



# Phase Transitions in Porous Media

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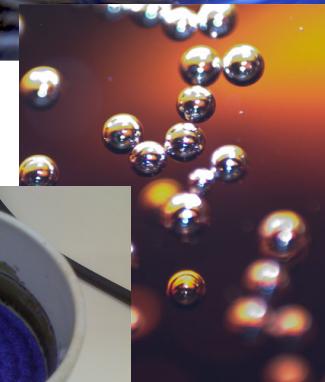


## Components

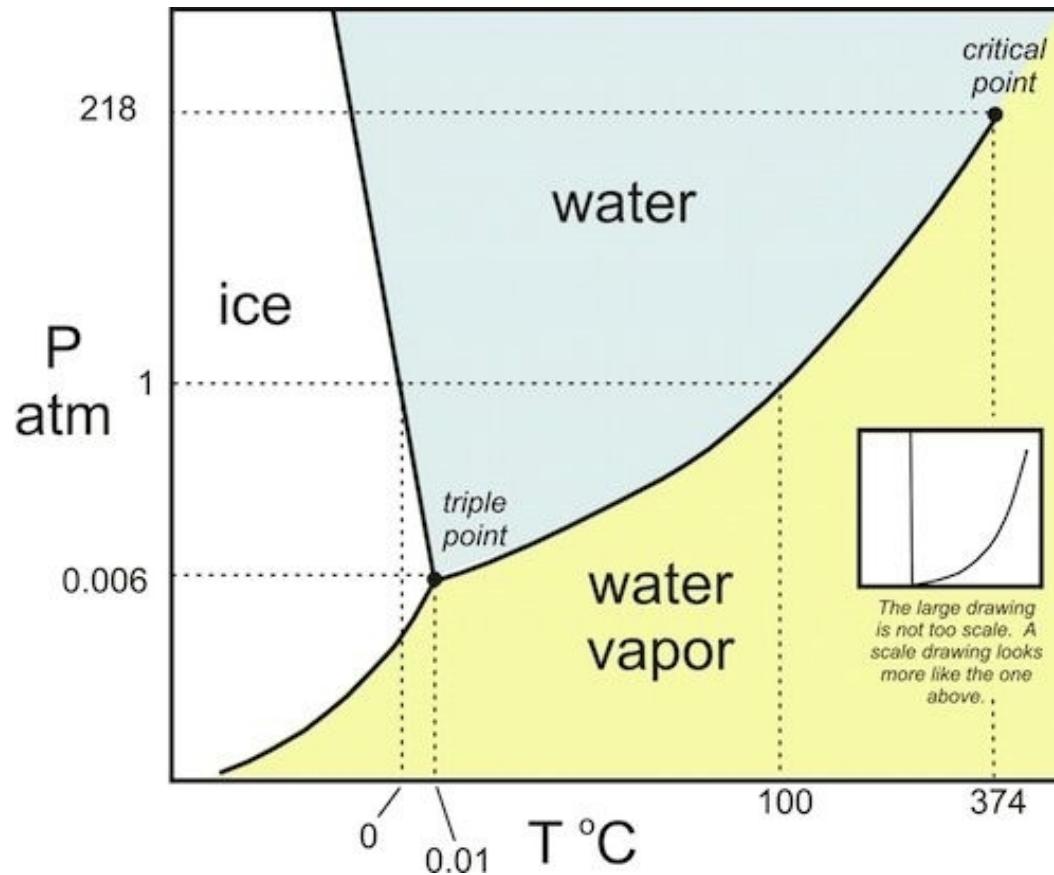
- Water
- Carbon Dioxide
- Methane
- Salt
- C7
- Nitrogen
- Oil

## Phases

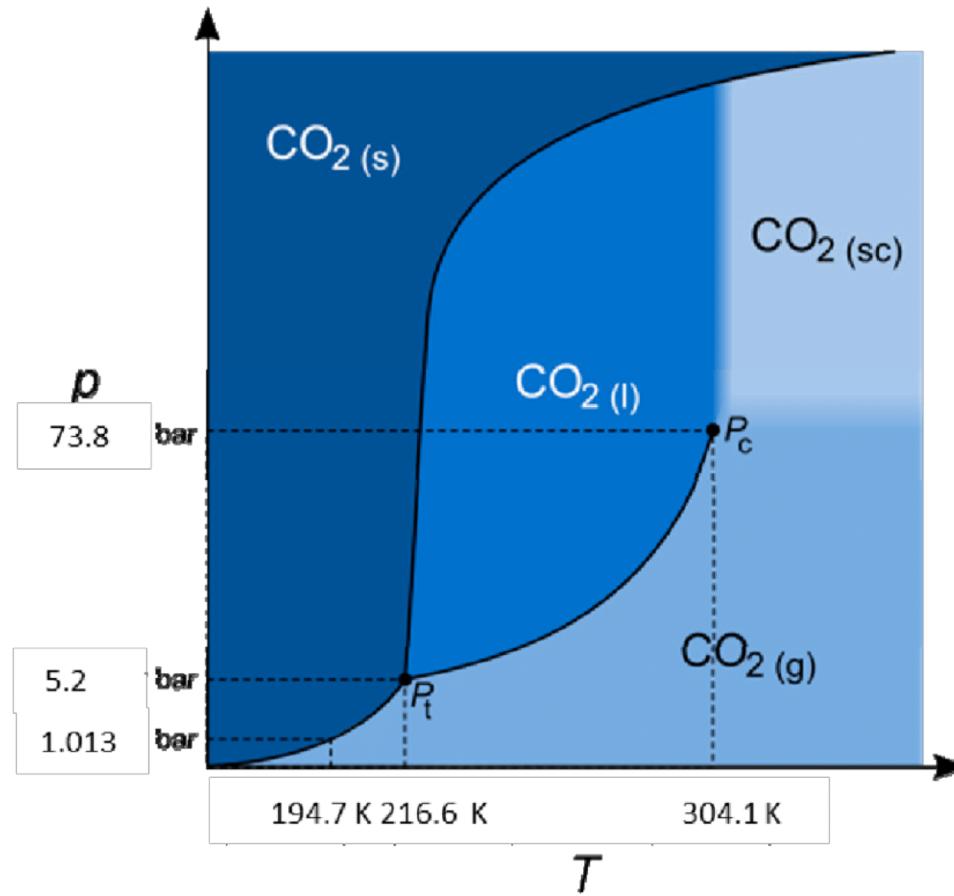
- Aqueous
- Gas
- Non-aqueous Liquid
- Hydrate
- Ice
- Precipitated Salt
- Minerals



## Pressure-Temperature Phase Diagram for Water



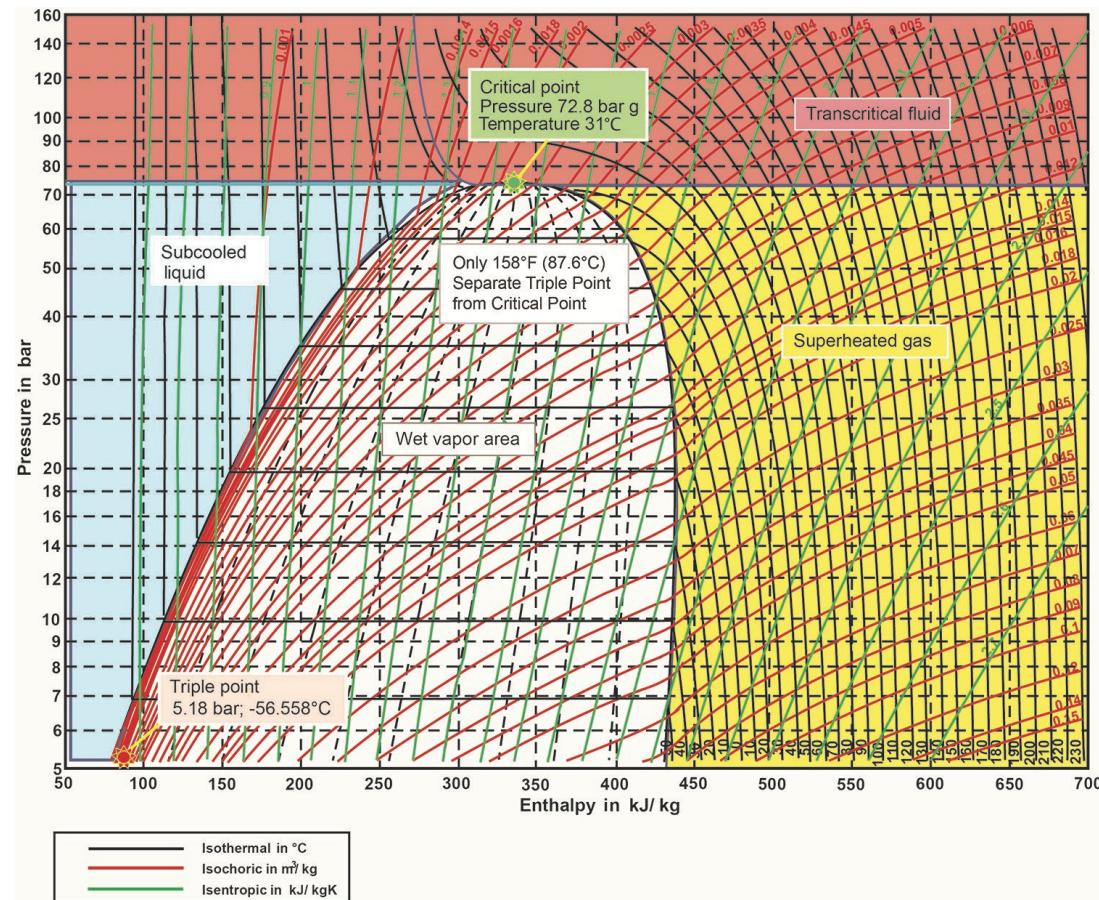
## Pressure-Temperature Phase Diagram for $\text{CO}_2$



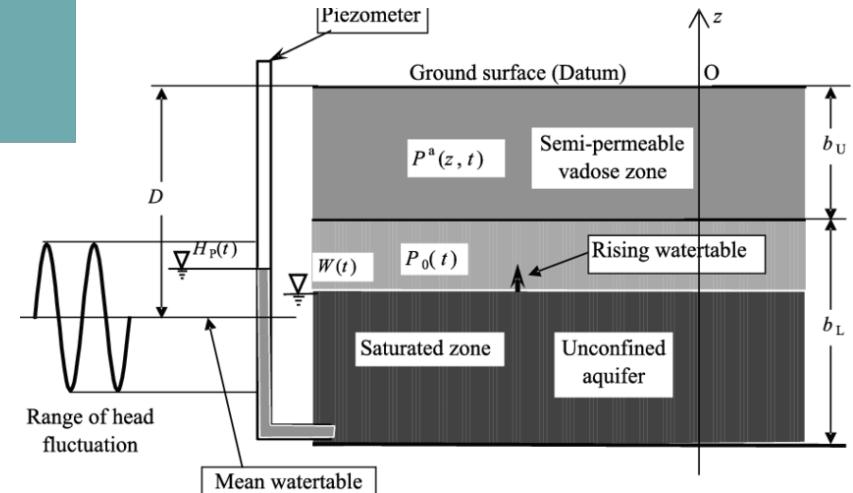
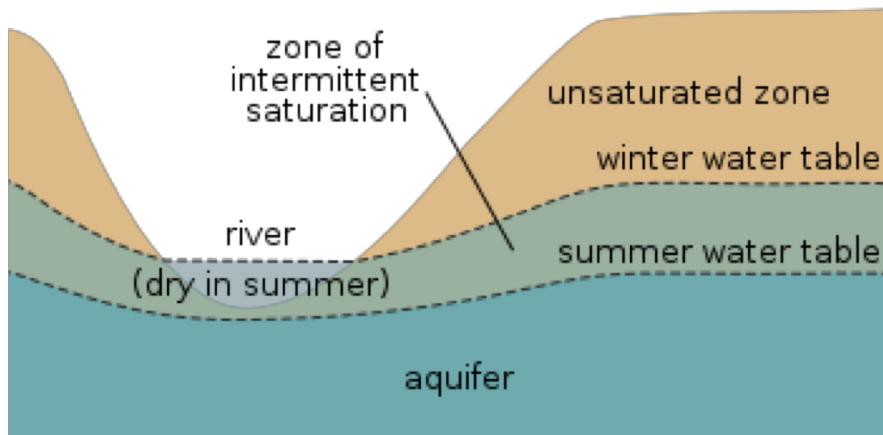


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## Pressure-Enthalpy Phase Diagram for CO<sub>2</sub>



## Phase Transitions: Fluctuating Water Table Examples





## Modeling Scheme for Saturated to Unsaturated Phase Transitions

### Fixed Variables

- Temperature (Isothermal)
- Gas Pressure (Passive Gas)

