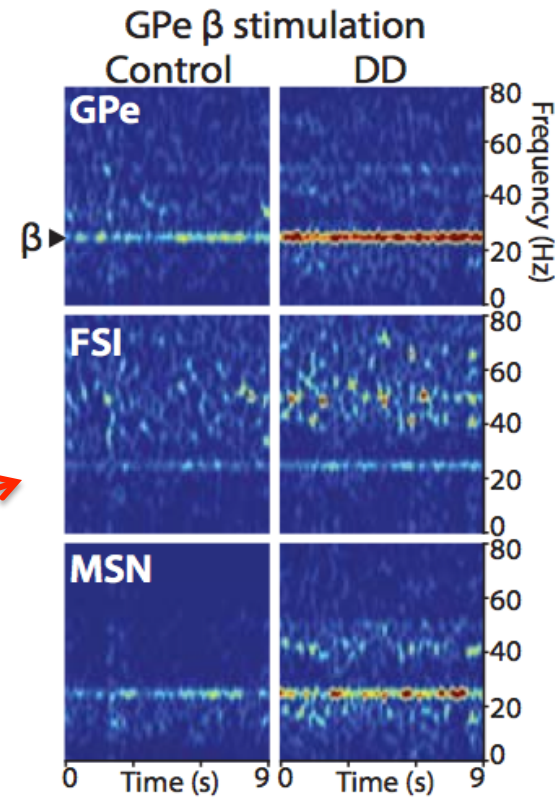


Kuhn et al., *J. Neurosci.*, 2008

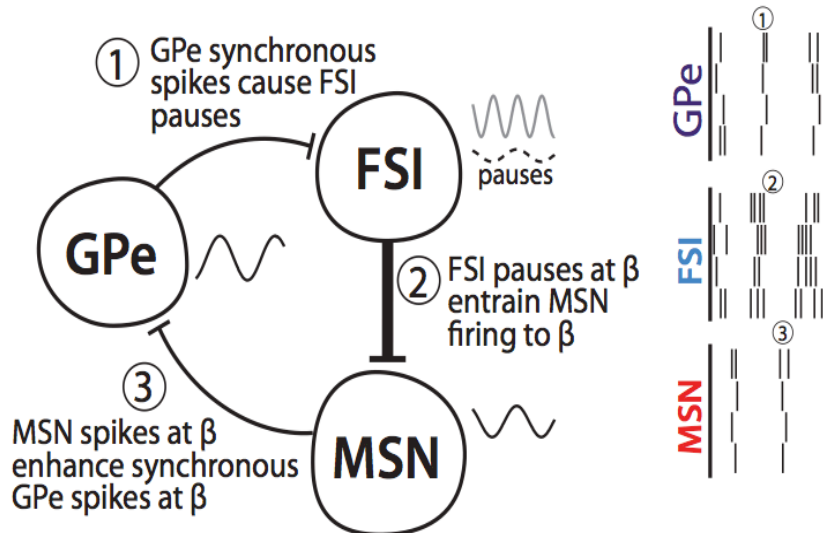


# Conclusions I

- Parkinson's disease involves pathological activity in the basal ganglia that includes *enhanced  $\beta$  oscillations*
- these oscillations may originate in *or be amplified by* the pallidostriatal circuit
- all circuit elements contribute:

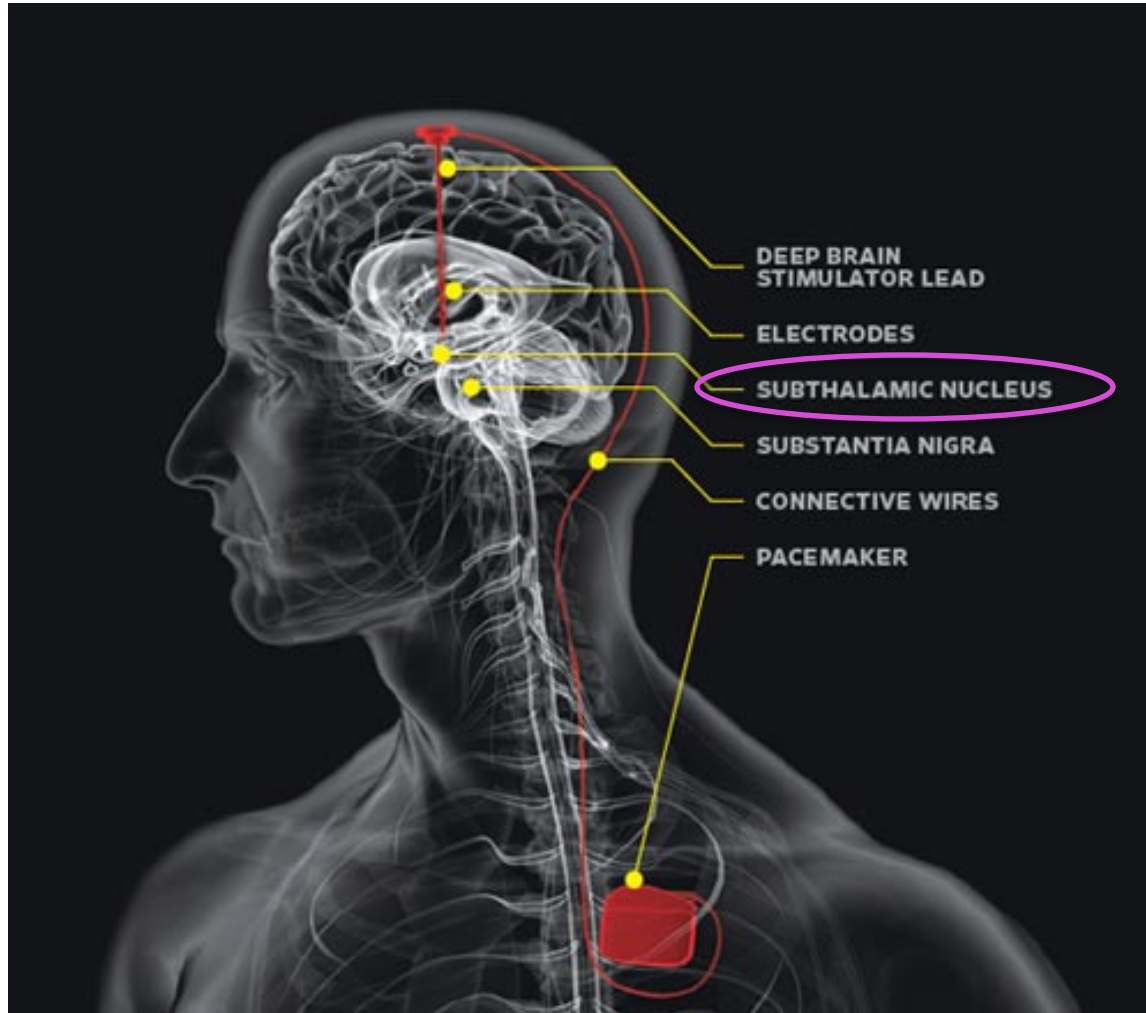


## Dopamine Depleted



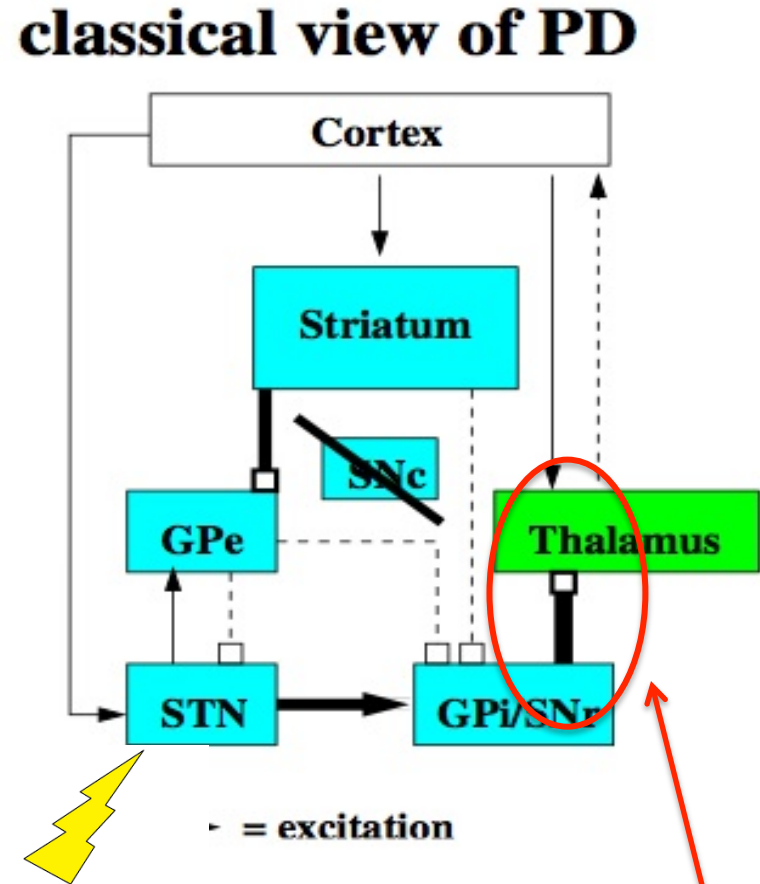
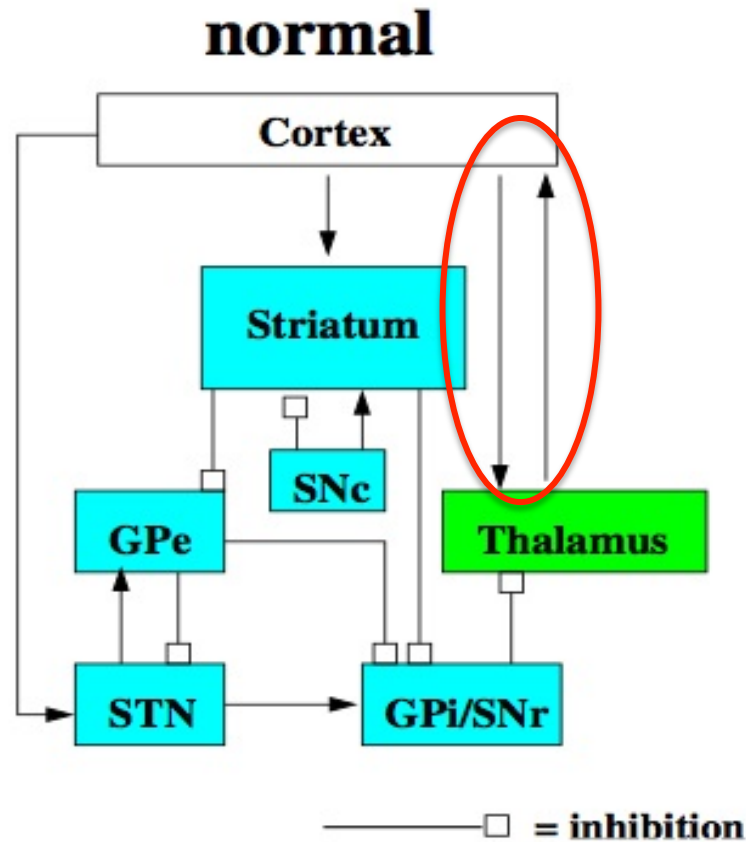
# how can motor symptoms be mitigated? *deep brain stimulation* (STN-DBS shown here)

The Mayo Clinic



**OP**: looks great – but how does this work??

# idea 1: BG outputs go to thalamic relay station

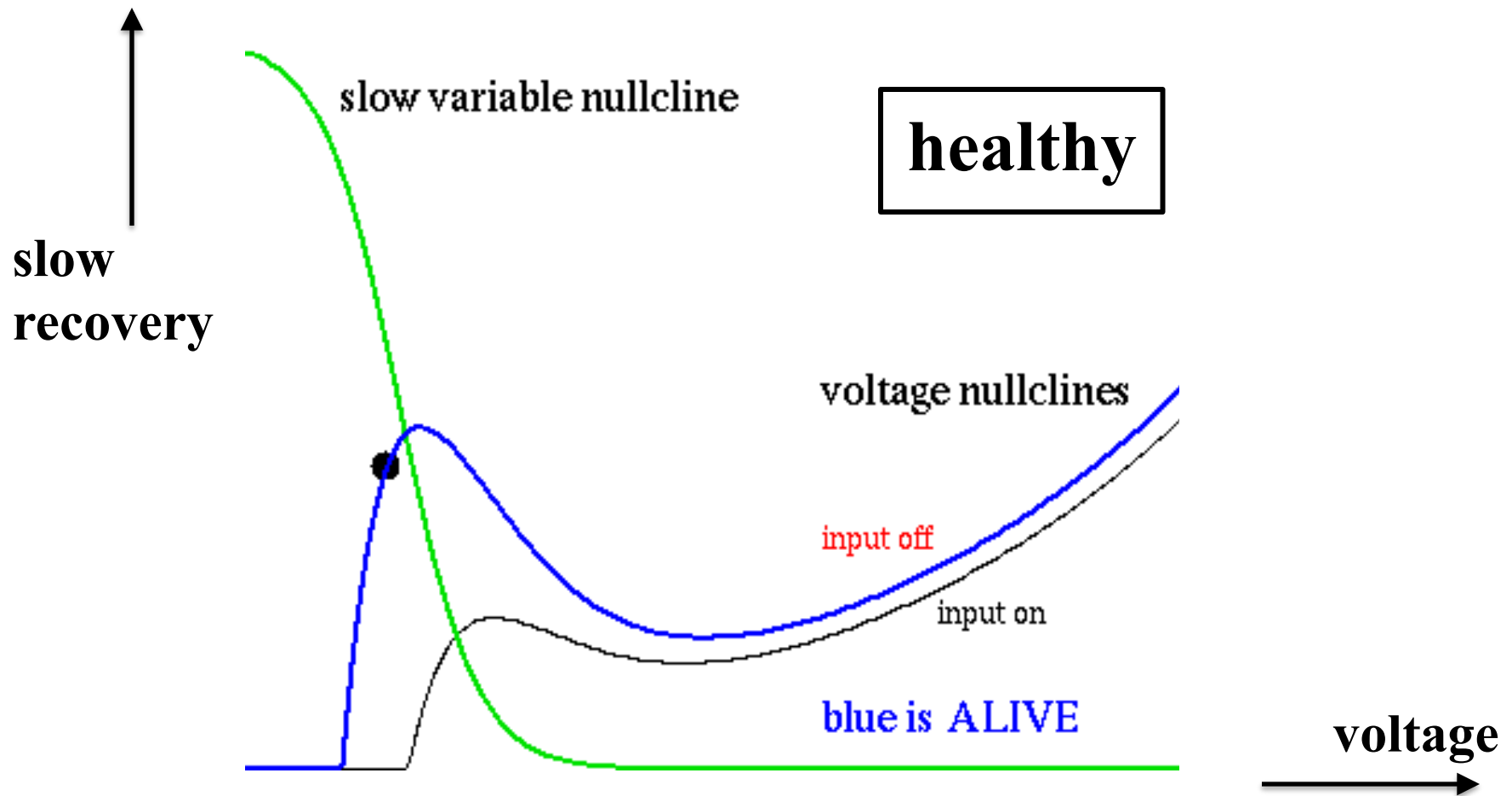


***paradox:* how can more inhibition make things better??**

**perhaps relay is compromised in PD!**

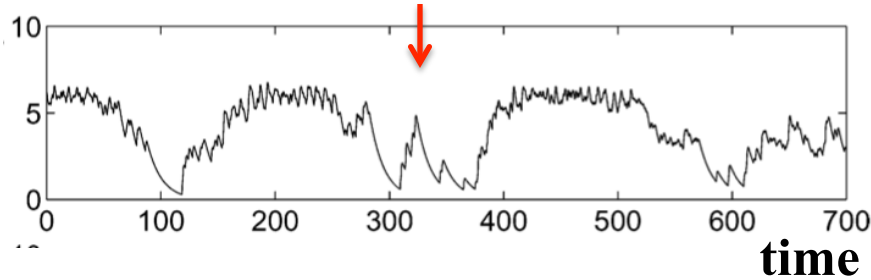
*answer:* **pattern** of inhibition trumps amount

**TC (relay) cell should give voltage spike to each input:**



*answer:* **pattern** of inhibition trumps amount

**PD** – *oscillation* of inhibition throws relay out of whack:



↑  
slow  
recovery

**PD**

slow variable nullcline

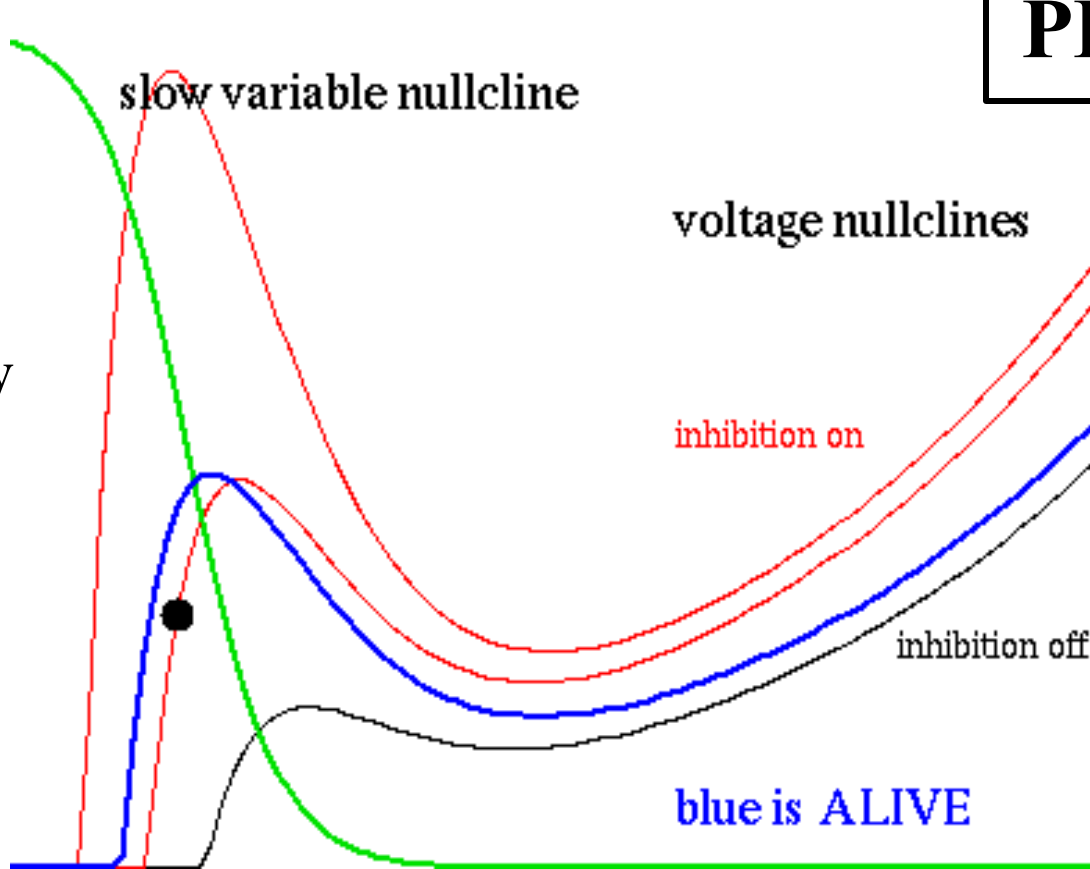
voltage nullclines

inhibition on

inhibition off

blue is ALIVE

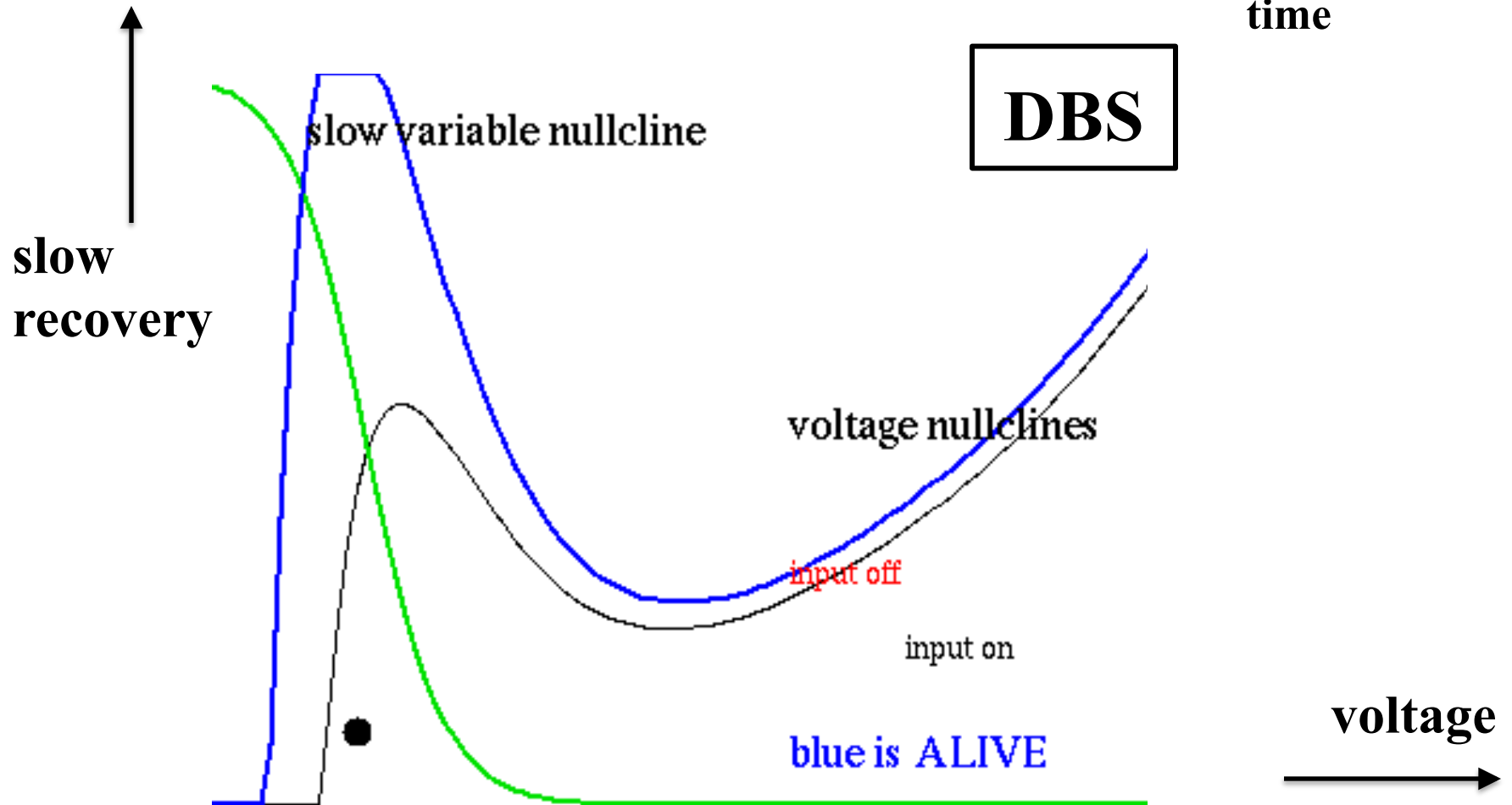
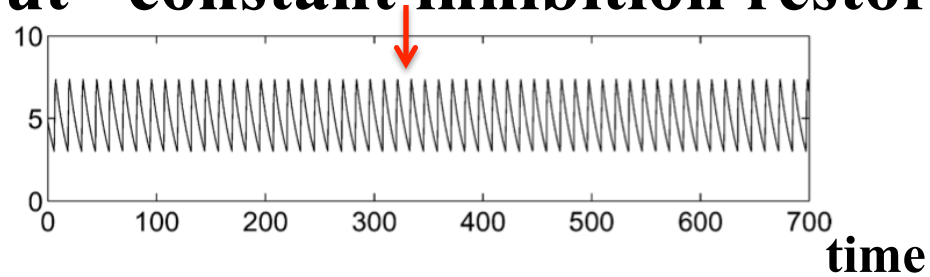
→  
voltage



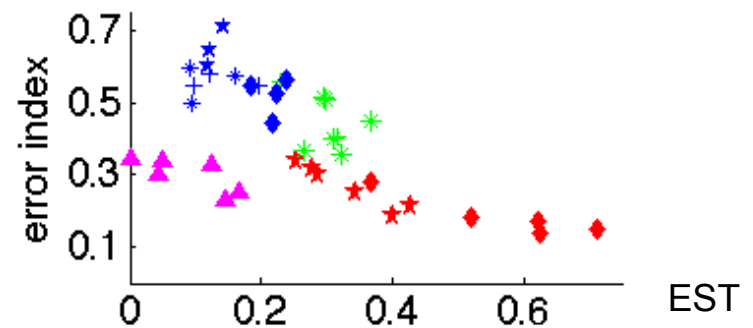
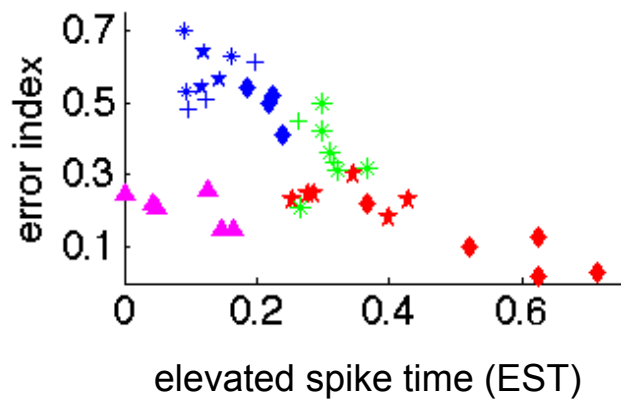
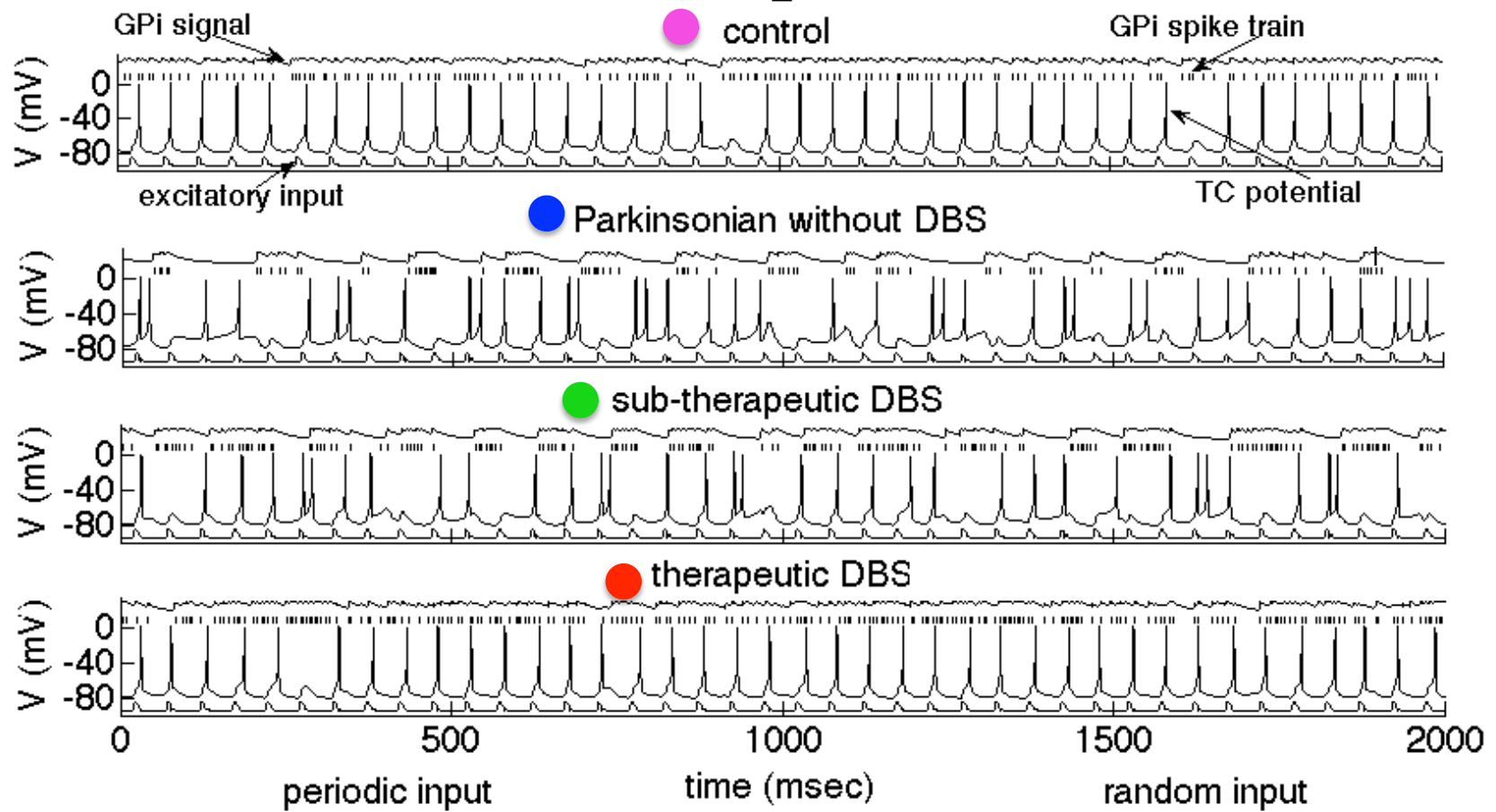


*answer:* **pattern** of inhibition trumps amount

**PD + DBS – higher but ~constant inhibition restores relay:**



# test with data-driven computational model



Guo\*, Rubin\* et al., *J. Neurophys.*, 2008

# Conclusions II

- parkinsonian oscillations in basal ganglia will be transmitted to thalamic relay cells

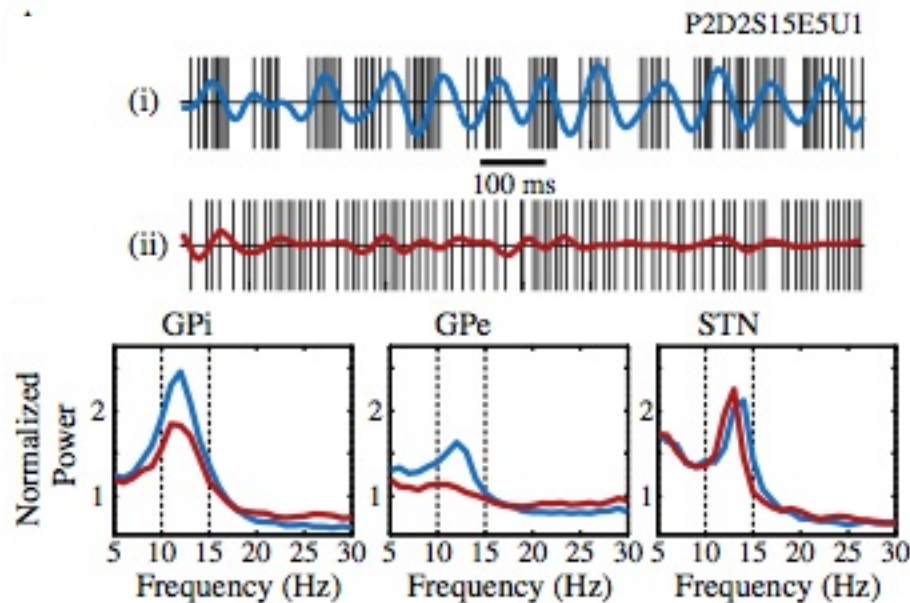
- inhibitory oscillations → compromise relay

- although DBS drives basal ganglia outputs and may yield larger inhibition, *inhibition that becomes less variable may restore relay* →

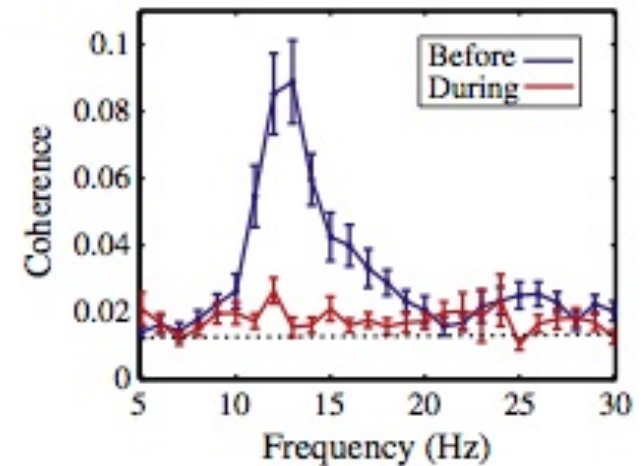


## more experiments on STN-DBS:

- (1) suppresses  $\beta$  oscillations in GPi despite ongoing  $\beta$  in STN (which drives GPi) and
- (2) destroys STN-GPi coherence