### Primary Variable Options

- Aqueous Saturation
- Aqueous Pressure

### Simple Relaxation Scheme

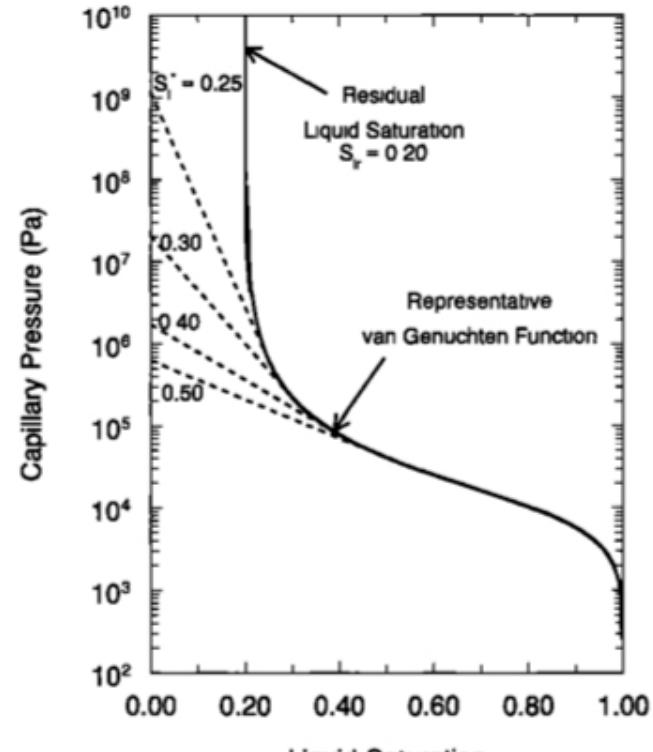
DPL – Update to Aqueous Pressure

PG(2,N) – Gas Pressure

PL(2,N) – Aqueous Pressure

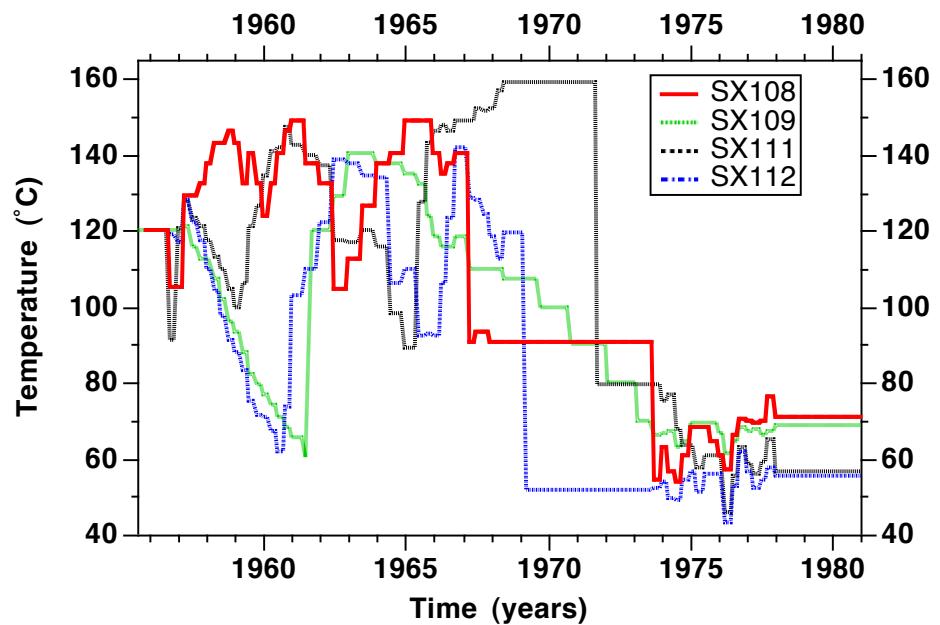
PAE – Air Entry Pressure

```
IF( PG(2,N)-PL(2,N)-PAE.GT.ZERO .AND.  
PG(2,N)-PL(2,N)-PAE-DPL.LT.ZERO ) DPL = 6.D-1*DPL  
PL(2,N) = PL(2,N) + DPL
```





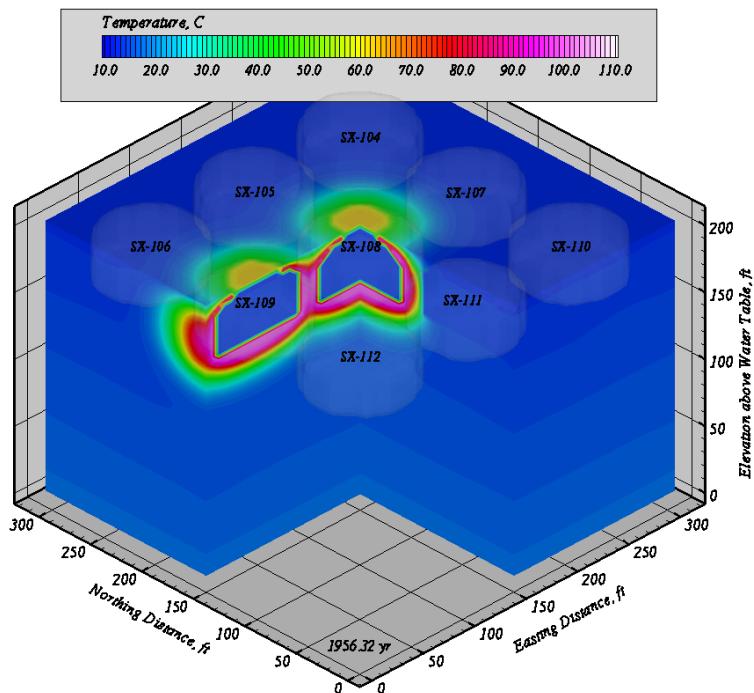
## Low-Pressure Air-Water Systems: Example of Coupled Thermal and Hydraulic Environments



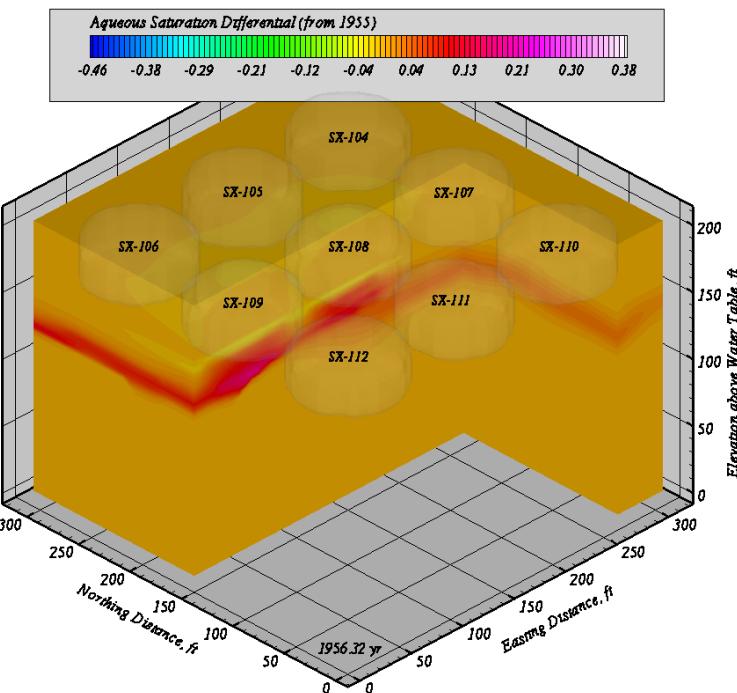


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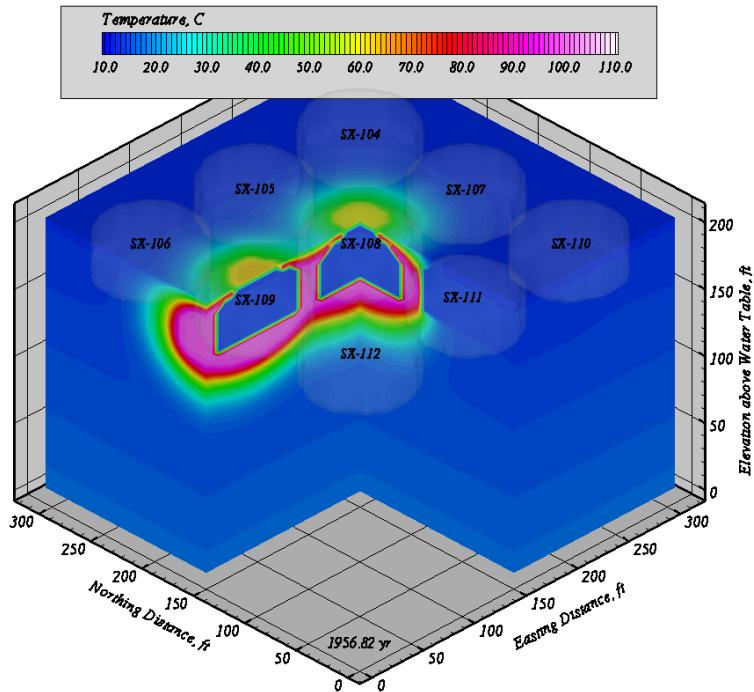


1956.32

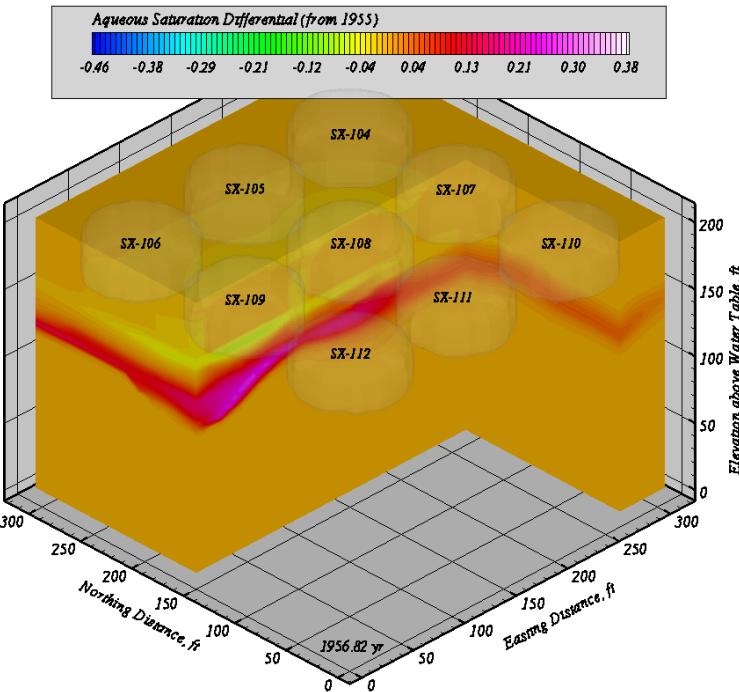




## Low-Pressure Air-Water Systems: Example of Coupled Thermal and Hydraulic Environments



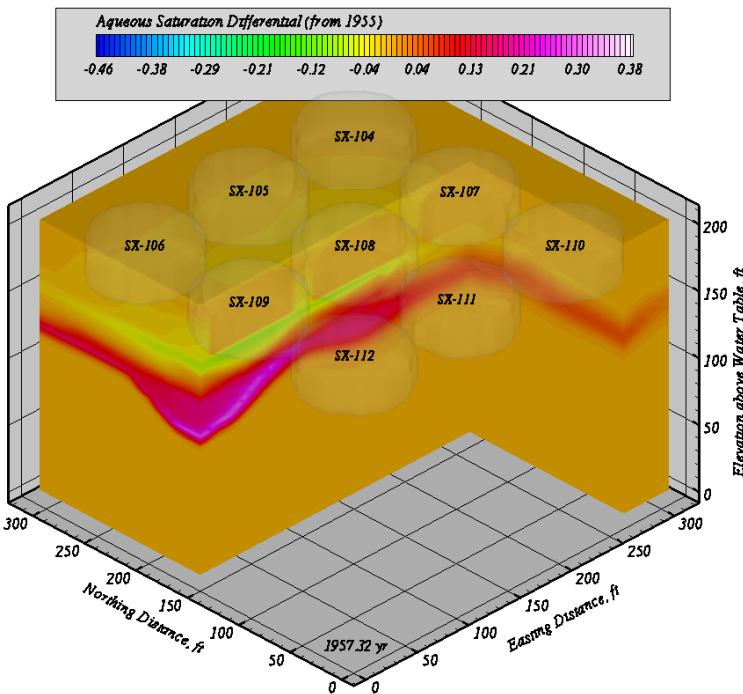
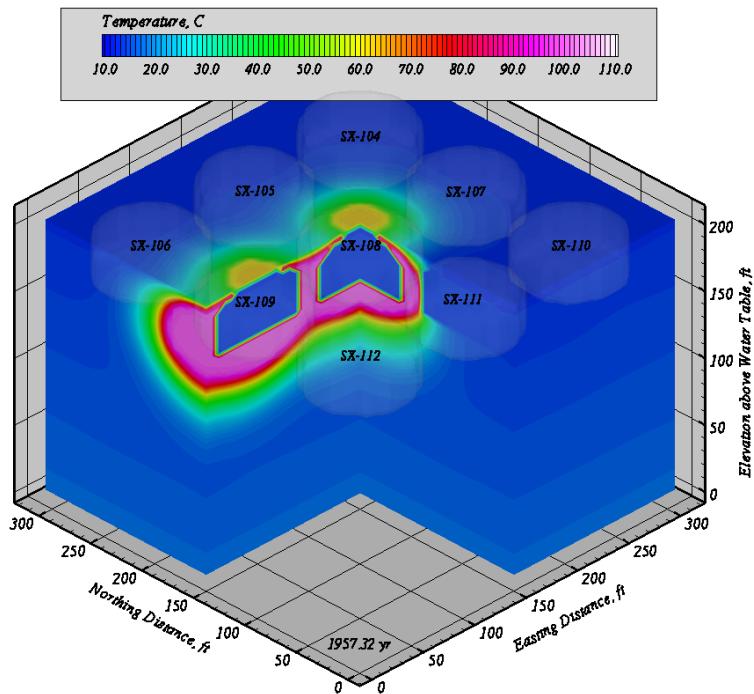
1956.82





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## Low-Pressure Air-Water Systems: Example of Coupled Thermal and Hydraulic Environments



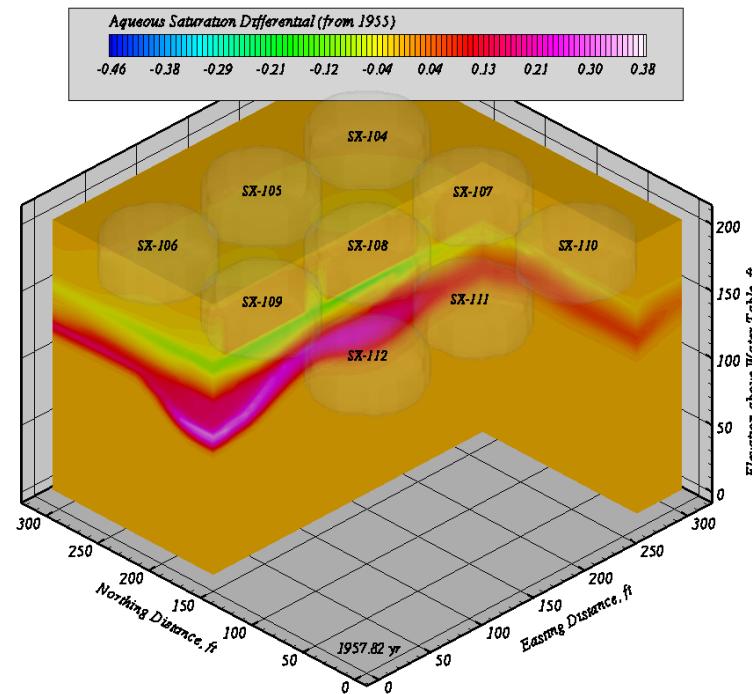
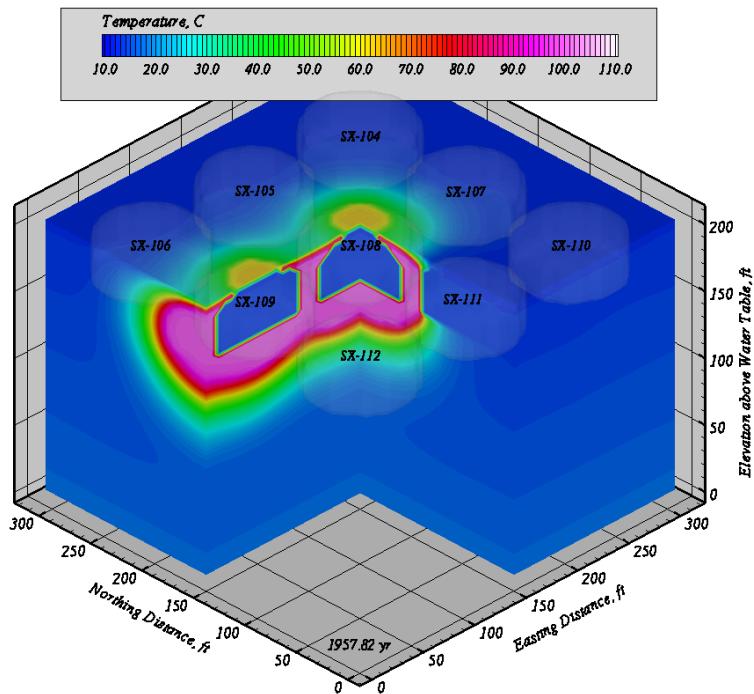
1957.32





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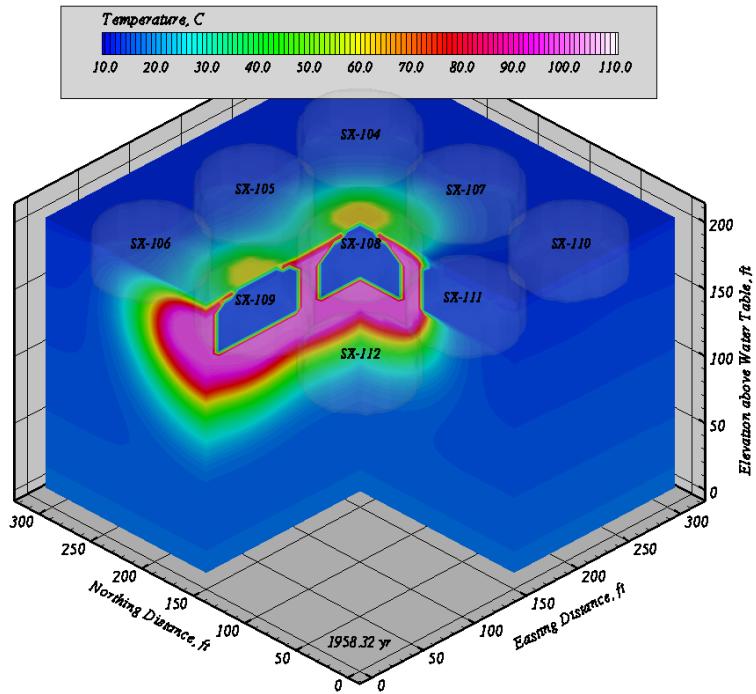


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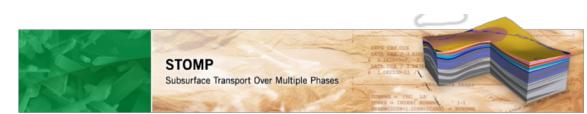
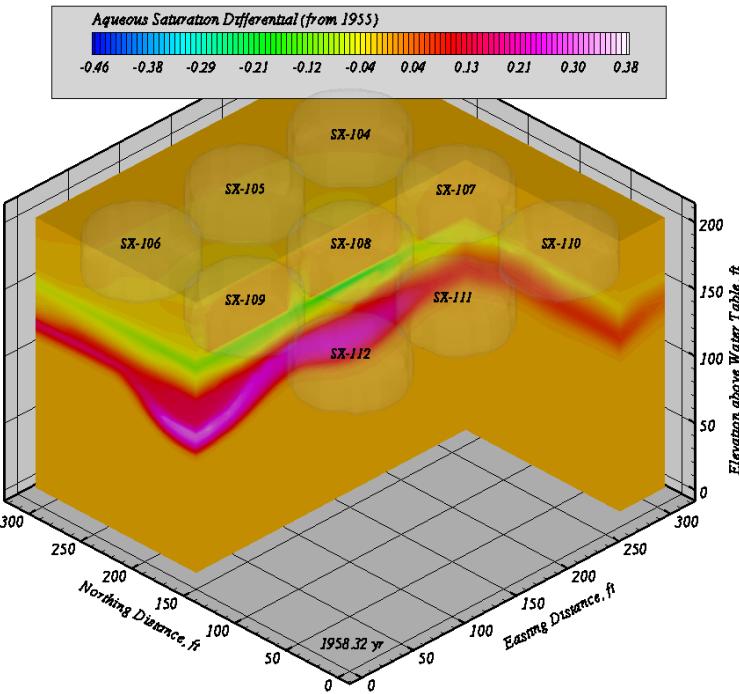




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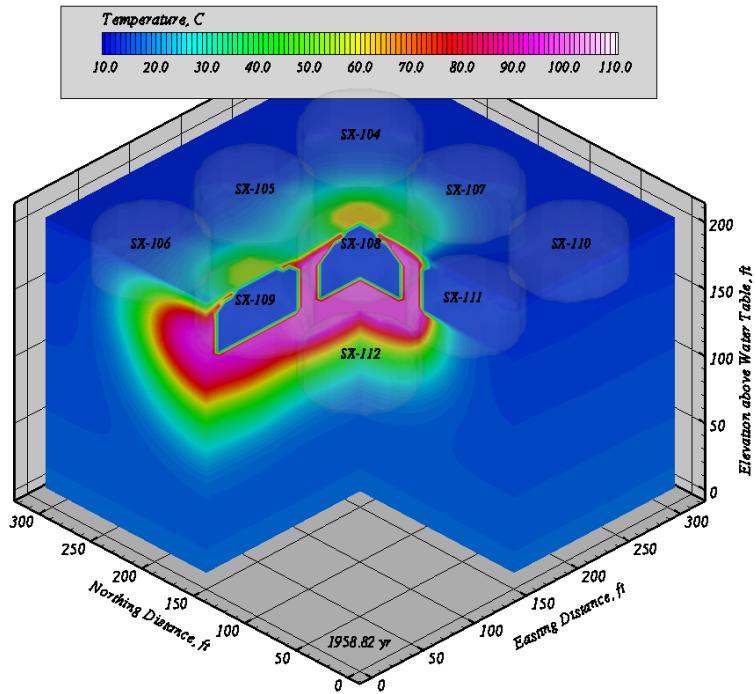


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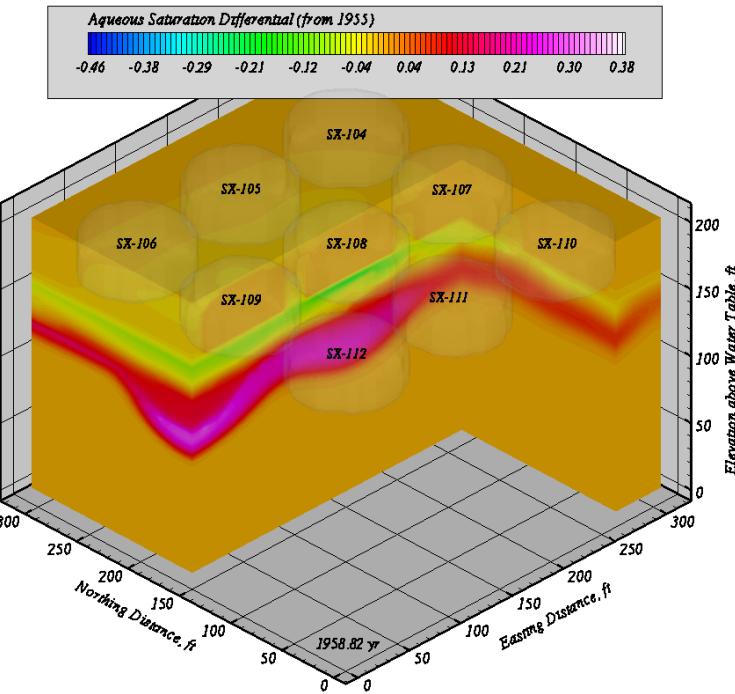




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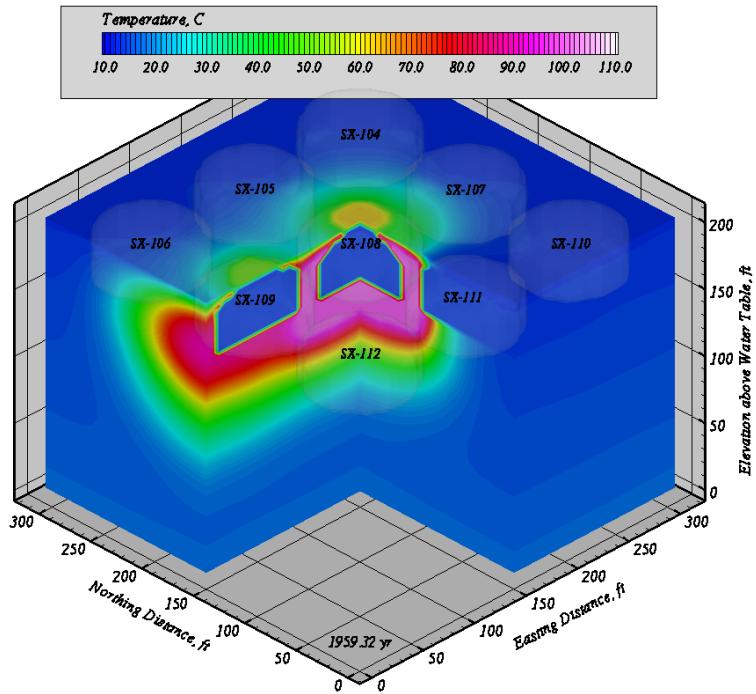


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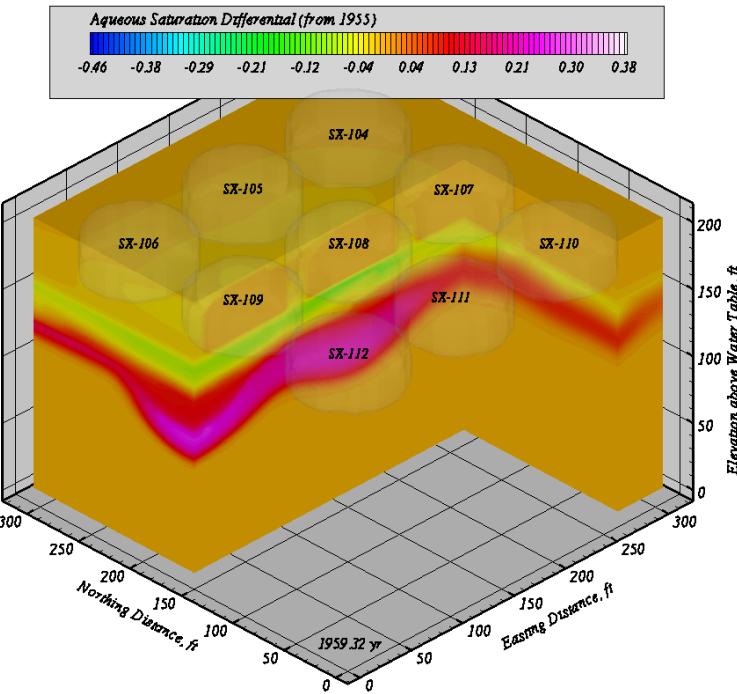