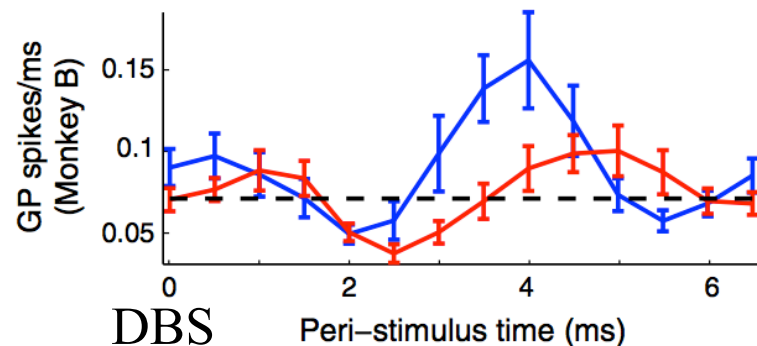
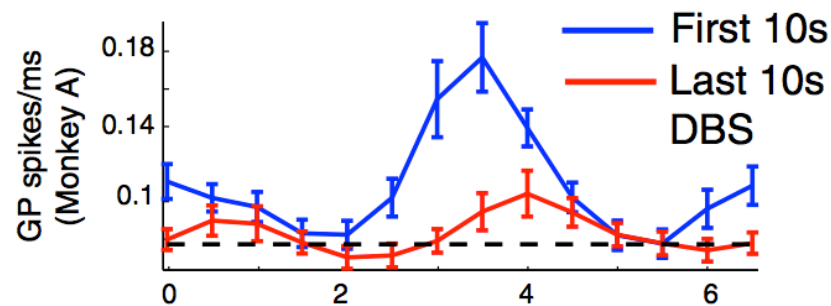
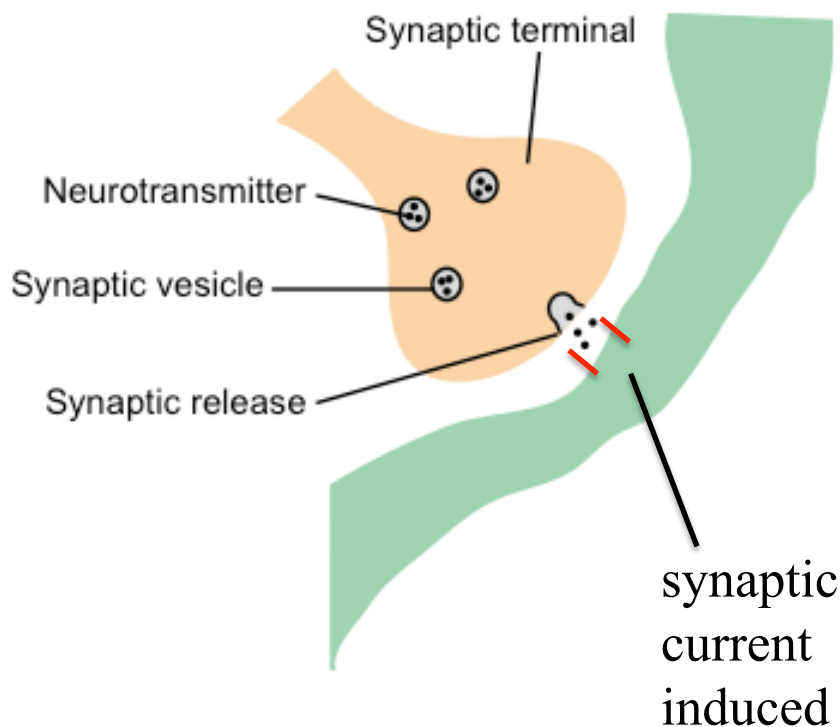
(2)



**idea 2: more STN spikes  $\nrightarrow$  proportionally more downstream inhibition: *synaptic depression***

neuronal synapse:

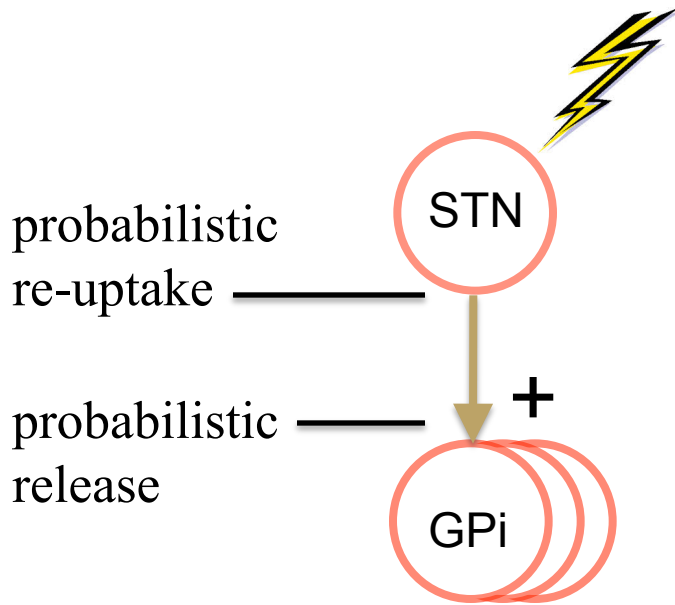
*clue:*



***GPI entrainment gradually reduced***

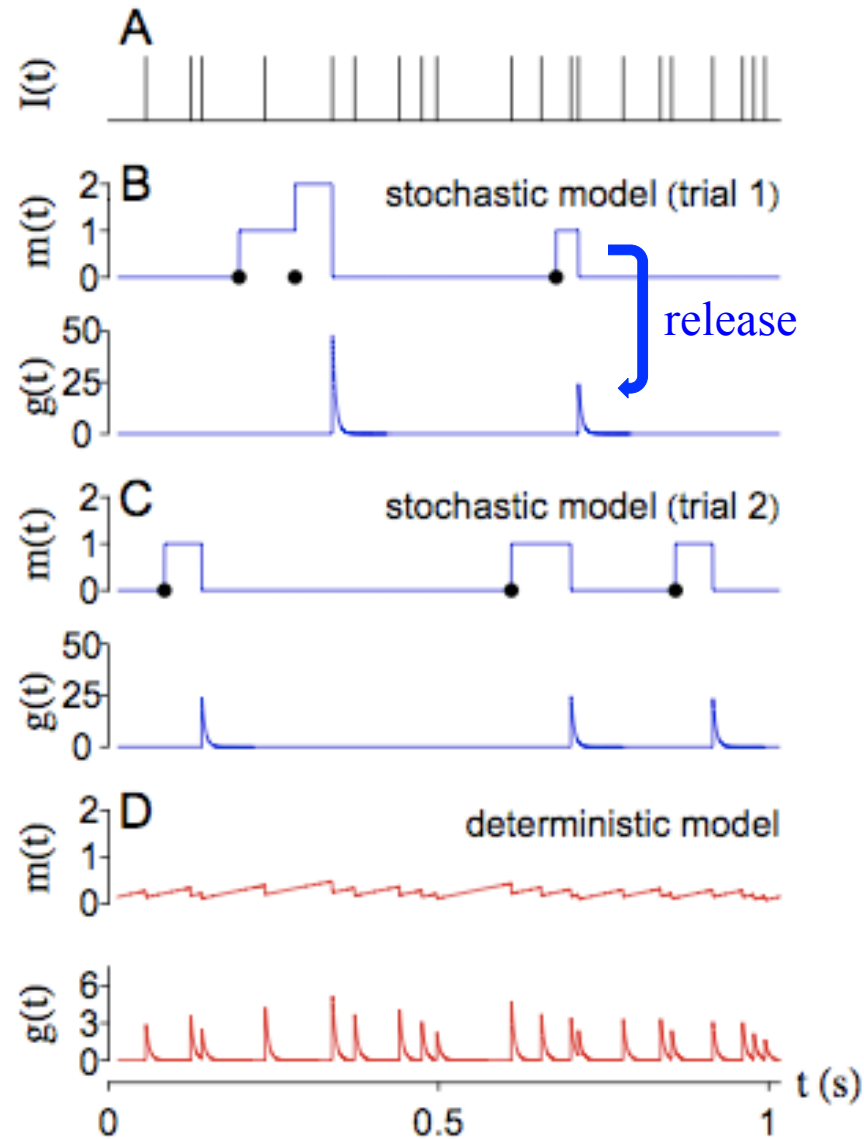


# stochastic vesicle dynamics



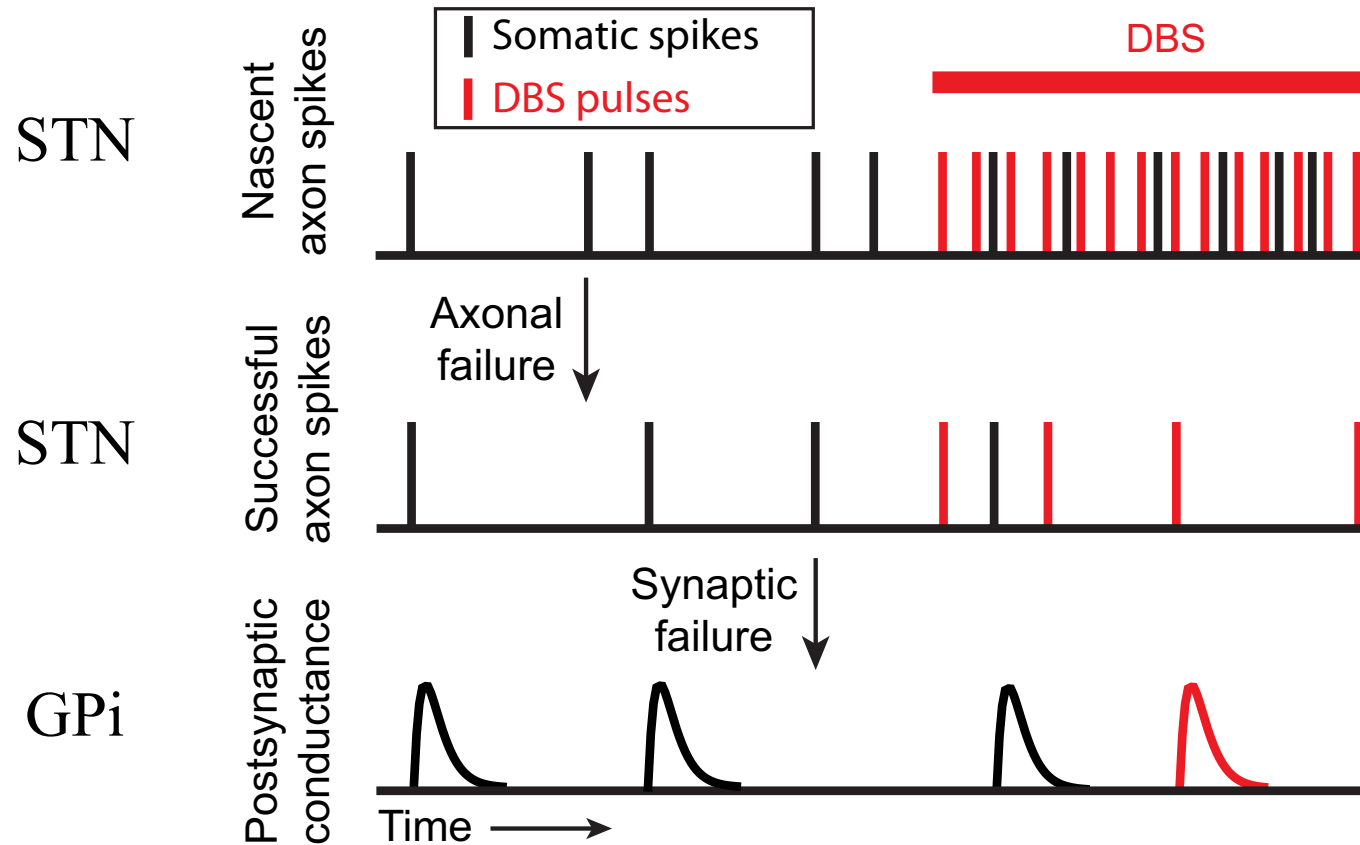
Rosenbaum et al., *PLoS Comp. Biol.*, 2012; *J. Neurophysiol.*, 2013

(see also: Abbott et al., 1997; Goldman et al., 1999; Fuhrmann et al., 2002; **Goldman, 2004**; de la Rocha & Parga, 2005; Grande & Spain, 2005, Lindner et al., 2009, Merkel & Lindner, 2010)