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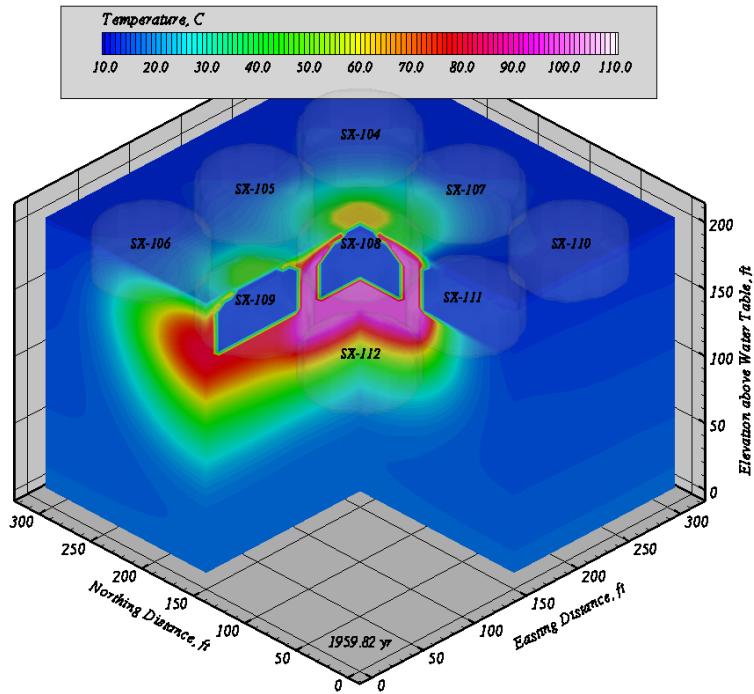


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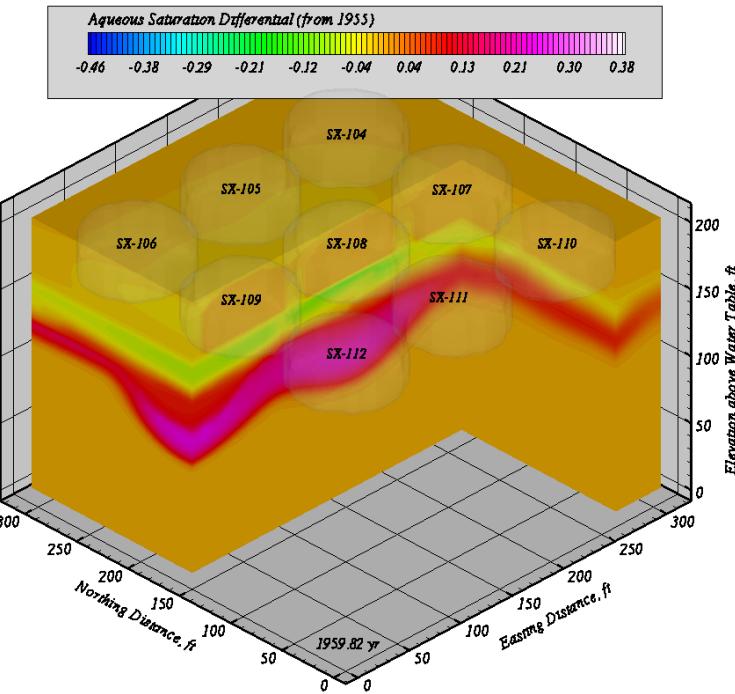




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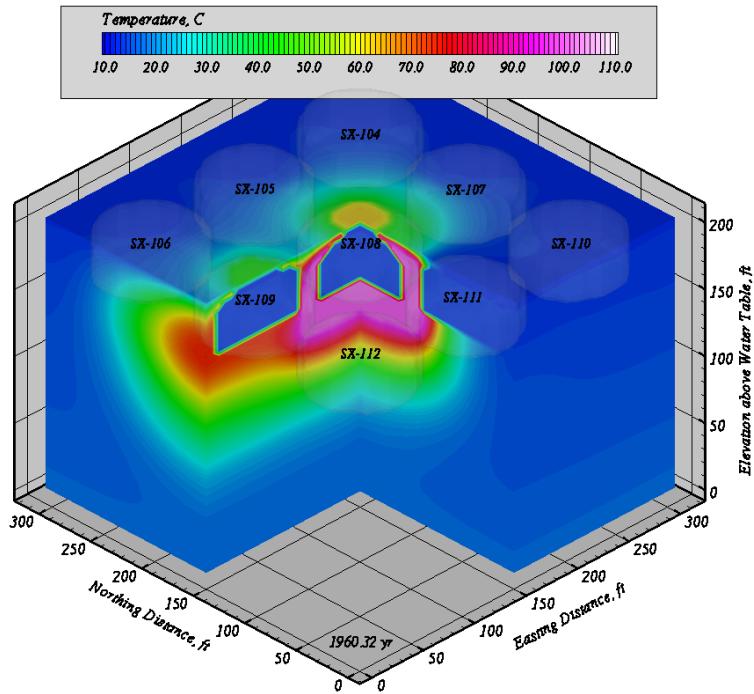


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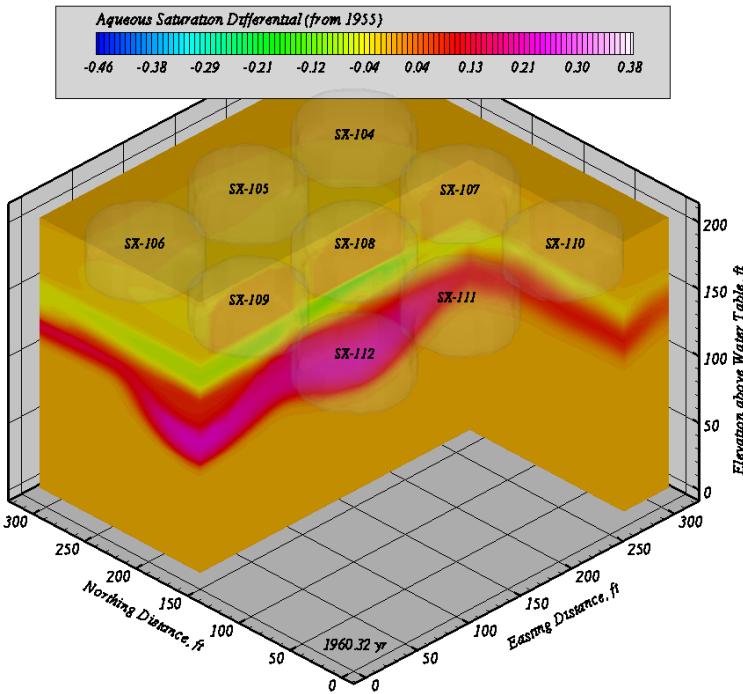




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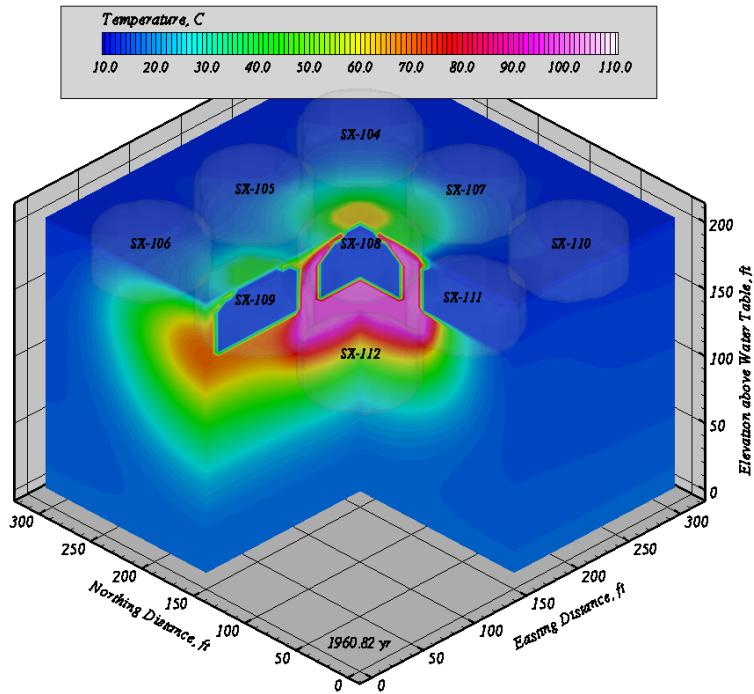


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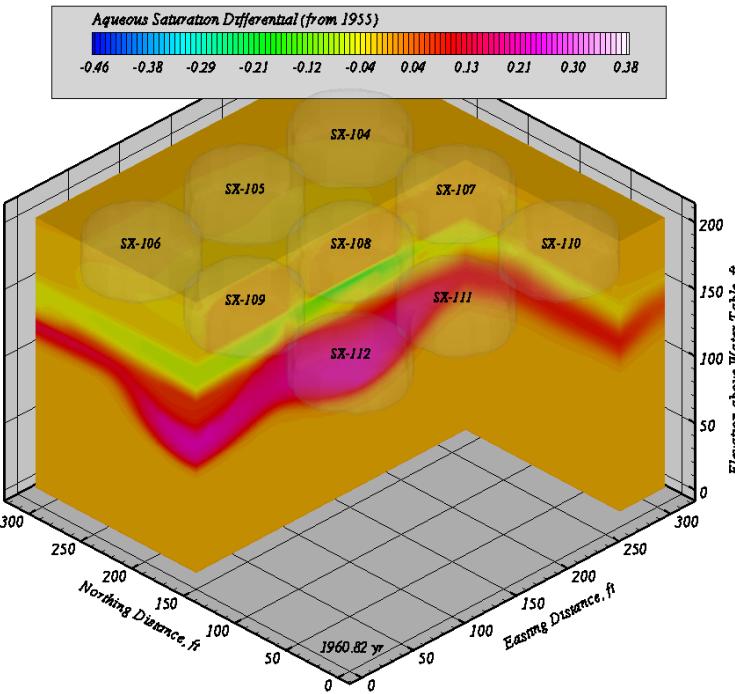




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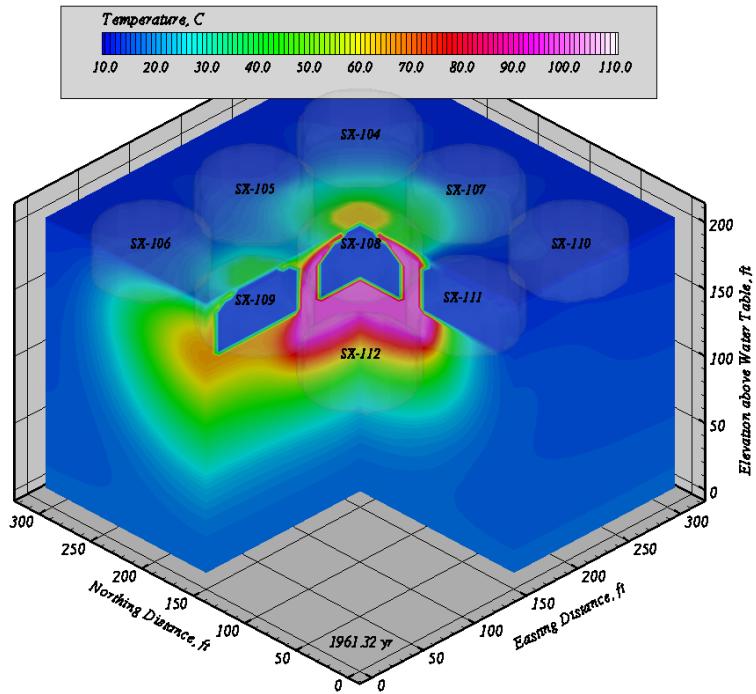


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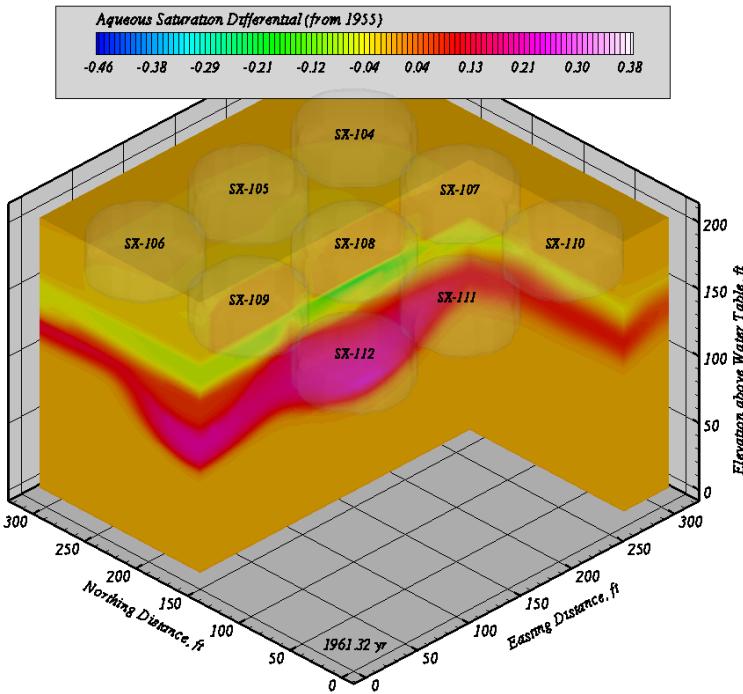




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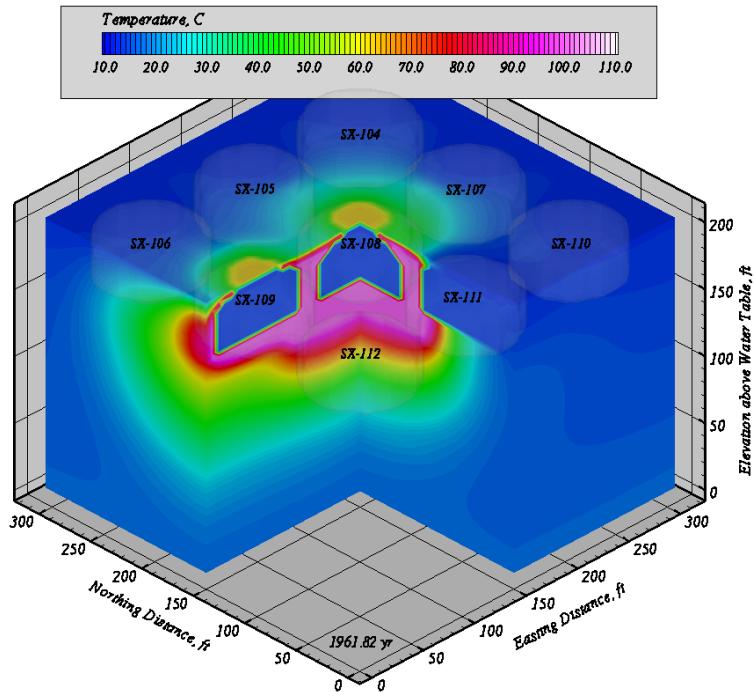


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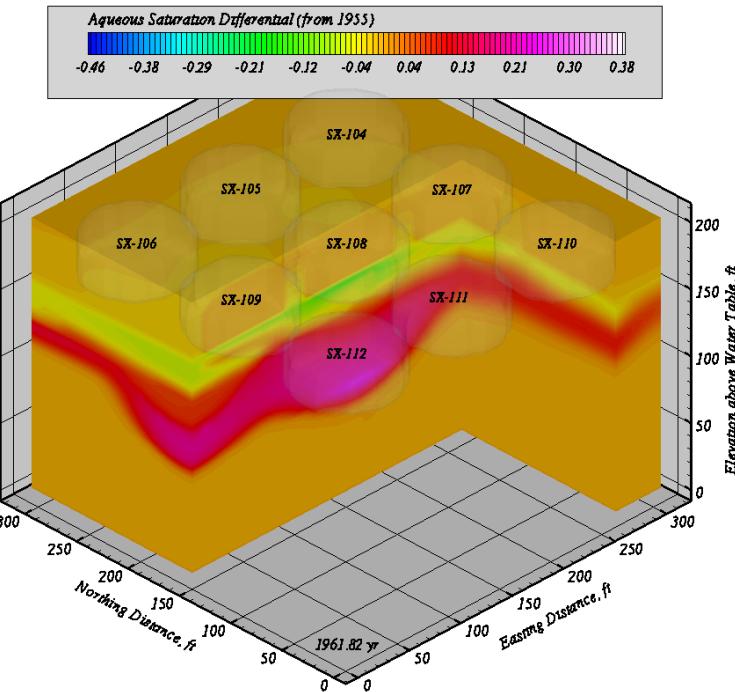




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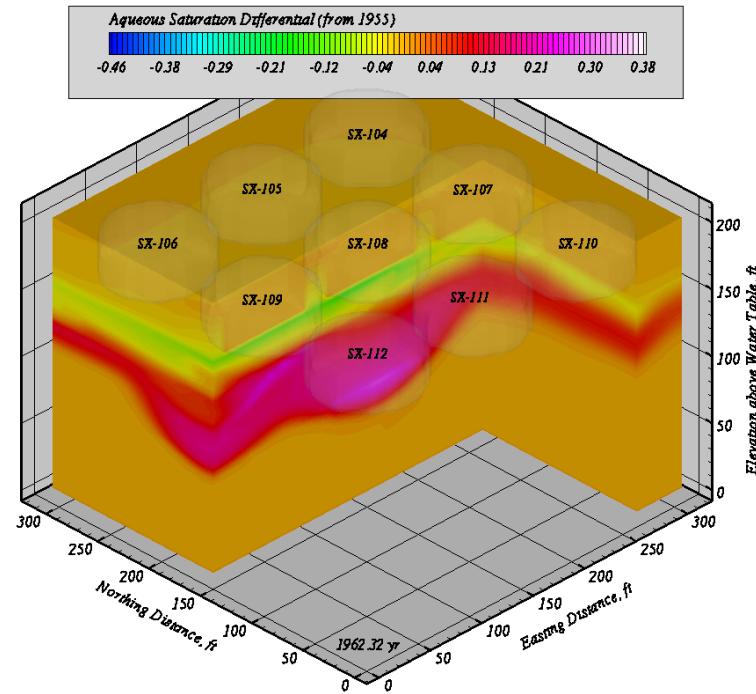
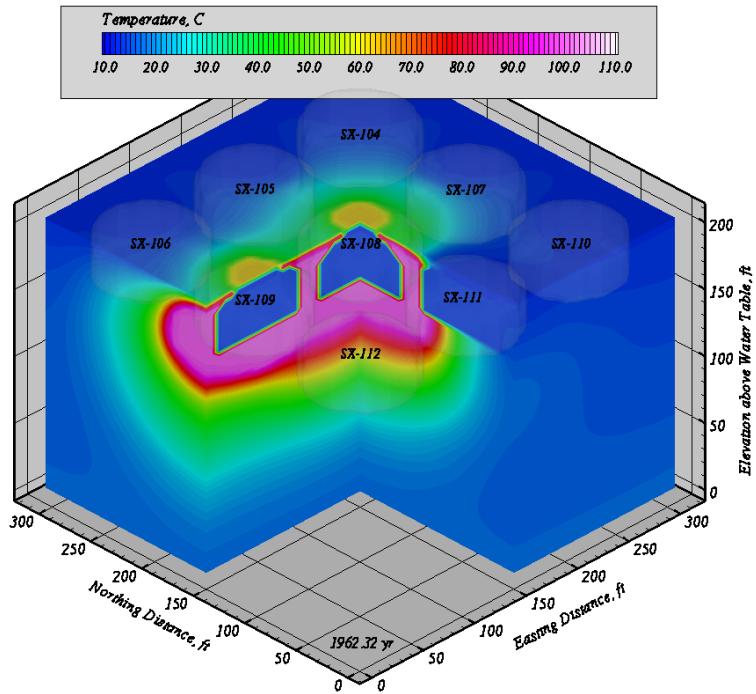


1961.82





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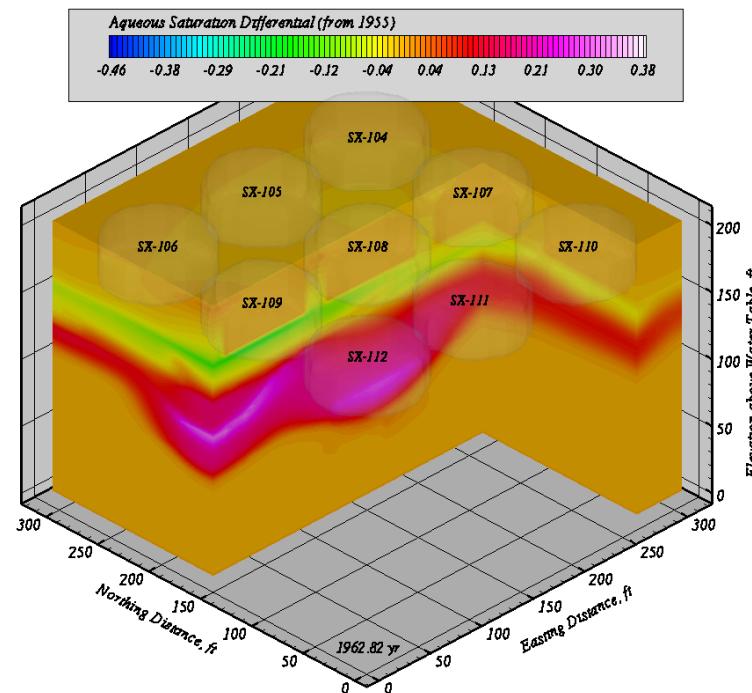
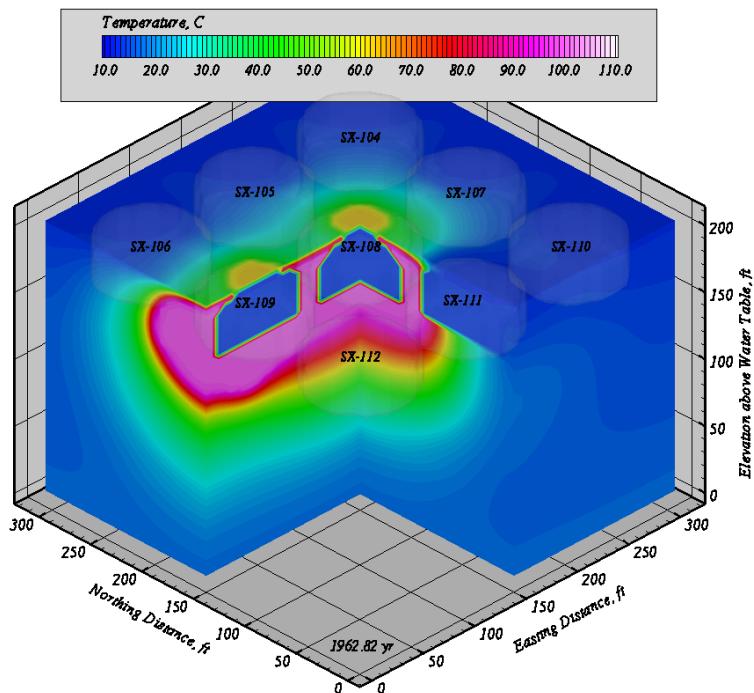
1962.32





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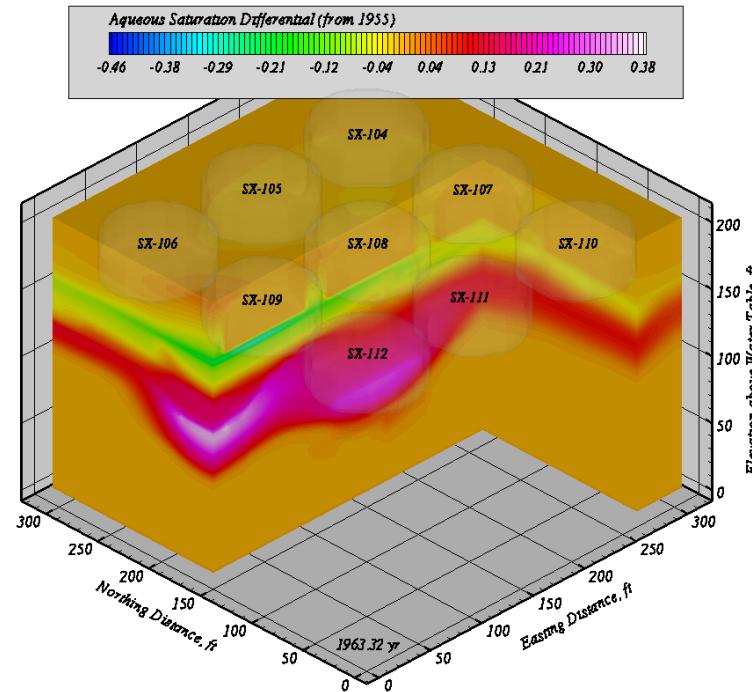
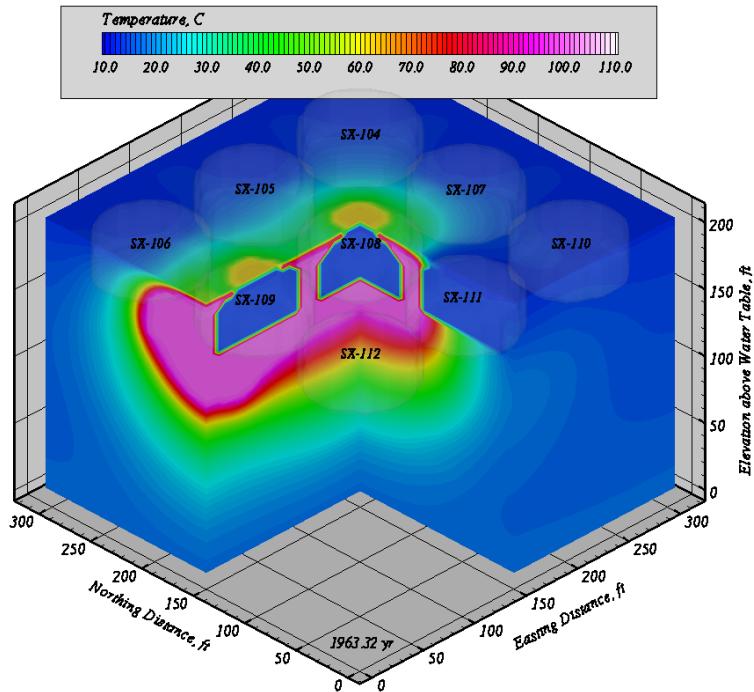
1962.82