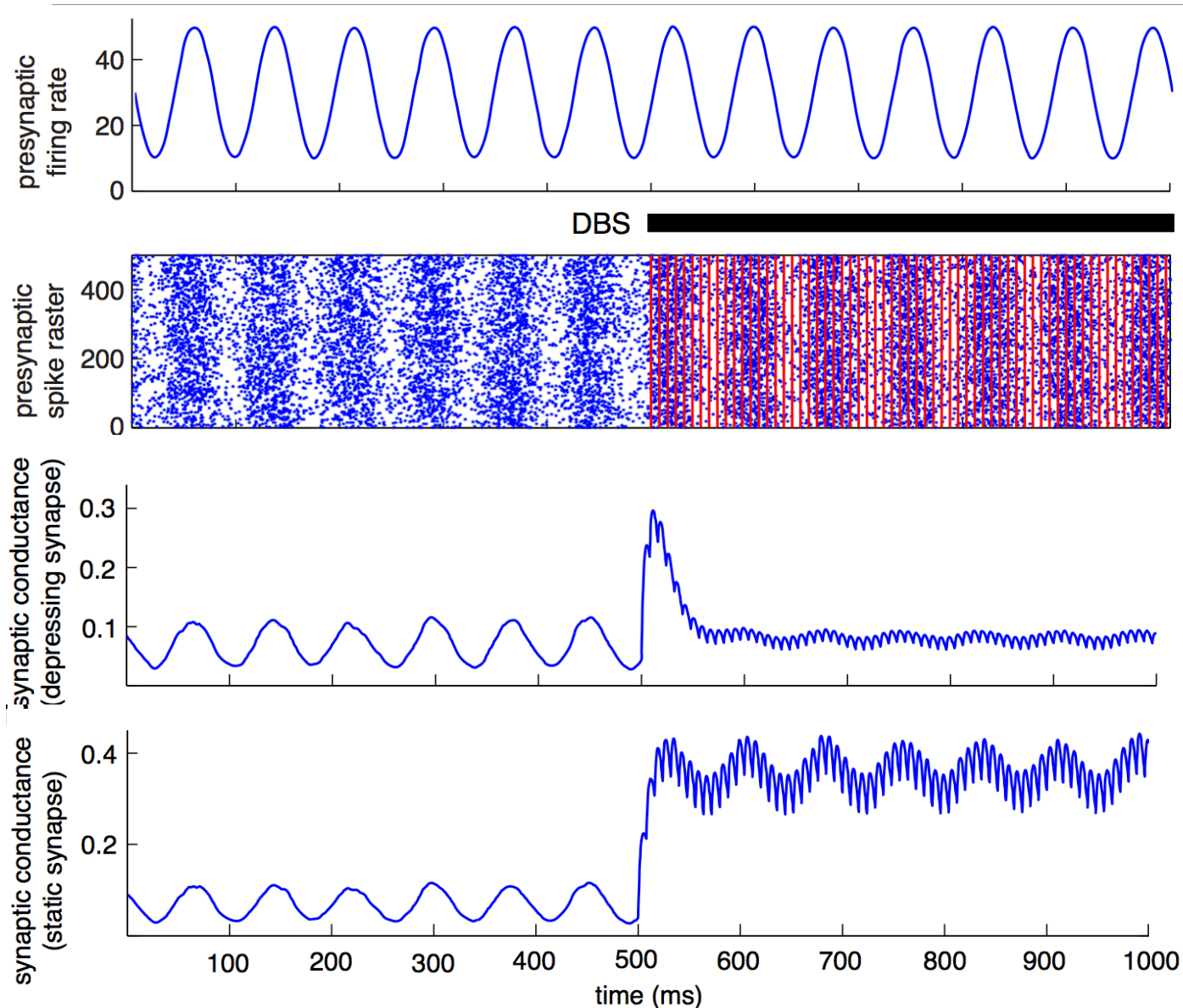


- $m(t)$  = number of available vesicles
- $g(t)$  = synaptic conductance

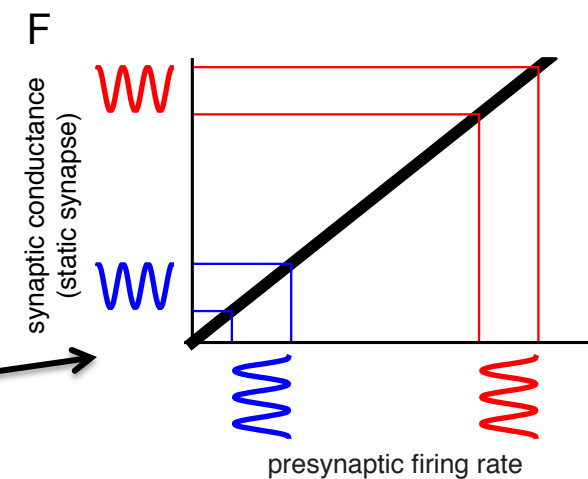
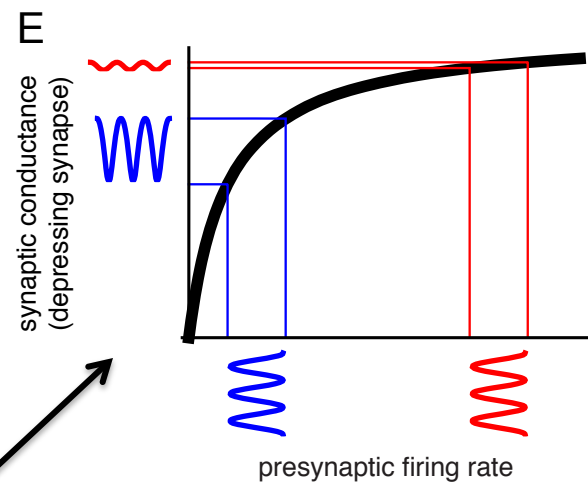
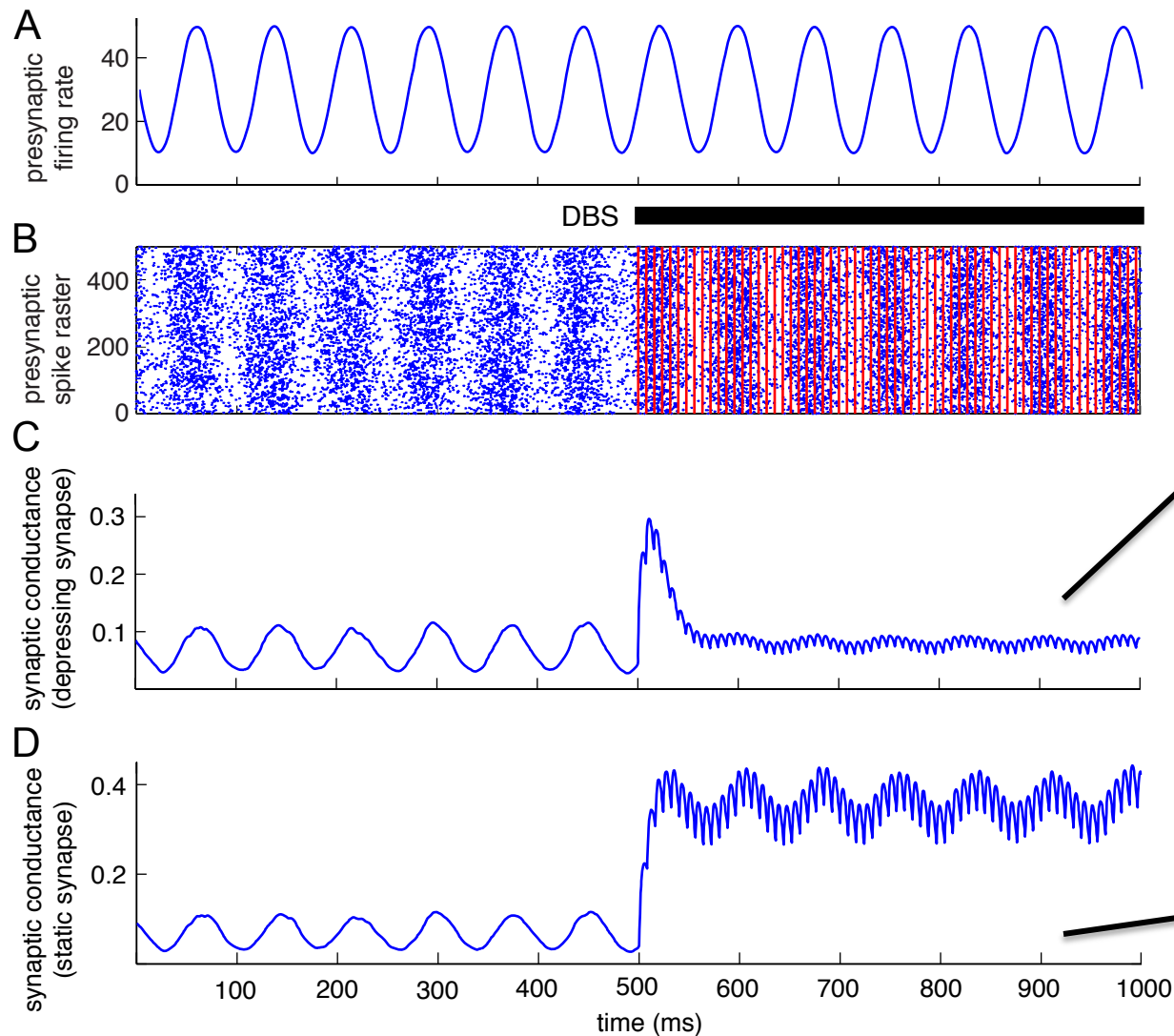
# computational model (1) of short term depression in STN-GPi pathway



# DBS-induced synaptic depression suppresses the transfer of low frequency oscillations



# DBS-induced synaptic depression suppresses the transfer of low frequency oscillations

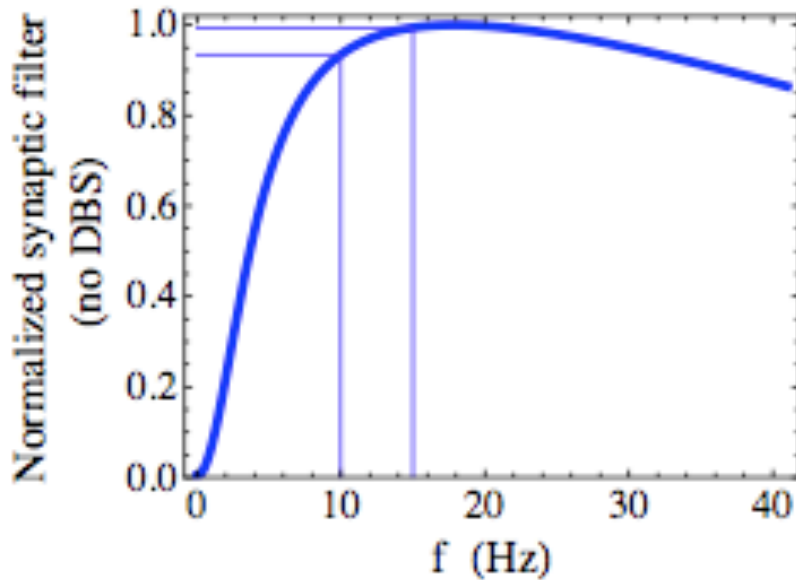


# key expression

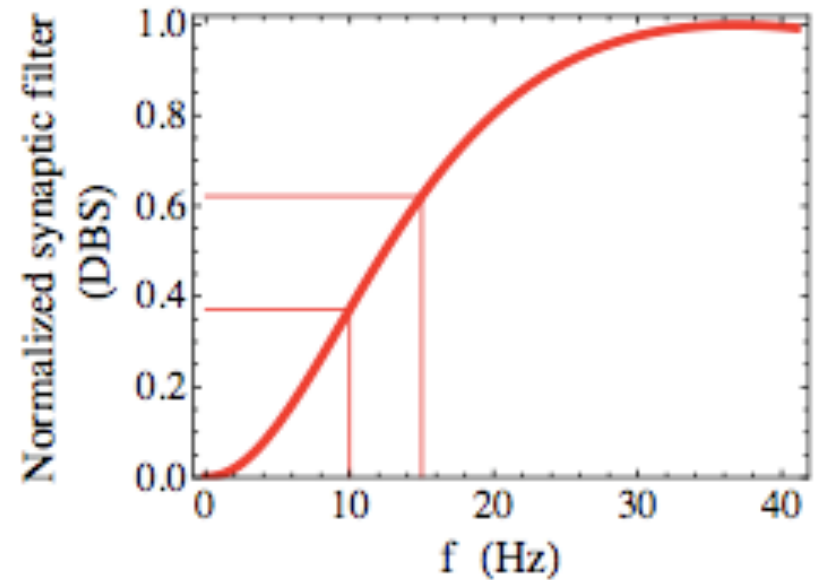
Poisson re-uptake rate      release probability      firing rate

$$f_0 = (1/\tau_u + U\nu)/(2\pi)$$

*effective synaptic cutoff frequency*



blue: before stimulation

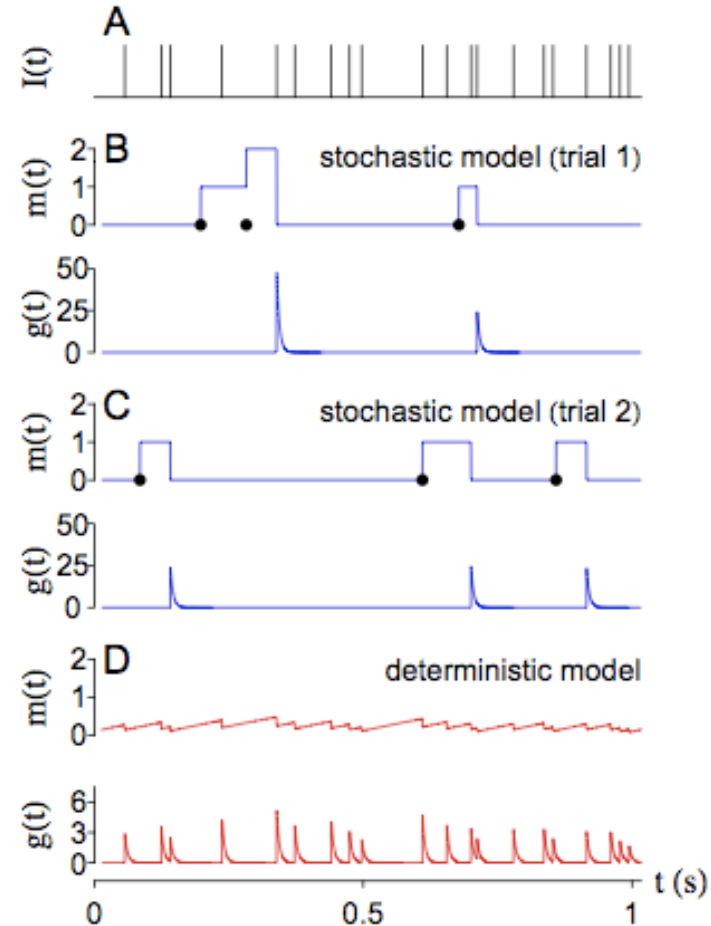
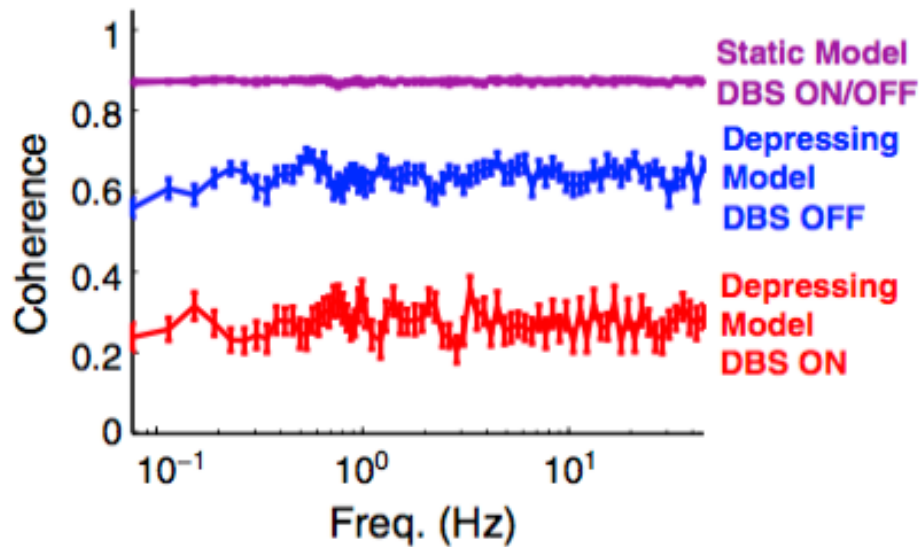


red: during STN-DBS

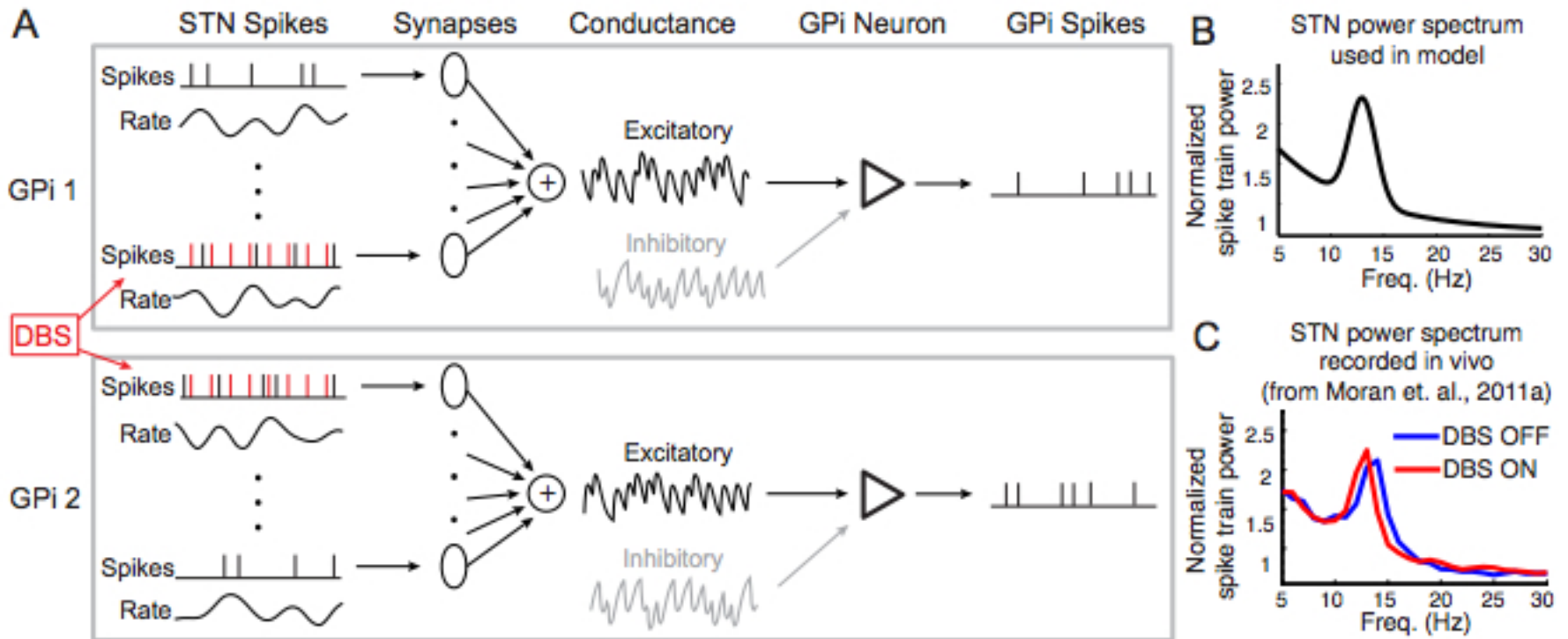
- STN  $\beta$  transmission to GPi suppressed in STN-DBS & GPi output becomes less oscillatory, less tied to STN

# DBS-induced synaptic depression suppresses downstream coherence

for high rate inputs, uptake contributes relatively more to transmission:  
decorrelate inputs and outputs, *lower coherence within GPe & with STN*



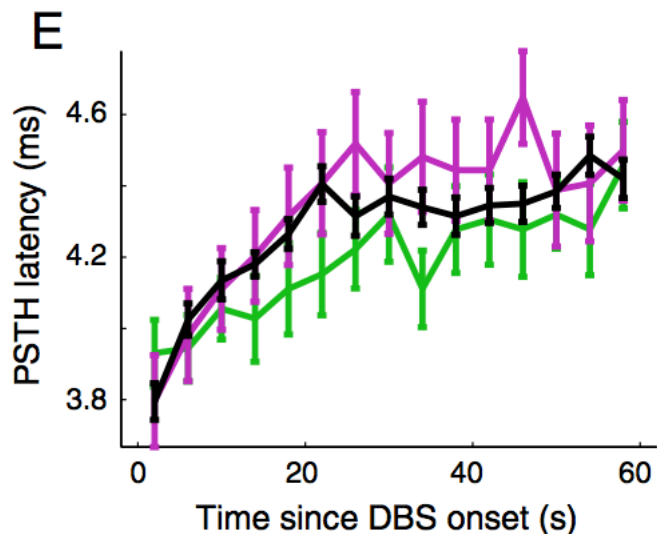
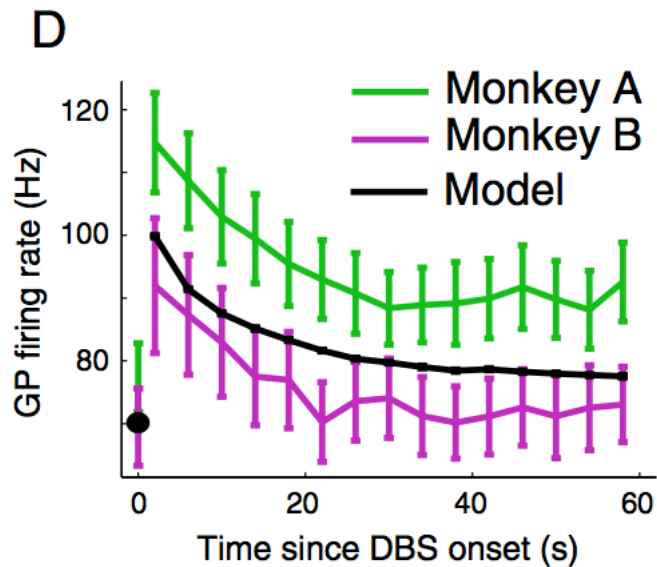
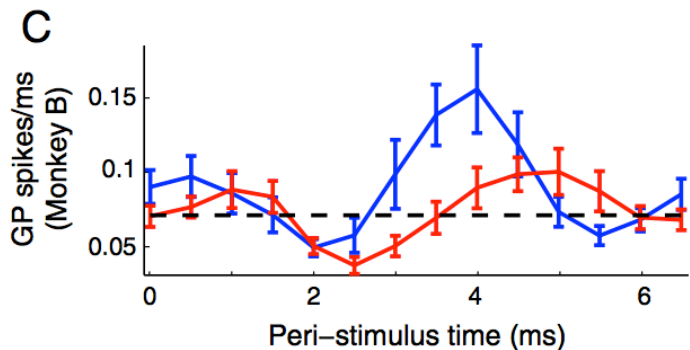
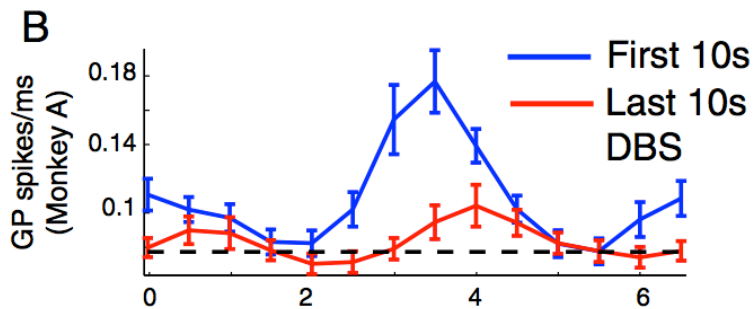
# computational model (2) of short term depression in STN-GPi pathway





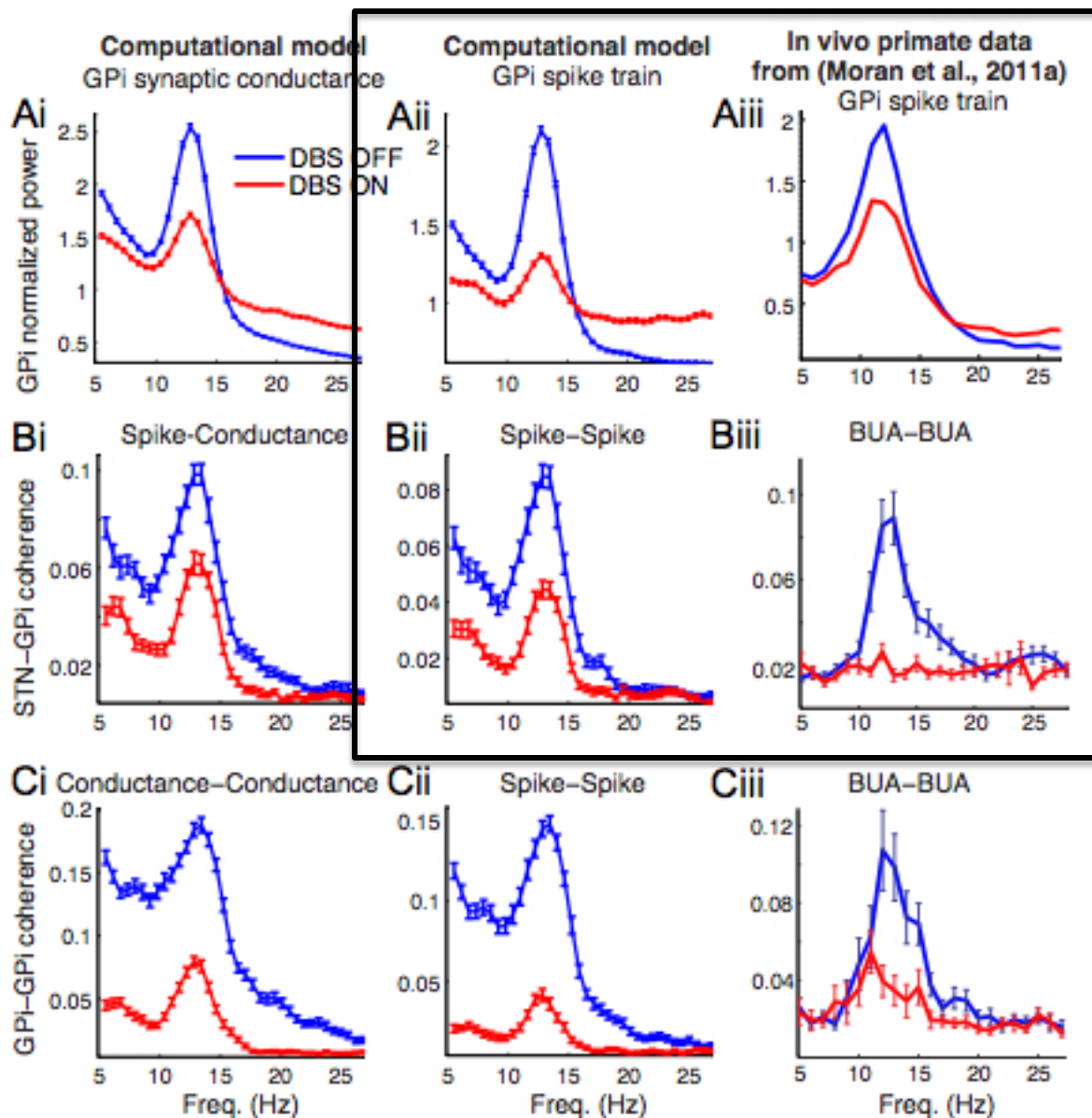
# results from computational model:

-- gradual decrease in entrainment, as in data



# results from computational model:

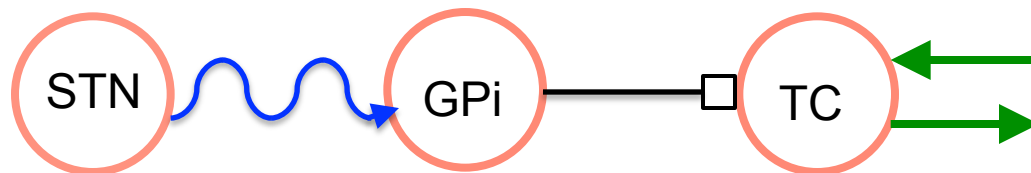
-- reduced beta oscillations and coherence, ~ as in data



cf. Moran et al.,  
*Neurobiol. Disease*, 2012

# FINAL SUMMARY on DBS

- **mechanism 1:** bursting in GPi can compromise thalamic relay in parkinsonism
- **STN-DBS** that entrains and regularizes GPi can restore TC relay
- **mechanism 2:** excessively synchronized  $\beta$  oscillations in GPi can compromise thalamic relay
- **STN-DBS** weakens GPi  $\beta$  & synchrony and makes GPi output less coherent/more steady – explained based on short term (synaptic and axonal) depression, also restores relay



# Collaborators

## Pallidostriatal circuit

- **Aryn Gittis, Carnegie Mellon University**
- *Victoria Corbit, CNUP*
- *Tim Whalen, PNC*
- *Kevin Zitelli, CNUP*
- *Stephanie Crilly, CMU*

## Basal ganglia and DBS modeling

- **David Terman, Ohio State**
- **Yixin Guo, Drexel University**
- Cameron McIntyre, CWRU
- Charles Wilson, UTSA
- Alice Yew, AMS
- Jerry Vitek, U. Minnesota

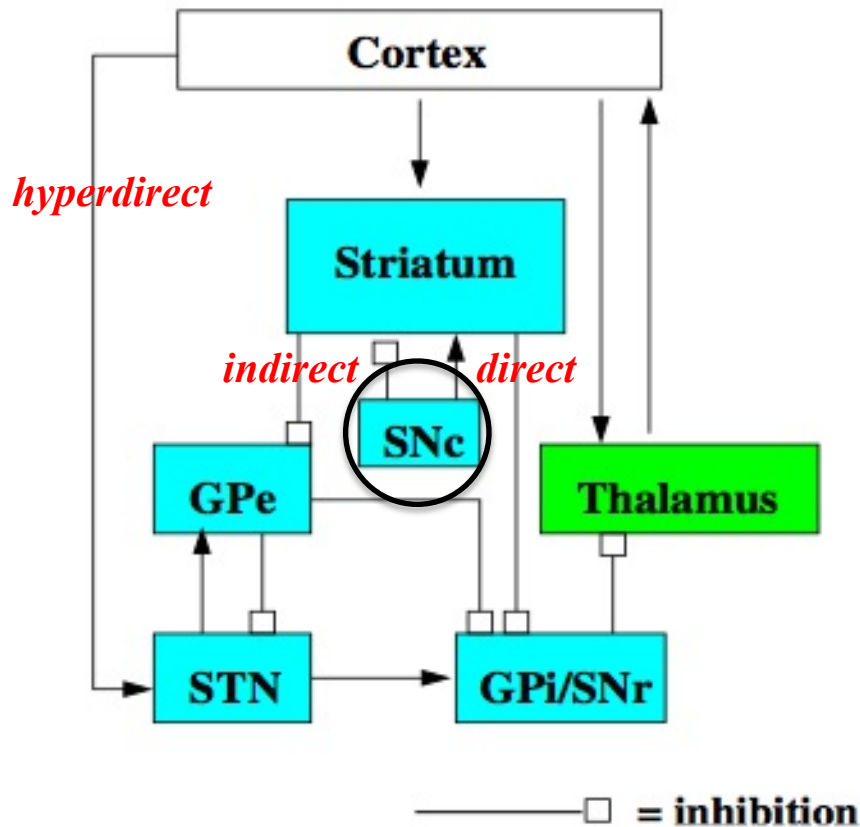
## Short term depression and DBS

- **Robert Rosenbaum, Notre Dame**
- **Robert Turner, Pitt**
- Brent Doiron, Pitt
- Andrew Zimnik, Columbia
- Christian Alzheimer, Nürnberg
- Fang Zheng, Nürnberg

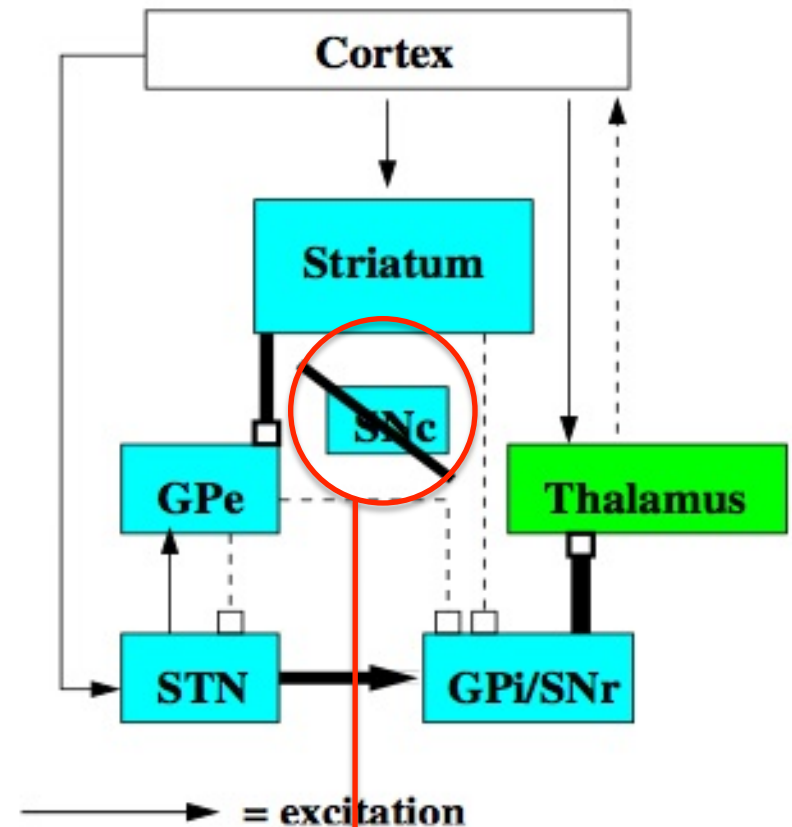


# Albus and DeLong: classical (1980's) arithmetical model of the basal ganglia (light blue) and PD

**normal**



**PD**



dopamine loss:

**imbalance of pathways**

**fundamental question of parkinsonism (1990's): how can changes in *rates* account for the parkinsonian symptoms?**

**what:** akinesia (difficulty initiating movement), bradykinesia (slowed movement), posture issues, rigidity, tremor

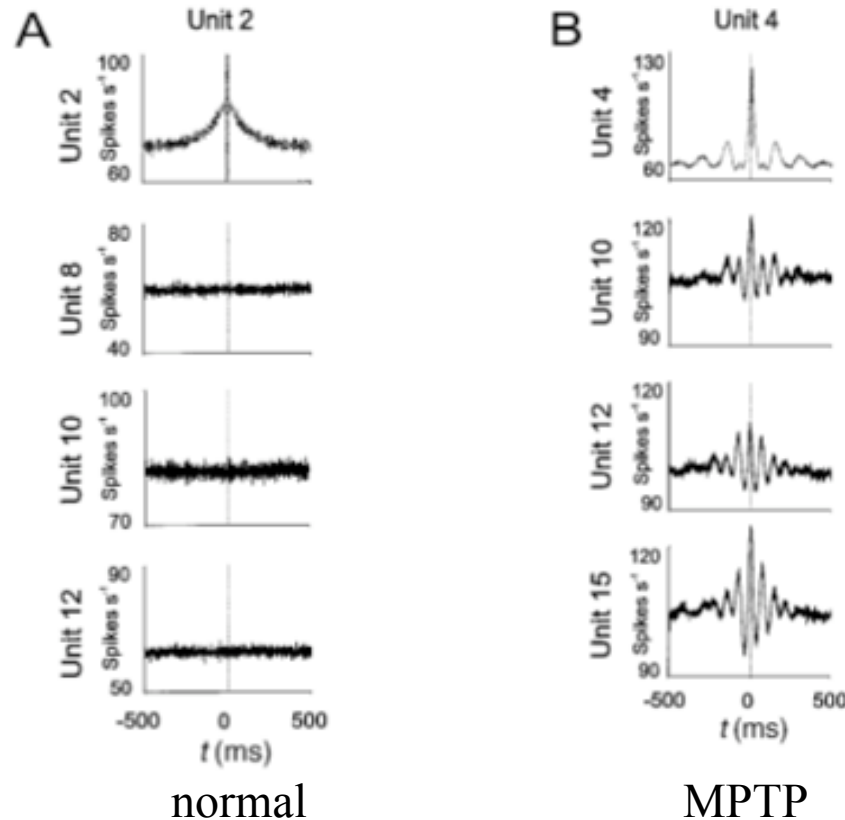
**A: they can't!**

**revised Q: (a) what changes in BG activity result from loss of dopamine, (b) how are these changes produced, (c) how do these changes translate into symptoms, and (d) how can these symptoms be mitigated?**



# altered BG activity patterns in parkinsonism

- *increased synchrony/correlations, loss of specificity*



Bergman et al., *TINS*, 1998; globus pallidus recordings

# (a) changes in BG activity in parkinsonism

- *changes in firing rates*
- *increased oscillations*
- *increased burstiness*



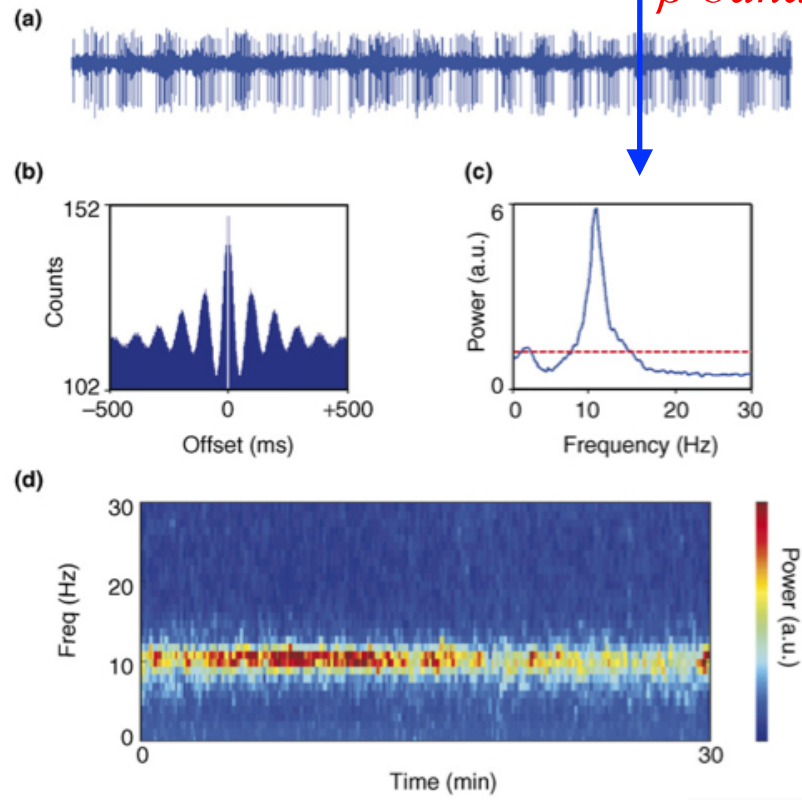
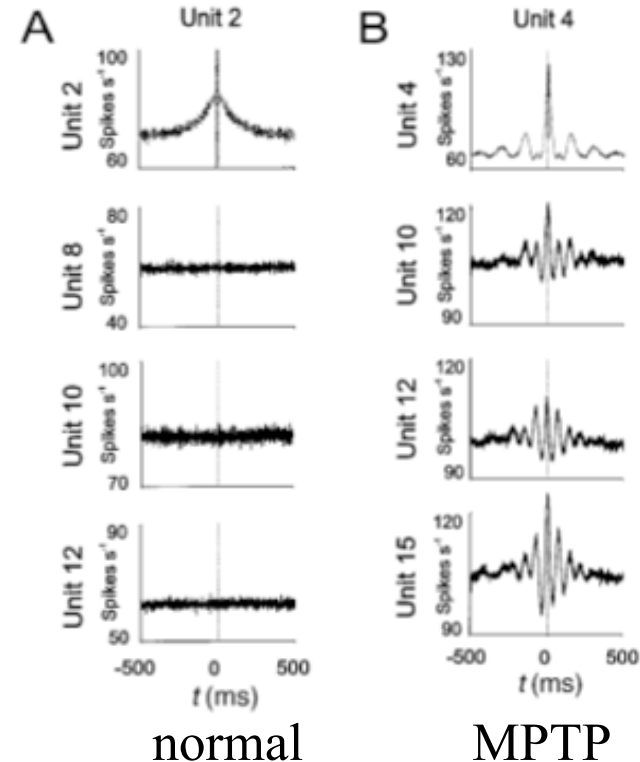
Magnin et al., *Neuroscience*, 2000