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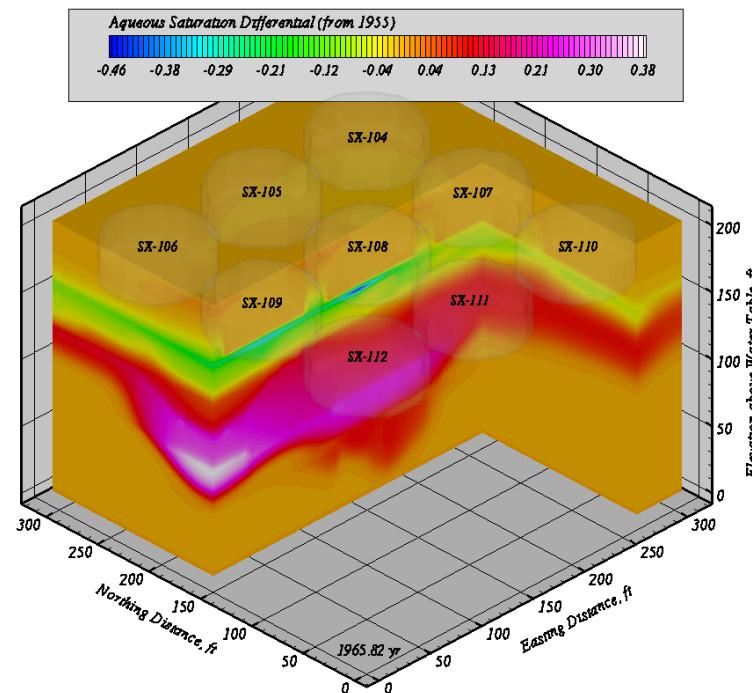
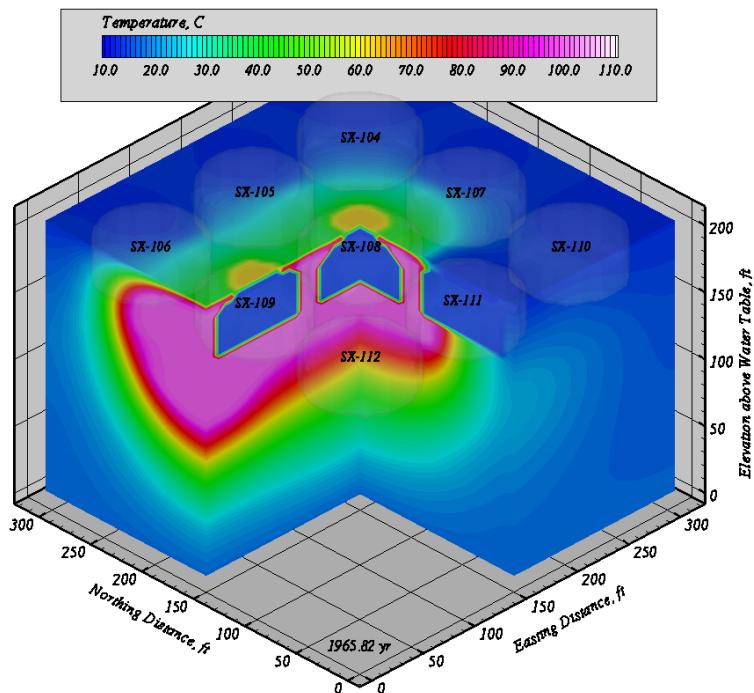
1963.32





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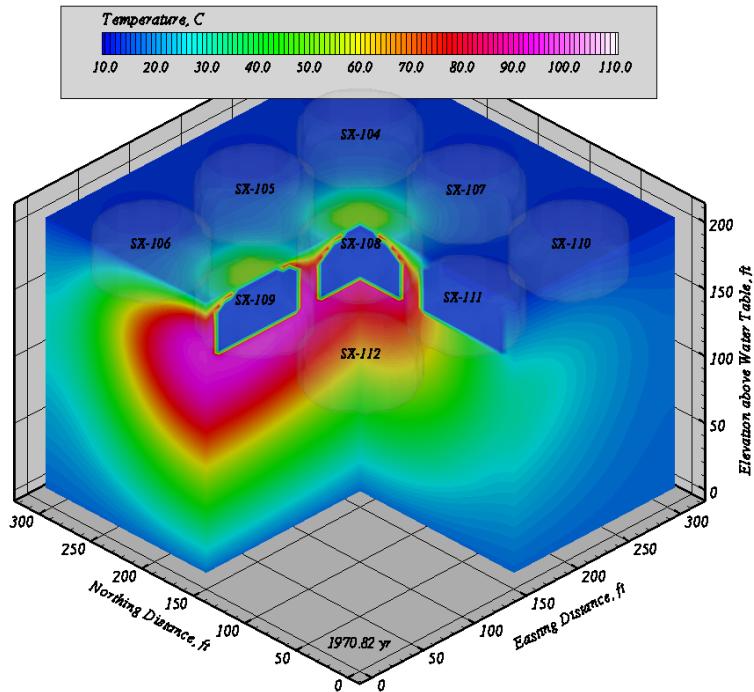


1965.82

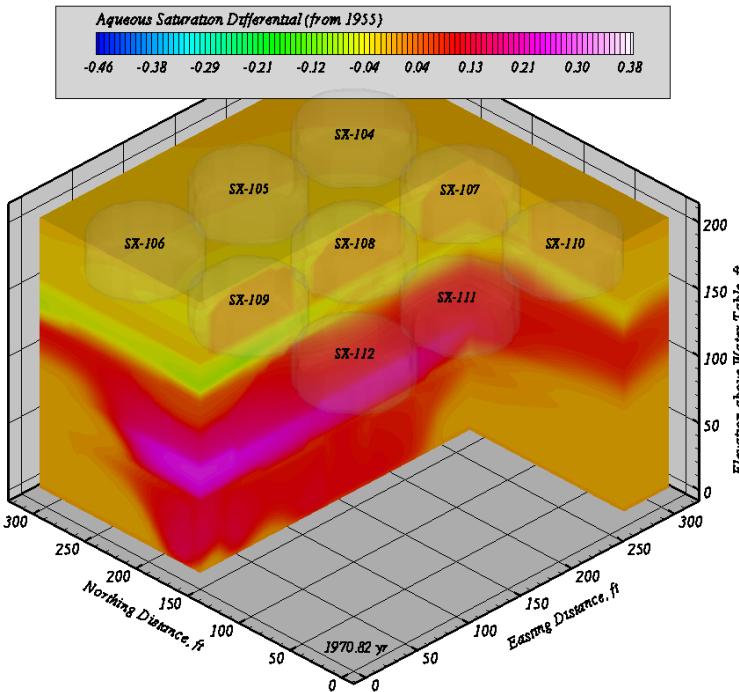




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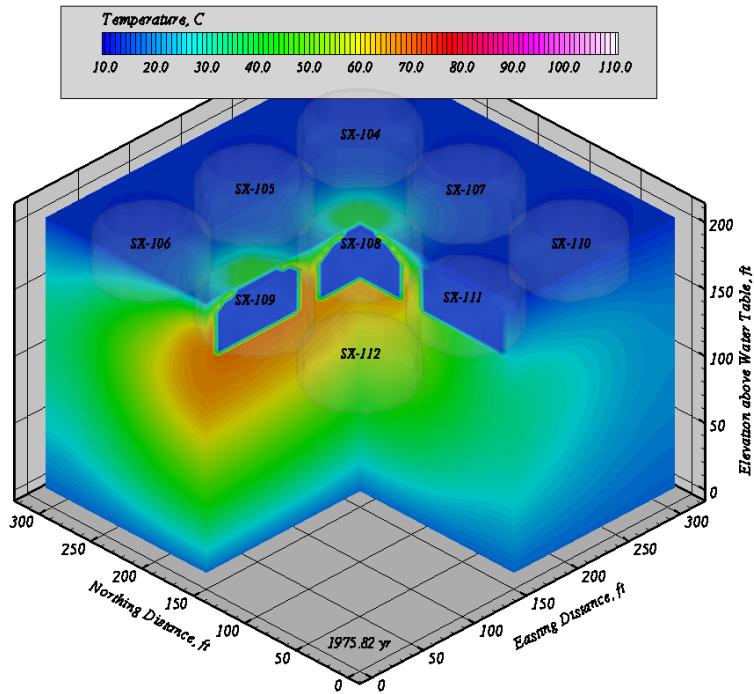


1970.82

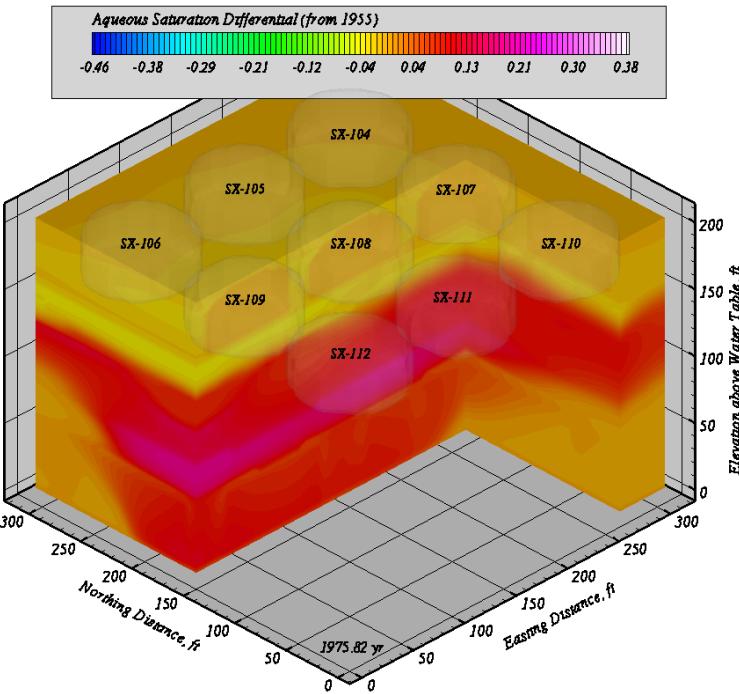




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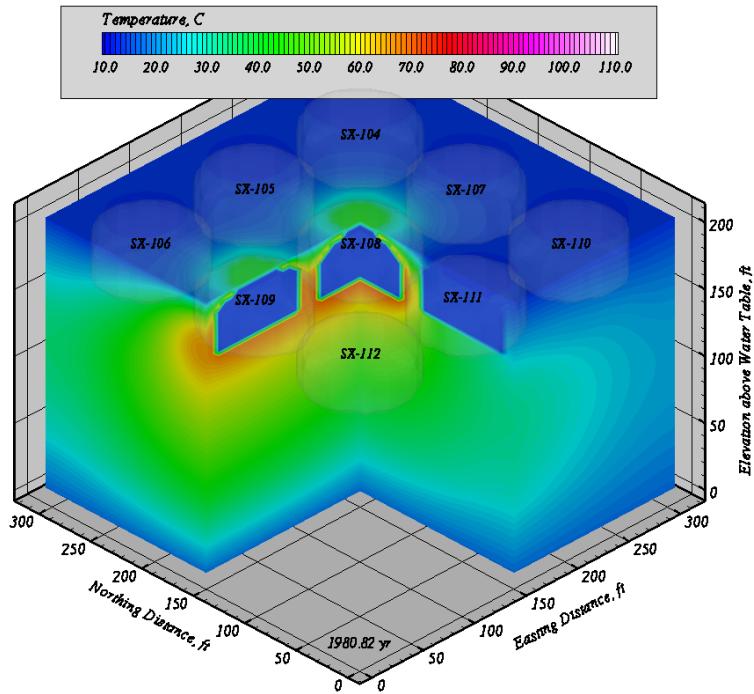


1975.82

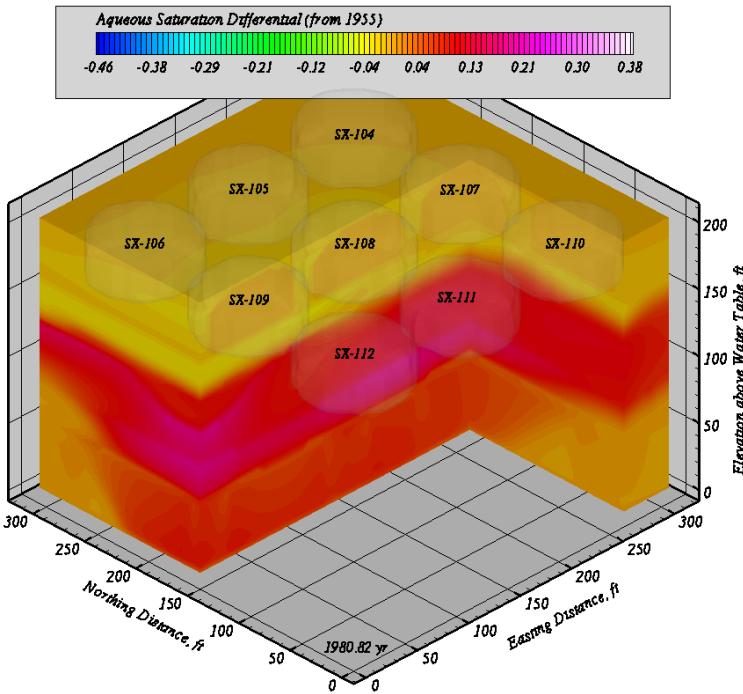




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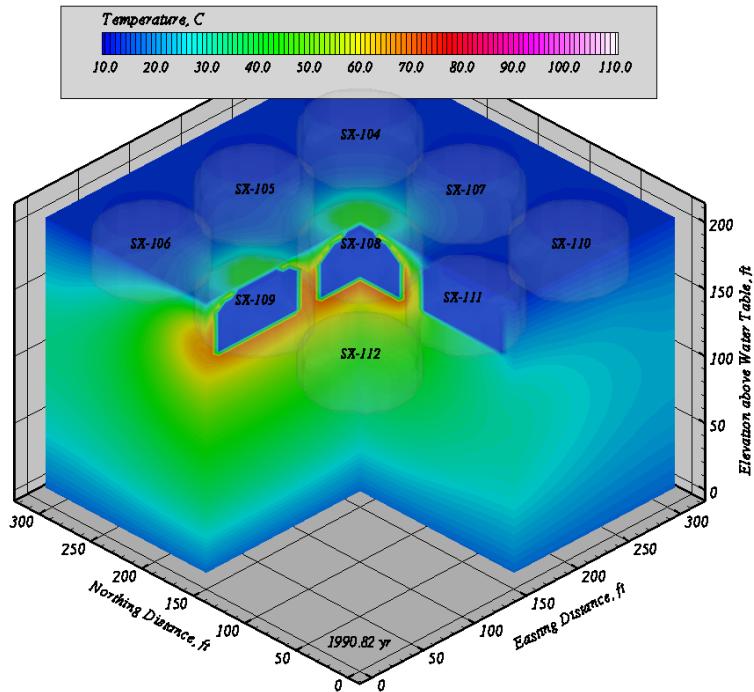