*$\beta$ -band*

- *increased correlations*

Bergman et al., *TINS*, 1998; GP

Hammond et al., *TINS*, 2007; GPi

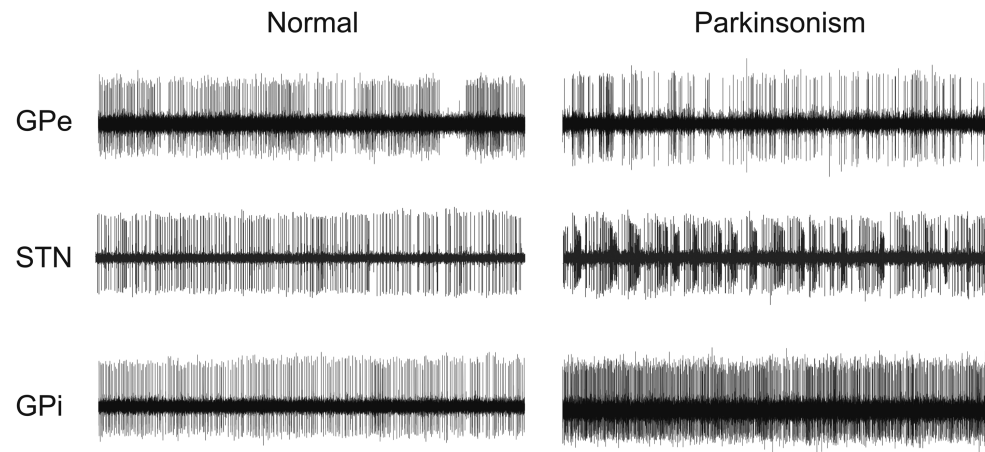
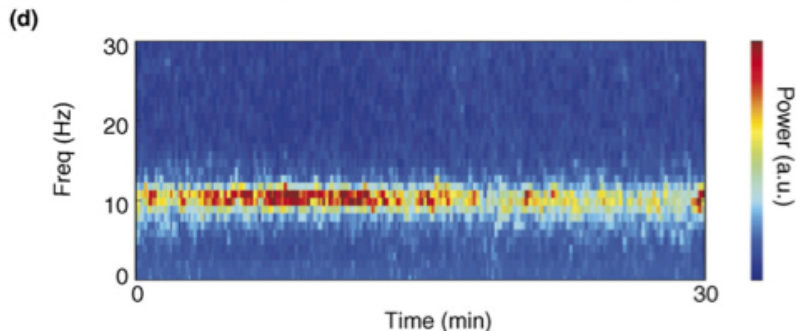
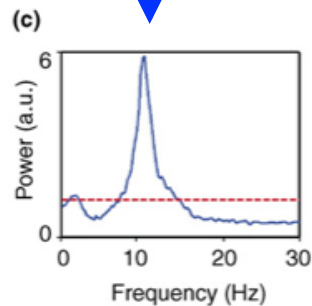
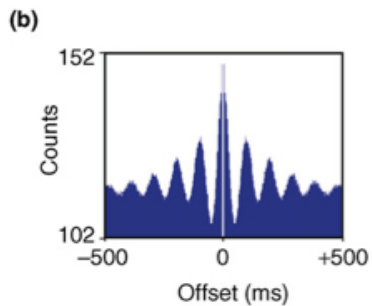


# (a) changes in BG activity in parkinsonism

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Magnin et al., *Neuroscience*, 2000



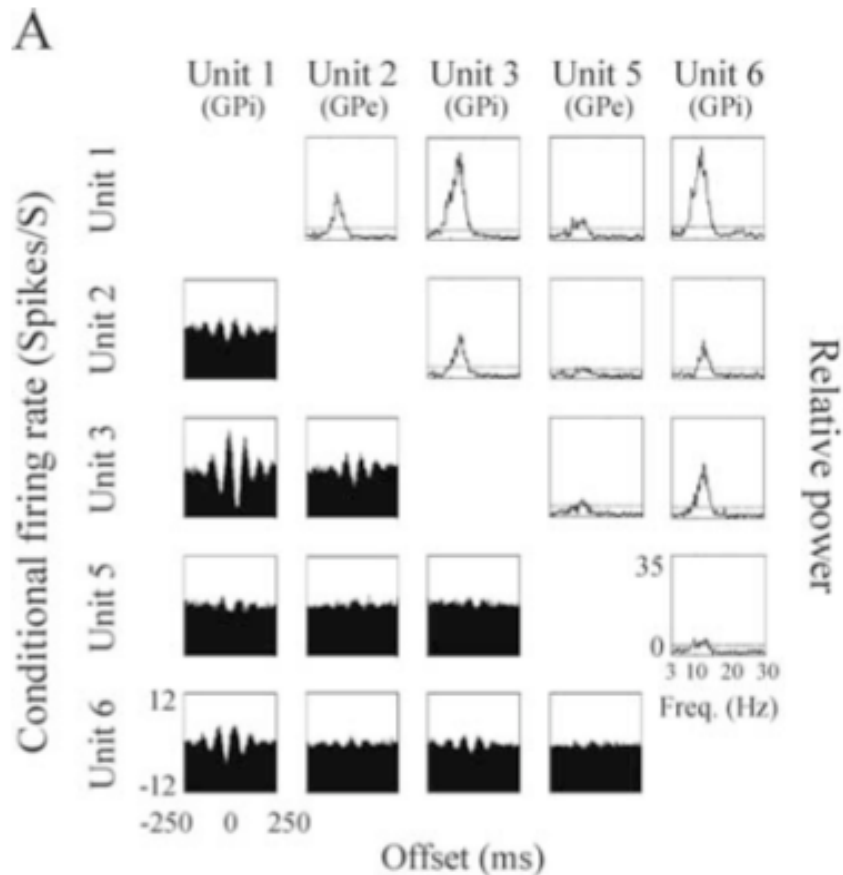
1 s

Galvan & Wichmann, *Clin. Neurophysiol.*, 2008

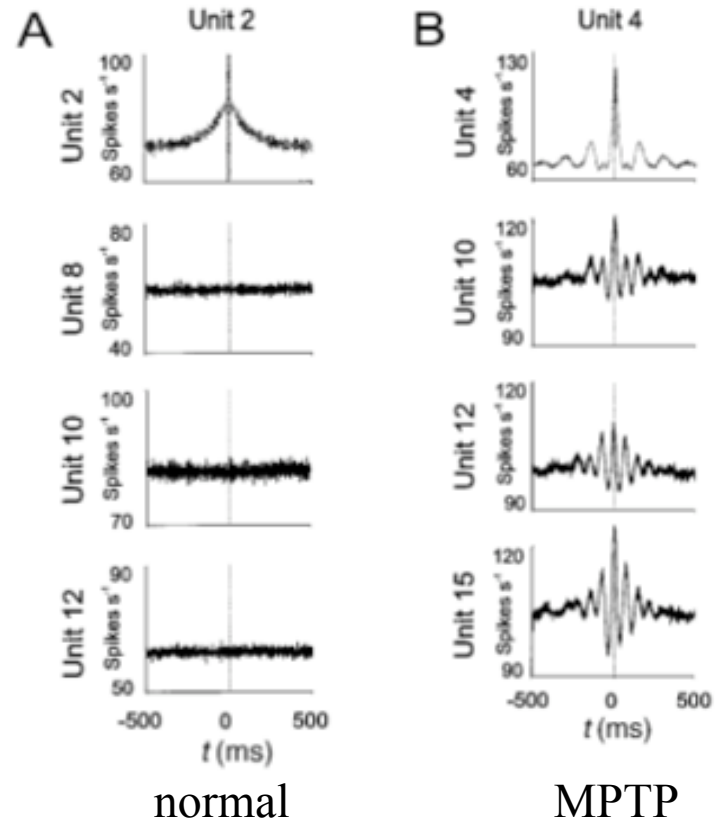
Hammond et al., *TINS*, 2007; GPI

# altered basal ganglia activity patterns in parkinsonism

- *loss of specificity/increased correlations*



Heimer et al., *J. Neurosci.*, 2006



Bergman et al., *TINS*, 1998; globus pallidus recordings

# some past computational models w/oscillations

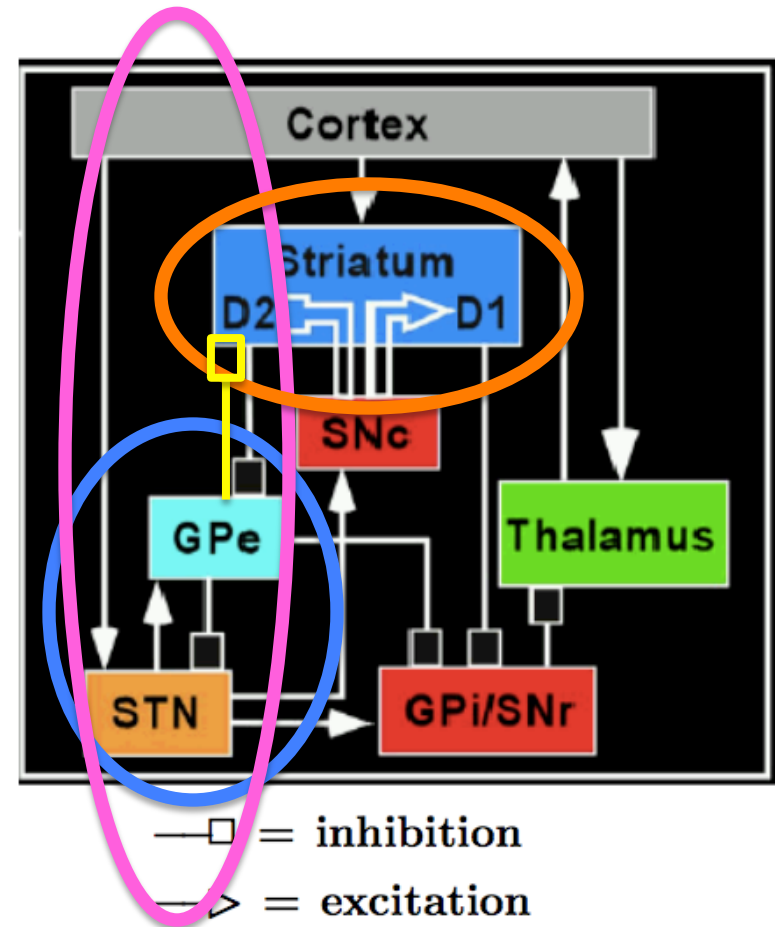
[Terman et al., 2002](#): STN-GPe (E-I loop); cf. Park & Rubchinsky

[Leblois et al., 2006](#): symmetry-breaking in full BG activity-based model

[Nevado-Holgado et al., 2010](#): STN-GPe firing rate model;  $\beta$  oscillations require cortical excitation to STN and synaptic delays

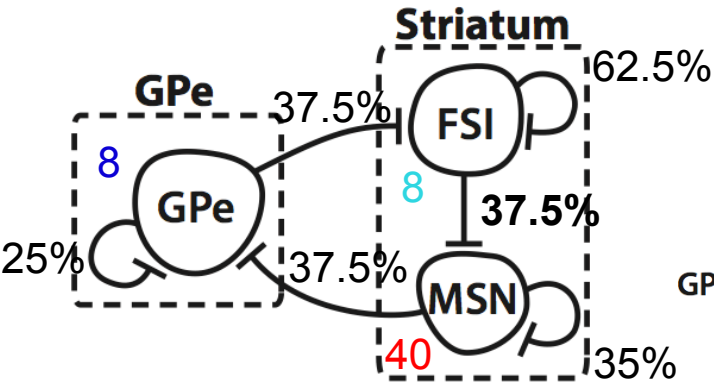
[McCarthy et al., 2011](#): inhibitory interactions in striatal medium spiny neurons (MSNs) sufficient for  $\beta$

[Kumar et al., 2011](#): large scale (LIF) STN-GPe model

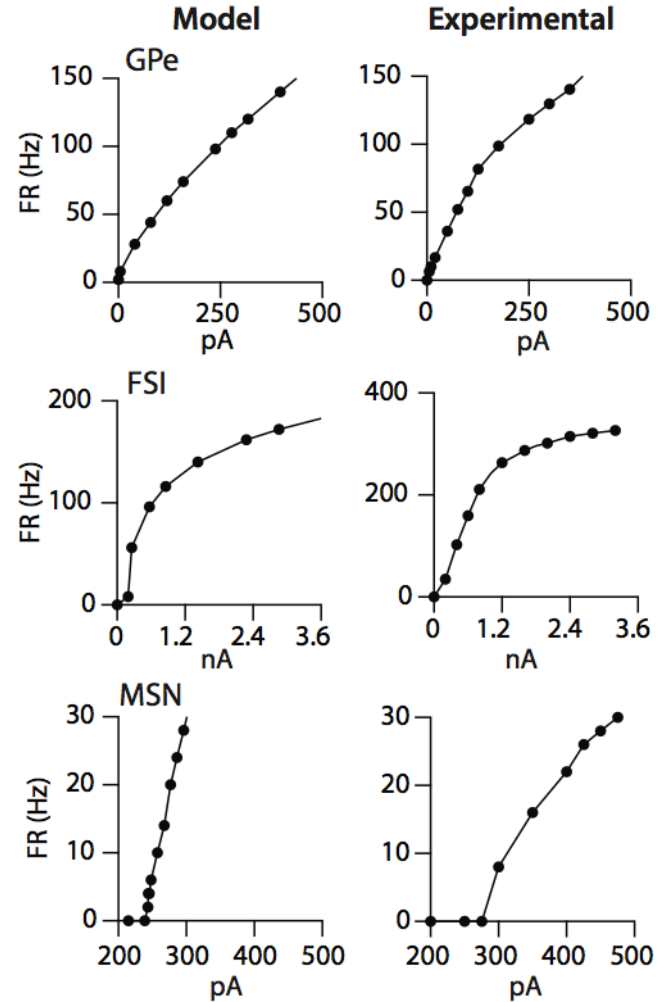
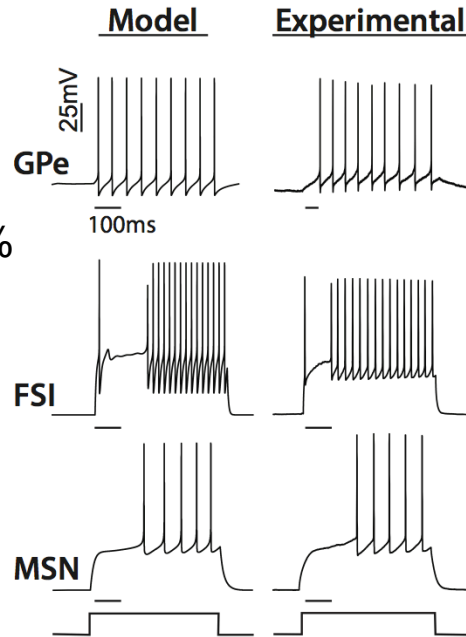
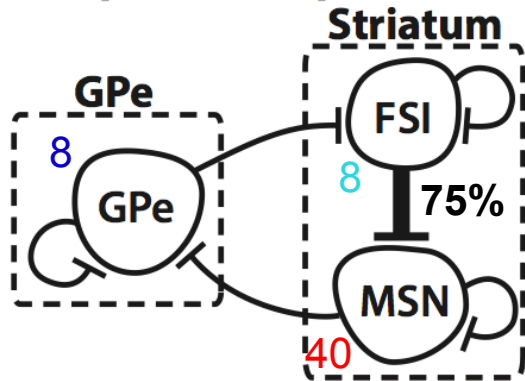