1980.82

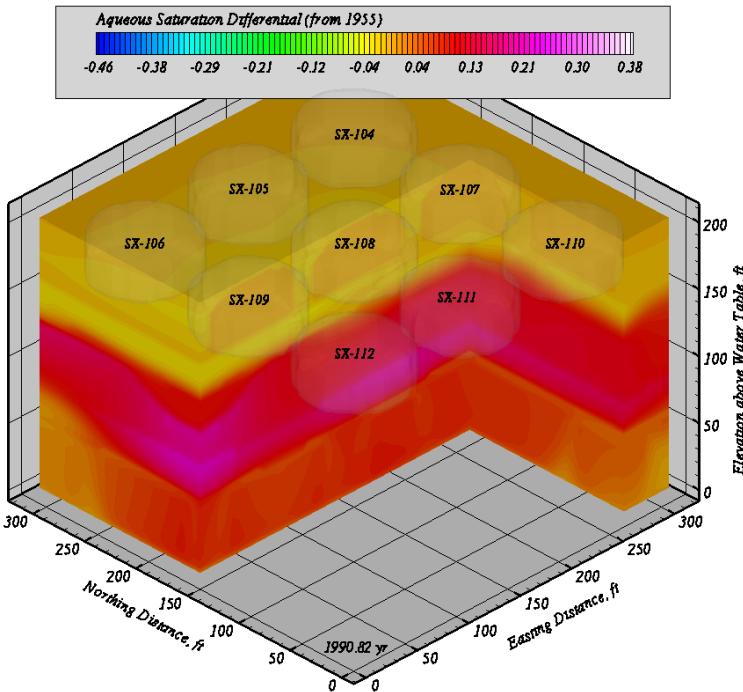




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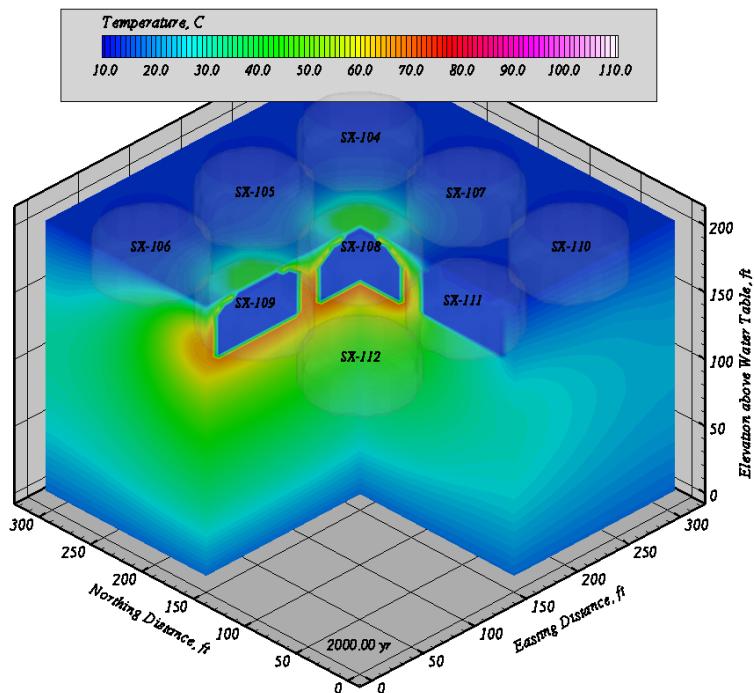
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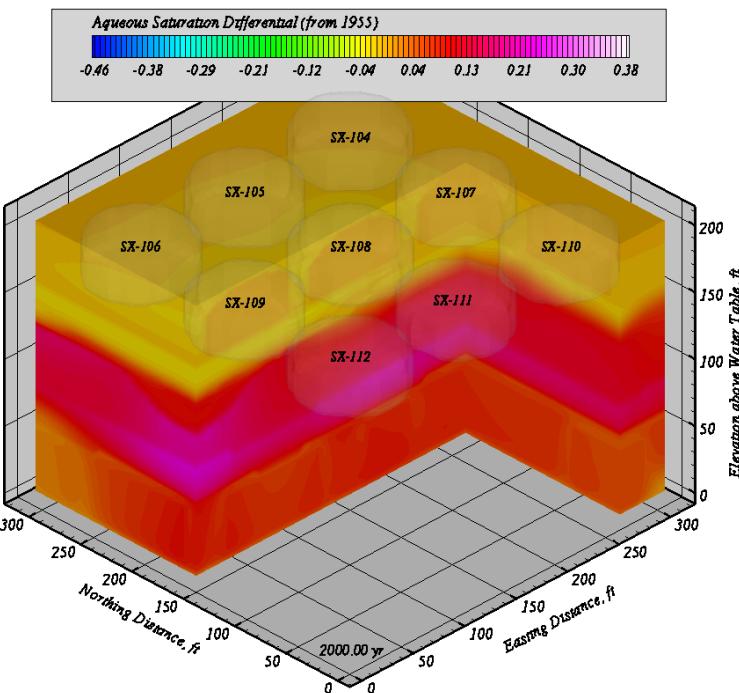


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## Low-Pressure Air-Water Systems: Example of Coupled Thermal and Hydraulic Environments



2000.00





# Low-Pressure Air-Water Systems: Phase Conditions and Transitions



## Phase Conditions

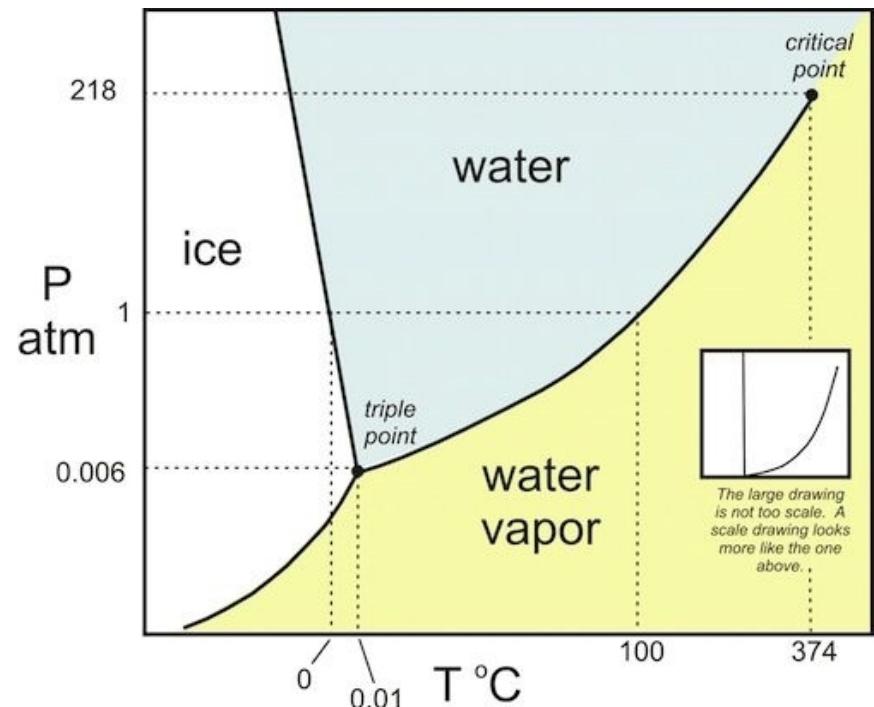
1. Saturated without Trapped Gas
  - Energy – Temperature
  - Water Mass – Aqueous Pressure
  - Air Mass – Aqueous Air Mole Fraction
  - Salt Mass – Total Brine Mass Fraction
2. Partially Saturated
  - Energy – Temperature
  - Water Mass – Aqueous Pressure
  - Air Mass – Gas Pressure
  - Salt Mass – Total Brine Mass Fraction
3. Saturated with Trapped Gas
  - Energy – Temperature
  - Water Mass – Aqueous Pressure
  - Air Mass – Trapped Gas Saturation
  - Salt Mass – Total Brine Mass Fraction
4. Fully Unsaturated
  - Energy – Temperature
  - Water Mass – Water Vapor Partial Pressure
  - Air Mass – Gas Pressure
  - Salt Mass – Salt Mass

# Low-Pressure Water Systems: Phase Conditions and Transitions



## Phase Conditions

1. Saturated without Trapped Gas
  - Energy – Temperature
  - Water Mass – Aqueous Pressure
  - Salt Mass – Total Brine Mass Fraction
2. Partially Saturated
  - Energy – Temperature
  - Water Mass – Beta Factor
  - Salt Mass – Total Brine Mass Fraction
3. Saturated with Trapped Gas
  - Energy – Temperature
  - Water Mass – Trapped Gas Saturation
  - Salt Mass – Total Brine Mass Fraction
4. Fully Unsaturated
  - Energy – Temperature
  - Water Mass – Water Vapor Partial Pressure
  - Salt Mass – Salt Mass





# Low-Pressure Air-Water Systems: Phase Conditions and Transitions

## Phase Conditions

1. Saturated without Trapped Gas
  - Energy – Temperature
  - Water Mass – Aqueous Pressure
  - Air Mass – Aqueous Air Mole Fraction
  - Salt Mass – Total Brine Mass Fraction
2. Partially Saturated
  - Energy – Temperature
  - Water Mass – Aqueous Pressure
  - Air Mass – Gas Pressure
  - Salt Mass – Total Brine Mass Fraction
3. Saturated with Trapped Gas
  - Energy – Temperature
  - Water Mass – Aqueous Pressure
  - Air Mass – Trapped Gas Saturation
  - Salt Mass – Total Brine Mass Fraction
4. Fully Unsaturated
  - Energy – Temperature
  - Water Mass – Water Vapor Partial Pressure
  - Air Mass – Gas Pressure
  - Salt Mass – Salt Mass



PGA – air partial pressure  
PGW – water partial pressure  
PG – gas pressure  
PL – aqueous pressure  
SG – gas saturation  
SL – aqueous saturation

PGA = FUNC( XMLA )  
PGW = FUNC( T,PCAP )  
PG = PGW + PGA  
PCAP = PG – PL  
SL = FUNC( PCAP )  
SG = 1.D+0 – SL  
IF( SG > 1.D-3 ) NPHAZ = 2



# Low-Pressure Air-Water Systems: Phase Conditions and Transitions

## Phase Conditions

### 1. Saturated without Trapped Gas

- Energy – Temperature
- Water Mass – Aqueous Pressure
- Air Mass – Aqueous Air Mole Fraction
- Salt Mass – Total Brine Mass Fraction

### 2. Partially Saturated

- Energy – Temperature
- Water Mass – Aqueous Pressure
- Air Mass – Gas Pressure
- Salt Mass – Total Brine Mass Fraction

### 3. Saturated with Trapped Gas

- Energy – Temperature
- Water Mass – Aqueous Pressure
- Air Mass – Trapped Gas Saturation
- Salt Mass – Total Brine Mass Fraction

### 4. Fully Unsaturated

- Energy – Temperature
- Water Mass – Water Vapor Partial Pressure
- Air Mass – Gas Pressure
- Salt Mass – Salt Mass



PG – gas pressure

PL – aqueous pressure

ASL – apparent aqueous sat.

SGT – trapped gas sat.

PCAP = PG – PL

ASL = FUNC( PCAP )

IF( ASL == 0 && SGT == 0 )

NPHAZ = 1



# Low-Pressure Air-Water Systems: Phase Conditions and Transitions



## Phase Conditions

1. Saturated without Trapped Gas
  - Energy – Temperature
  - Water Mass – Aqueous Pressure
  - Air Mass – Aqueous Air Mole Fraction
  - Salt Mass – Total Brine Mass Fraction
2. Partially Saturated
  - Energy – Temperature
  - Water Mass – Aqueous Pressure
  - Air Mass – Gas Pressure
  - Salt Mass – Total Brine Mass Fraction
3. Saturated with Trapped Gas
  - Energy – Temperature
  - Water Mass – Aqueous Pressure
  - Air Mass – Trapped Gas Saturation
  - Salt Mass – Total Brine Mass Fraction
4. Fully Unsaturated
  - Energy – Temperature
  - Water Mass – Water Vapor Partial Pressure
  - Air Mass – Gas Pressure
  - Salt Mass – Salt Mass



PG – gas pressure

PL – aqueous pressure

ASL – apparent aqueous sat.