# pallidostriatal circuit model

## Control

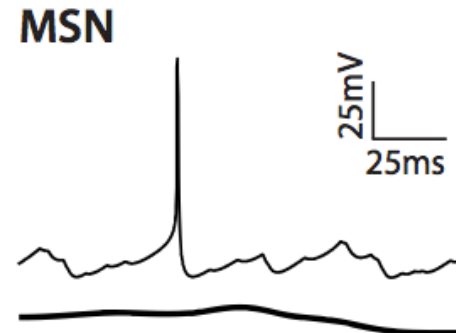
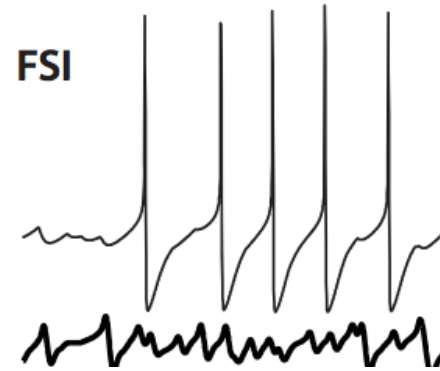
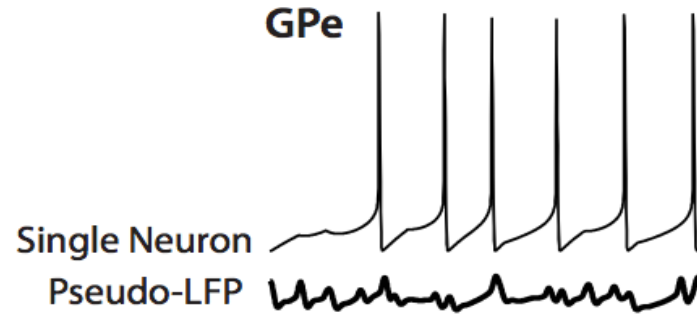
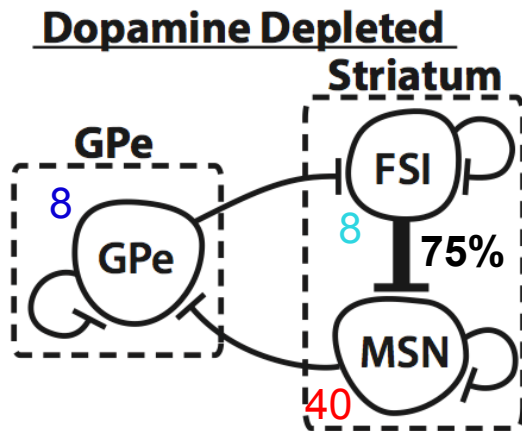
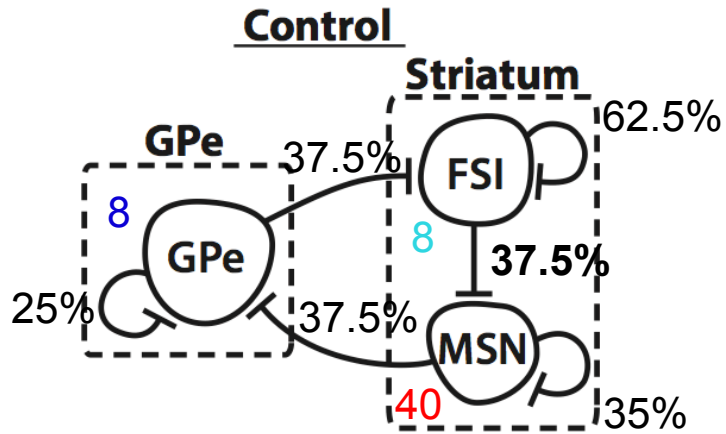


## Dopamine Depleted



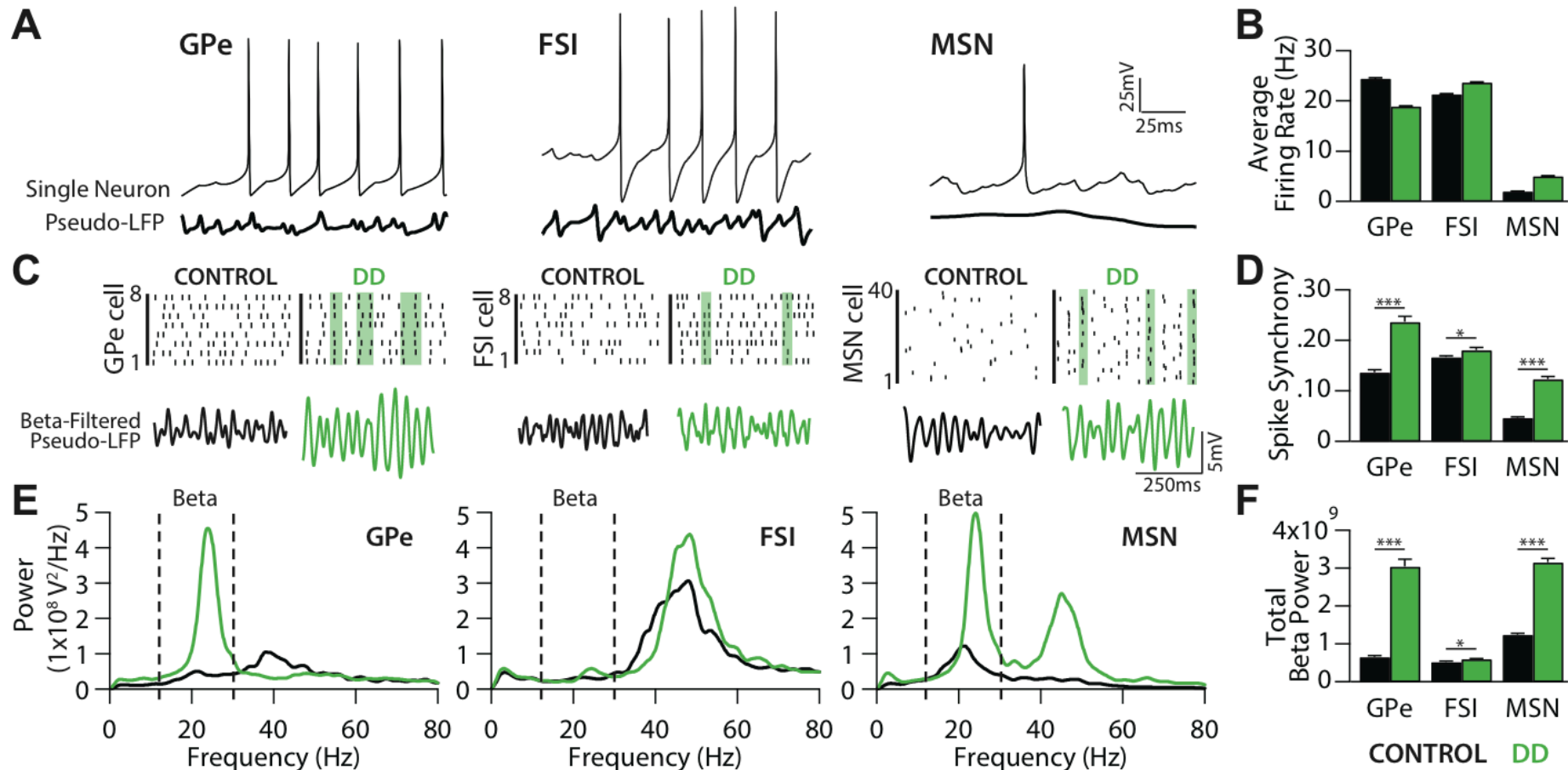
single cell responses

# pallidostriatal circuit model



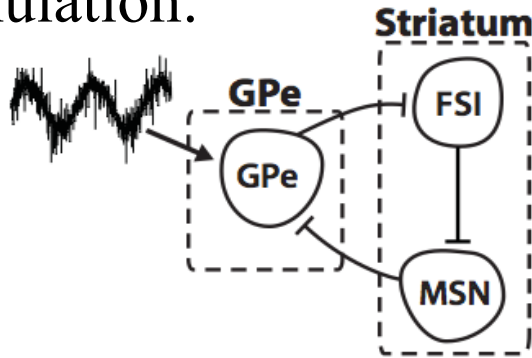


# model generates $\beta$ oscillations only in DD

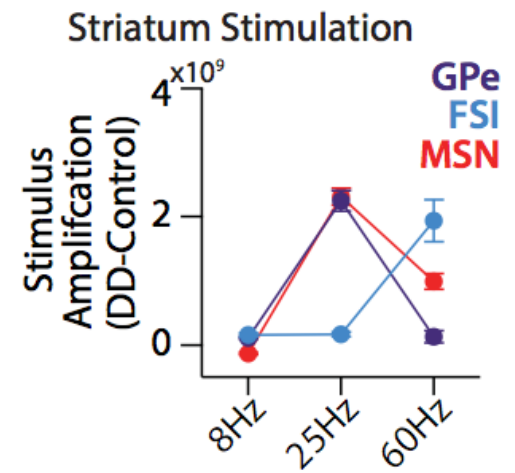
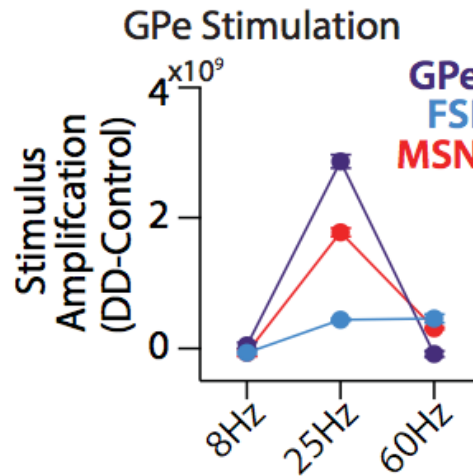
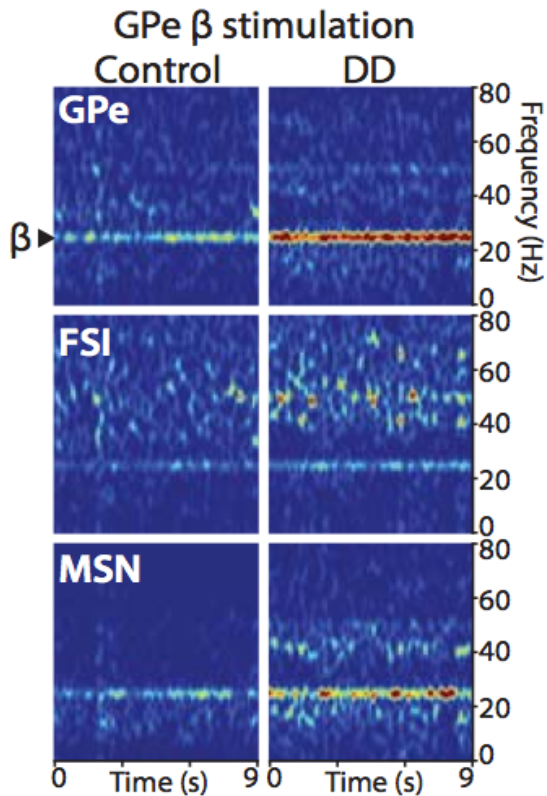
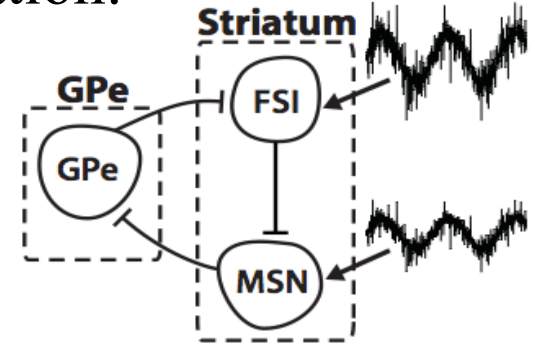


# pallidostriatal circuit could amplify $\beta$

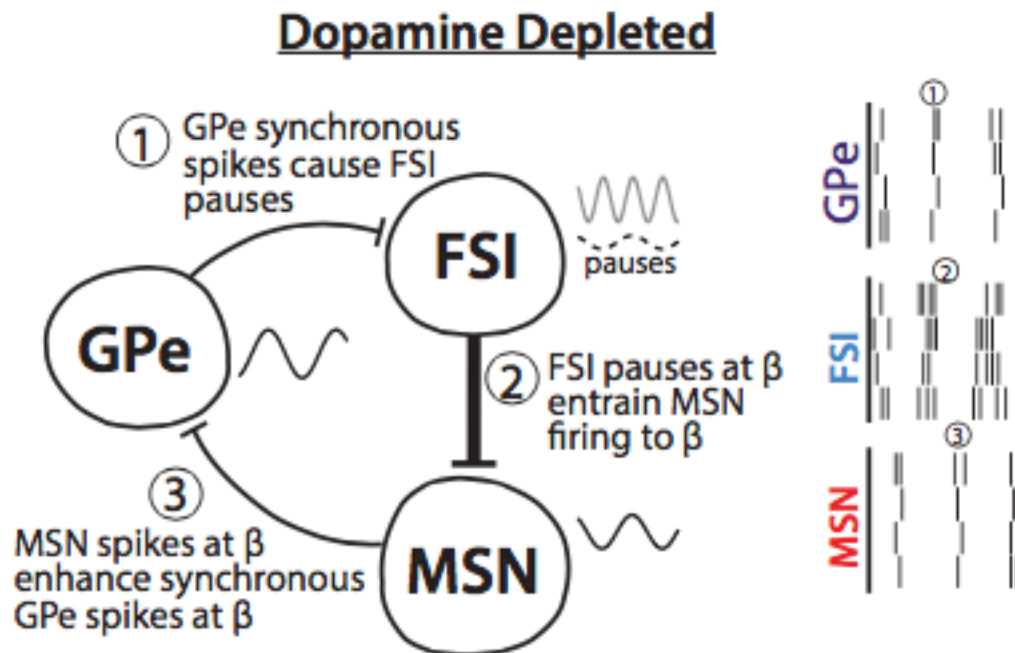
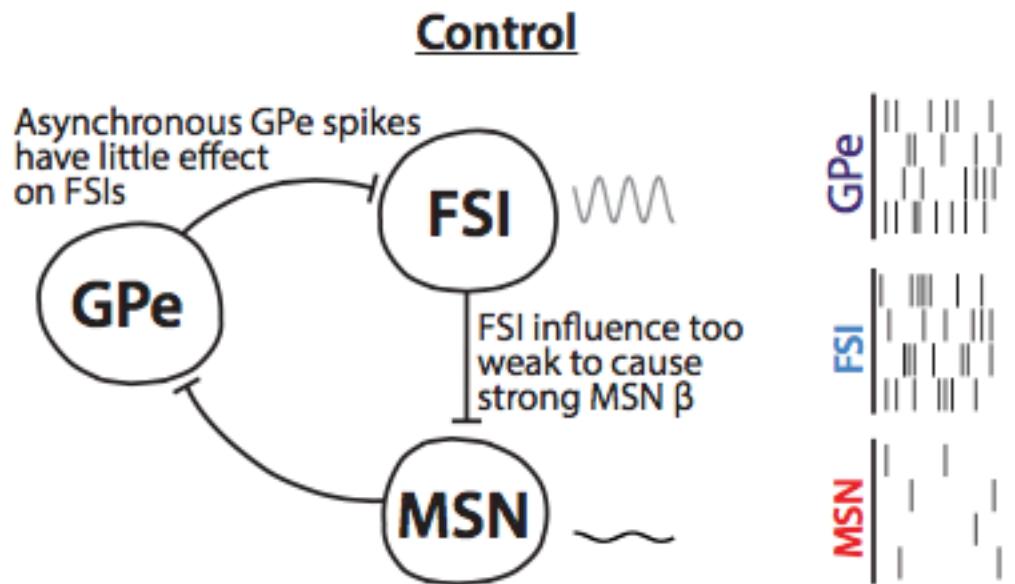
GPe stimulation:



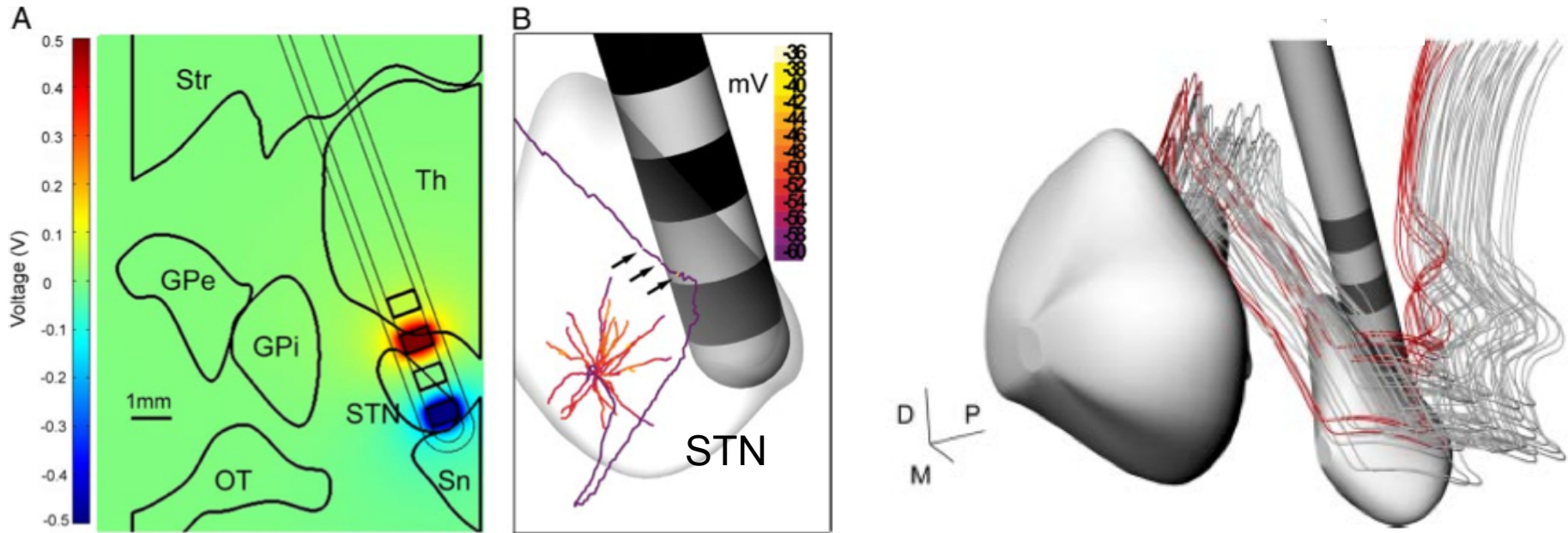
striatal stimulation:



# thrown for a loop



# zooming in

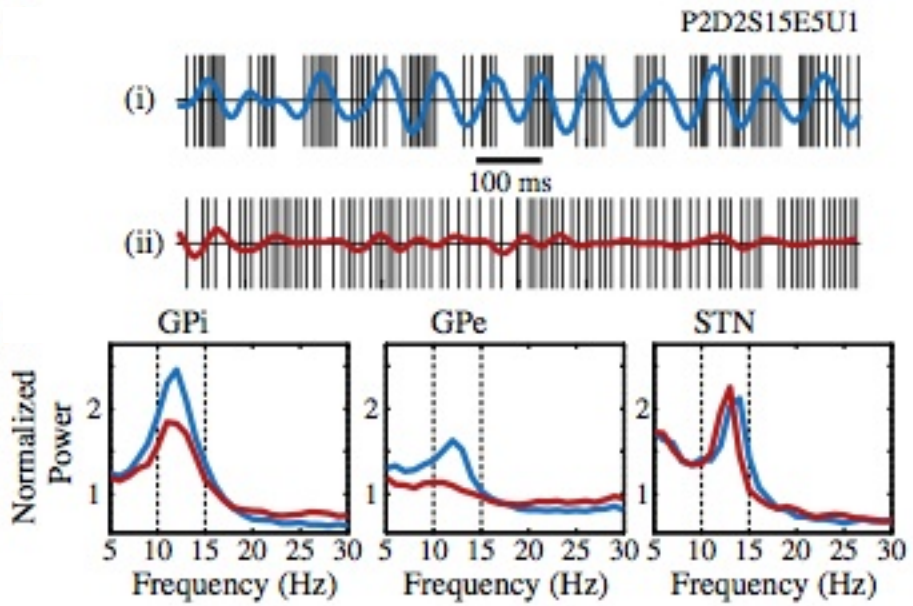


Miocinović et al., *J. Neurophysiol.*, 2006

OP: looks great – but how does this work??

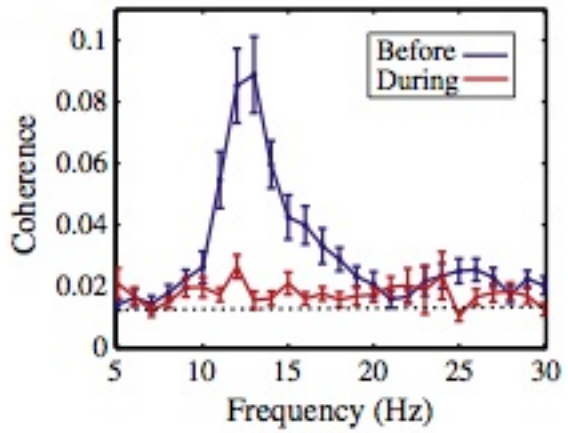
**more experiments: STN-DBS (1) suppresses beta oscillations in GPi despite ongoing beta in STN (which drives GPi) and (2) destroys GPi-STN coherence despite (3) GPi entrainment to STN in DBS**

**(1)**



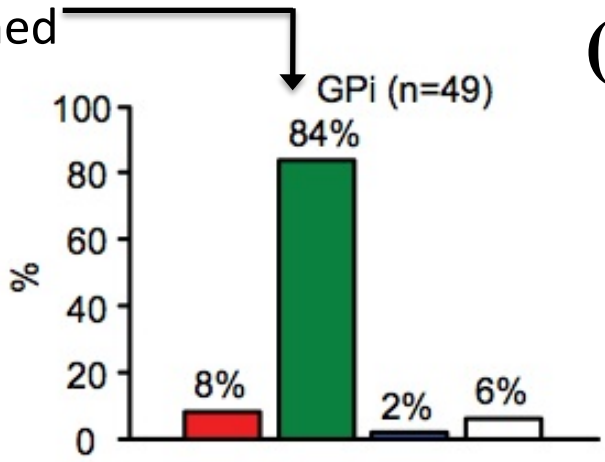
Moran et al.,  
2011 & 2012

**(2)**

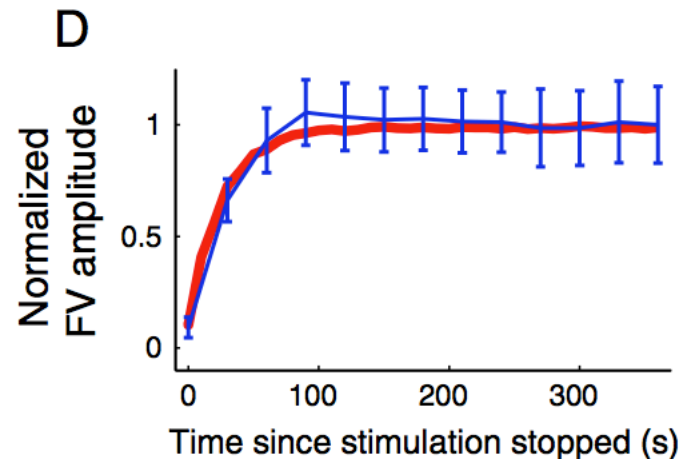
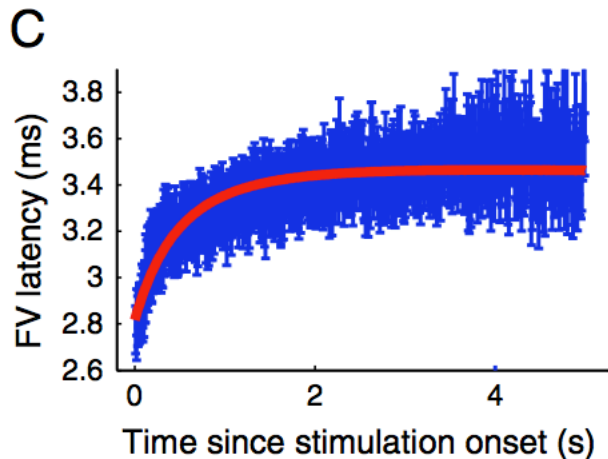
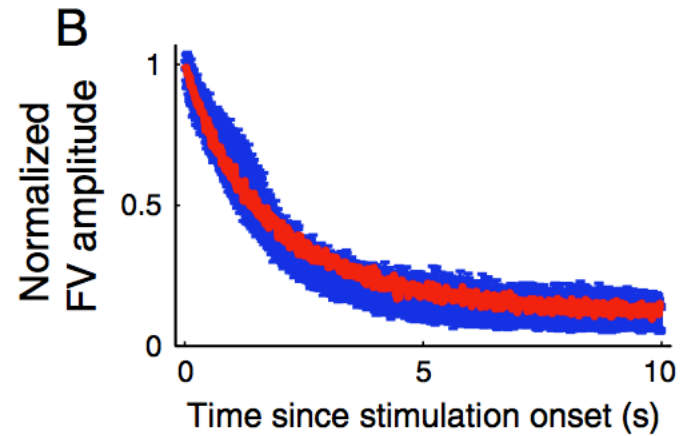
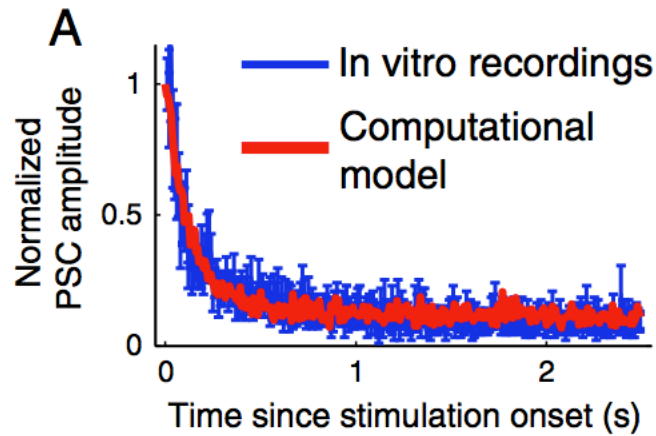


entrained

**(3)**



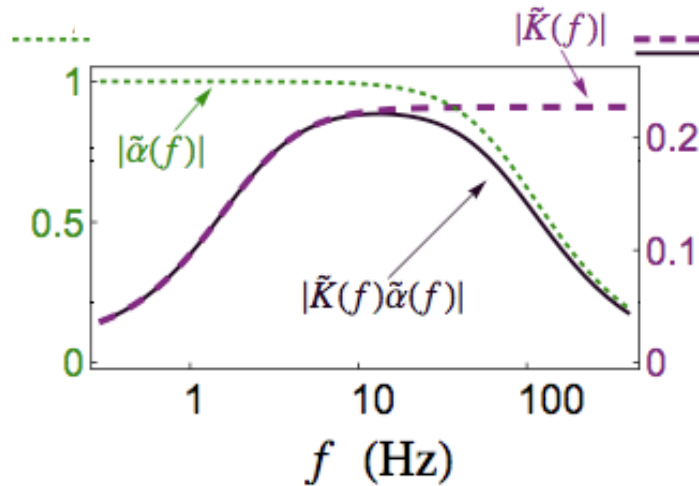
# DBS also induces axonal failure, another form of depression





# implications of depression: deterministic & stochastic

(a) band-pass synaptic filter yields peaked cross-spectrum of input/conductance

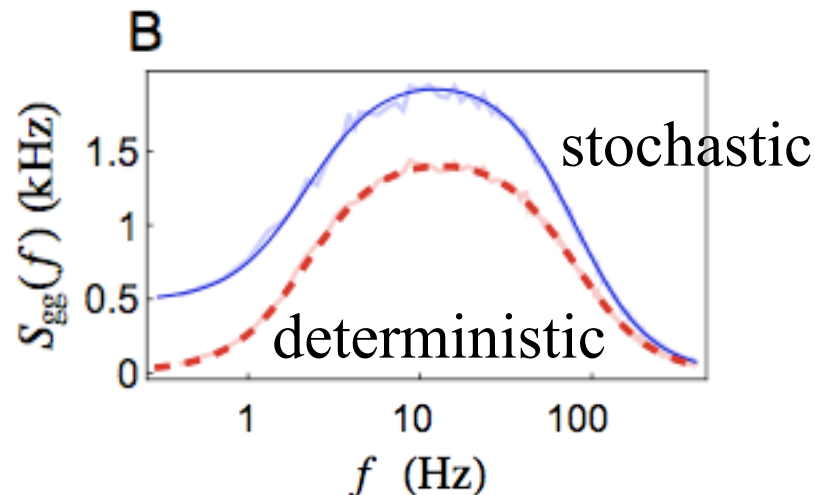


$$R_{I_g}(\tau) = \text{cov}(I(t), g(t + \tau))$$

$$S_{I_g}(f) = \int_{-\infty}^{\infty} R_{I_g}(\tau) e^{-2\pi I f \tau} d\tau$$

$$= \tilde{\alpha}(f) \tilde{K}(f) \nu$$

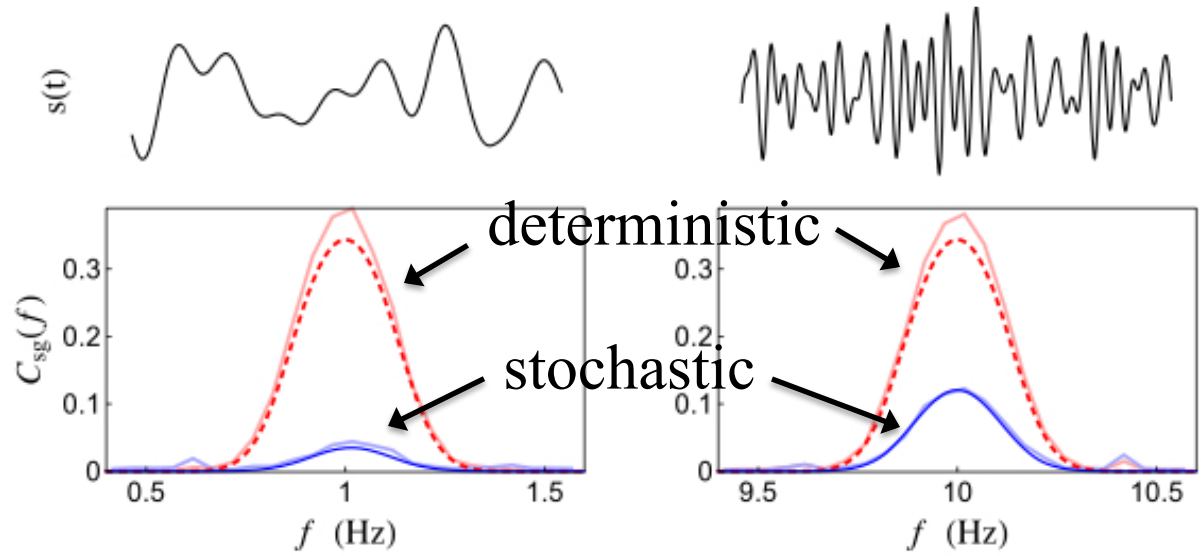
(b) at population level, power spectrum of total conductance is peaked



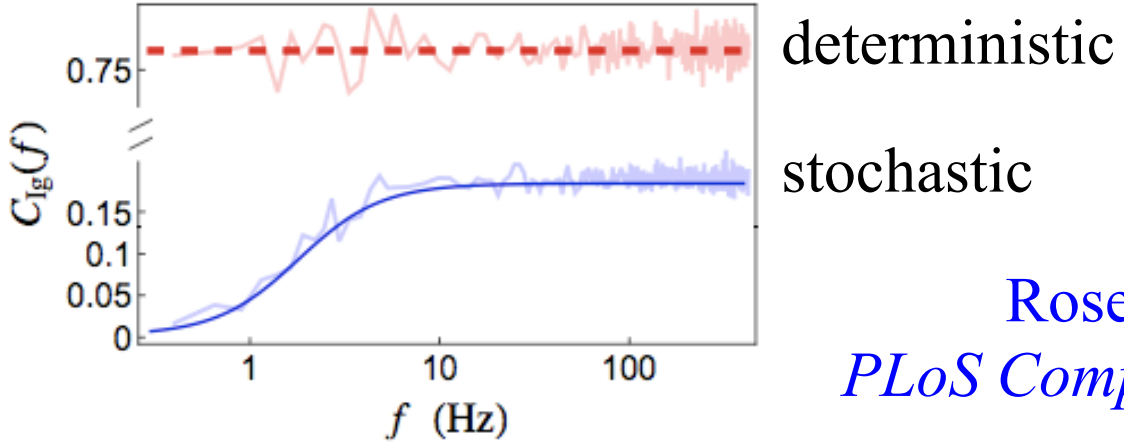
Rosenbaum et al.,  
*PLoS Comp. Biol.*, 2012

# implications: stochastic

(c) transmit high frequency signal more reliably than low frequency



(d) for high rate inputs, uptake contributes relatively more to transmission → decorrelate inputs and outputs, lower coherence



Rosenbaum et al.,  
*PLoS Comp. Biol.*, 2012