SGT – trapped gas sat.

PCAP = PG – PL

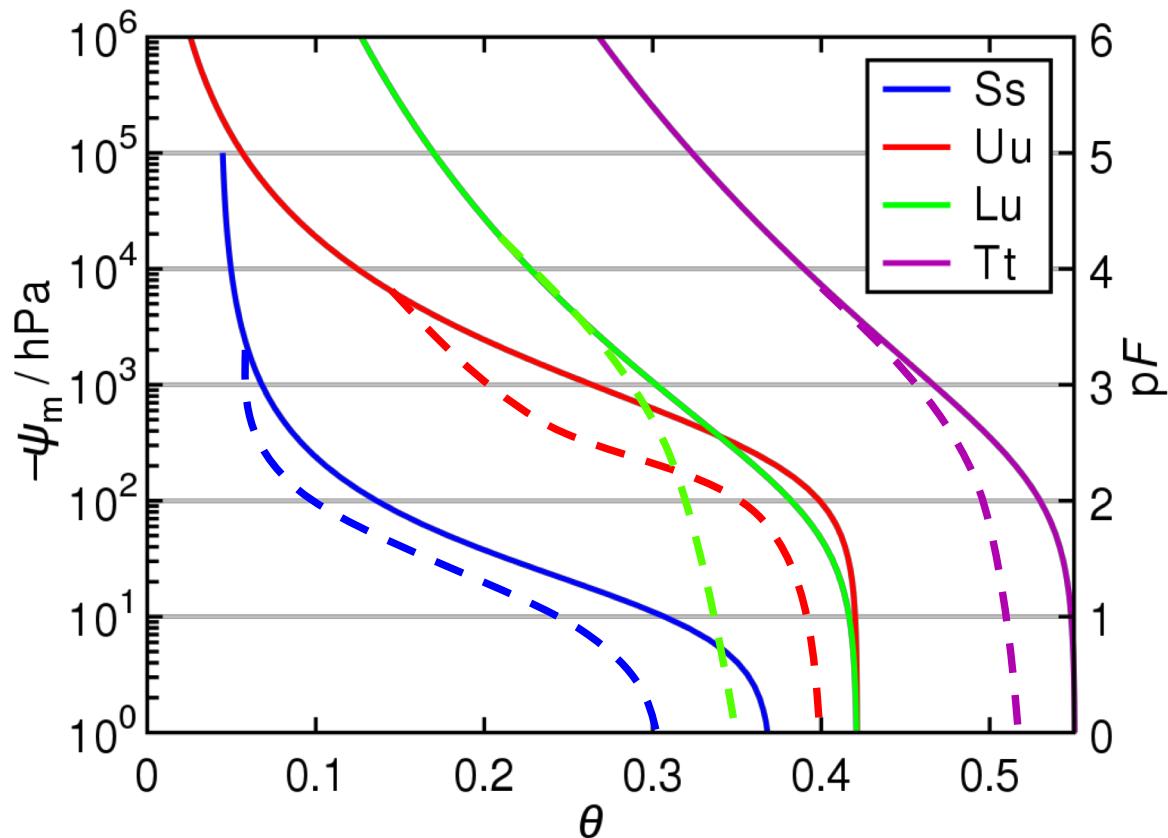
ASL = FUNC( PCAP )

IF( ASL == 0 && SGT > 0 )

NPHAZ = 3



## Low-Pressure Air-Water Systems: Phase Conditions and Transitions



Ss – sand  
Uu – silt or clay loam  
LU – loam-silt or clay  
Tt – clay or peat



# Low-Pressure Air-Water Systems: Phase Conditions and Transitions



## Phase Conditions

1. Saturated without Trapped Gas
  - Energy – Temperature
  - Water Mass – Aqueous Pressure
  - Air Mass – Aqueous Air Mole Fraction
  - Salt Mass – Total Brine Mass Fraction
2. Partially Saturated
  - Energy – Temperature
  - Water Mass – Aqueous Pressure
  - Air Mass – Gas Pressure
  - Salt Mass – Total Brine Mass Fraction
3. Saturated with Trapped Gas
  - Energy – Temperature
  - Water Mass – Aqueous Pressure
  - Air Mass – Trapped Gas Saturation
  - Salt Mass – Total Brine Mass Fraction
4. Fully Unsaturated
  - Energy – Temperature
  - Water Mass – Water Vapor Partial Pressure
  - Air Mass – Gas Pressure
  - Salt Mass – Salt Mass



PG – gas pressure

PL – aqueous pressure

ASL – apparent aqueous sat.

SL – aqueous saturation

SGT – trapped gas sat.

PCAP = PG – PL

ASL = FUNC( PCAP )

SL = ASL – SGT

IF( SL == 0 ) NPHAZ = 4



## Guidance on Primary Variables

- Direct Solution Path Between Primary and Secondary Variables
- Equation Residual is Sensitive to Primary Variable
- Think Creatively ...  $y_\ell^s$  - brine mass fraction of total salt

*Differential Form*

$$\frac{\partial}{\partial t} \left[ \sum_{\gamma=l,n,g,h,i,p} \left( \phi_D \rho_\gamma s_\gamma u_\gamma \right) + (1-\phi_T) \rho_s u_s + (\phi_T - \phi_D) \rho_l u_l \right] =$$

$$- \sum_{\gamma=l,n,g} \nabla \left( \rho_\gamma h_\gamma \mathbf{v}_\gamma \right) - \sum_{i=w,a,o} \nabla \left( h_g^i \mathbf{J}_g^i \right) + \nabla \left( \mathbf{k}_e \nabla T \right) + \sum_{\gamma=l,n,g} \left( h_\gamma m_\gamma \right) + q$$

*Nonlinear Algebraic Form*

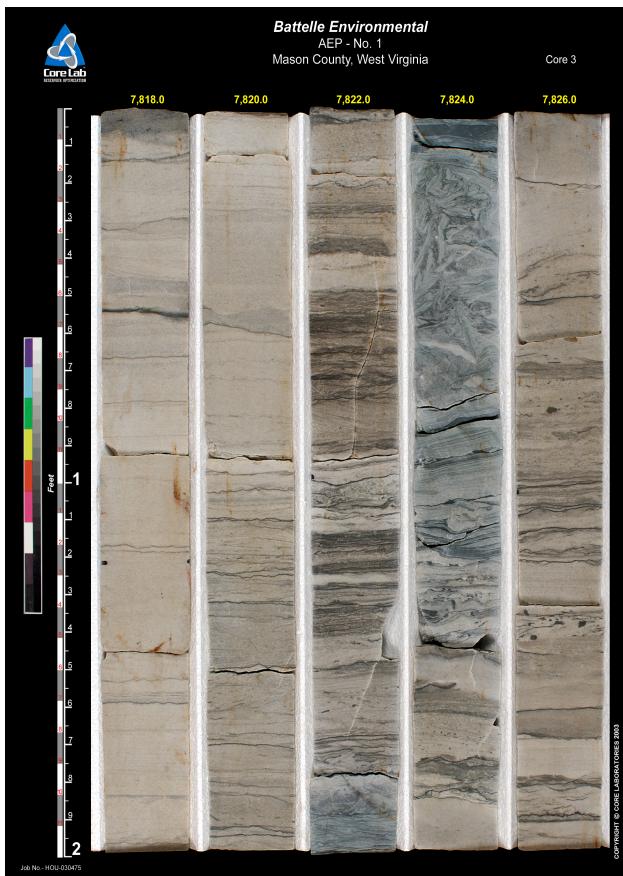
$$\mathbf{v}_\gamma = - \frac{k_{r\gamma} \mathbf{k}}{\mu_\gamma} \left( \nabla P_\gamma + \rho_\gamma g \mathbf{z}_g \right)$$

$$\mathbf{J}_g^i = -\phi_D \rho_g s_g \frac{M^i}{M_g} \left( \tau_g D_g^i + \mathbf{D}_{h_g} \right) \nabla \chi_g^i$$

*Spatial Discretization*

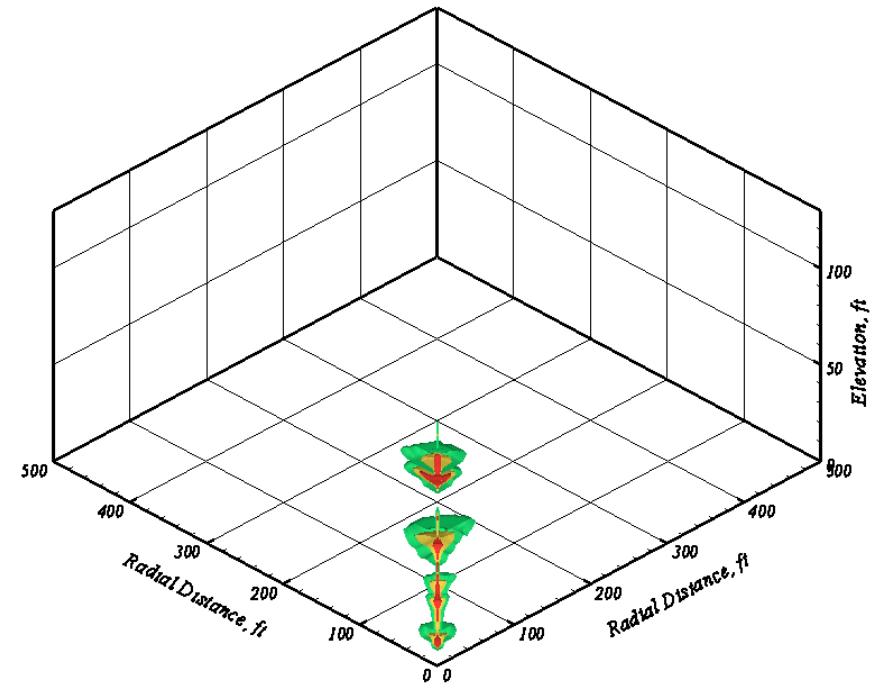
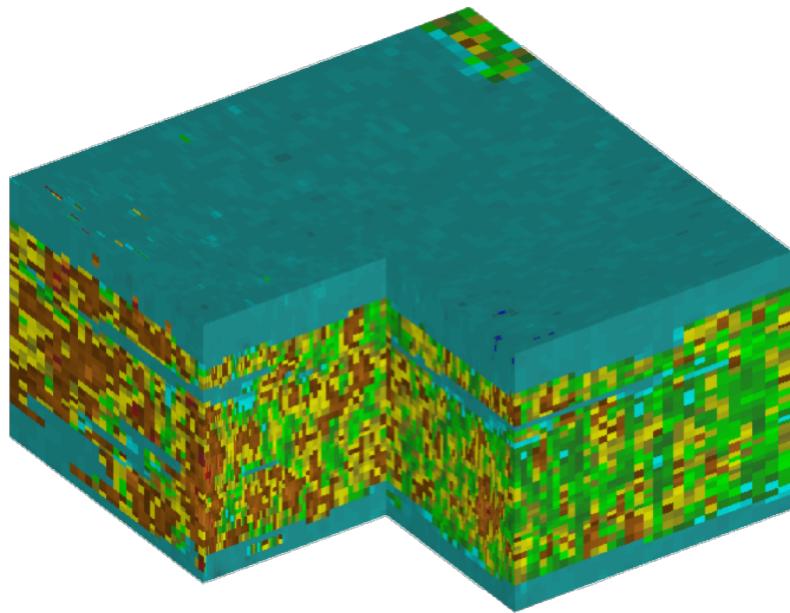


## High-Pressure CO<sub>2</sub>-Brine Systems



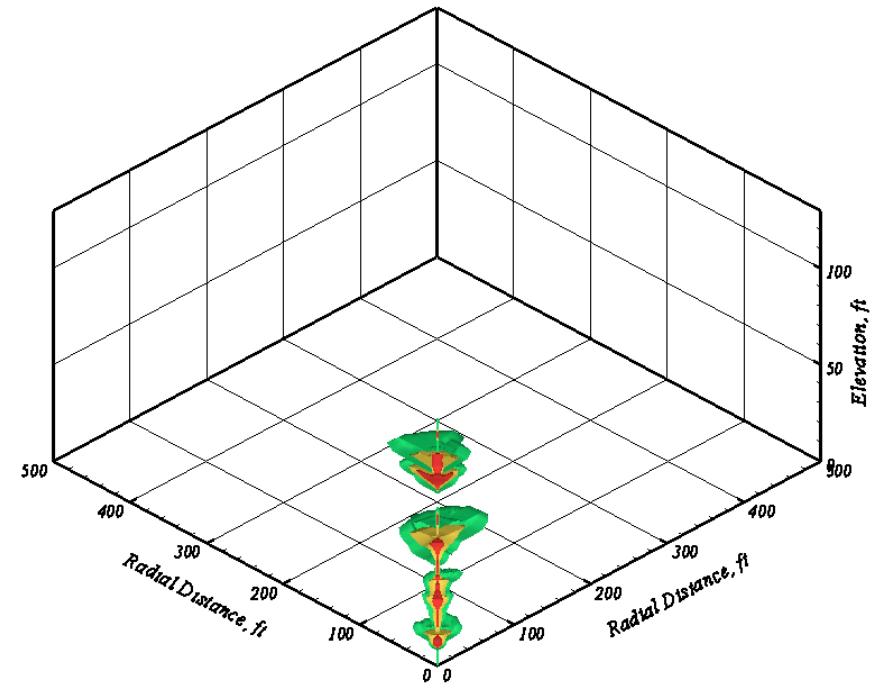
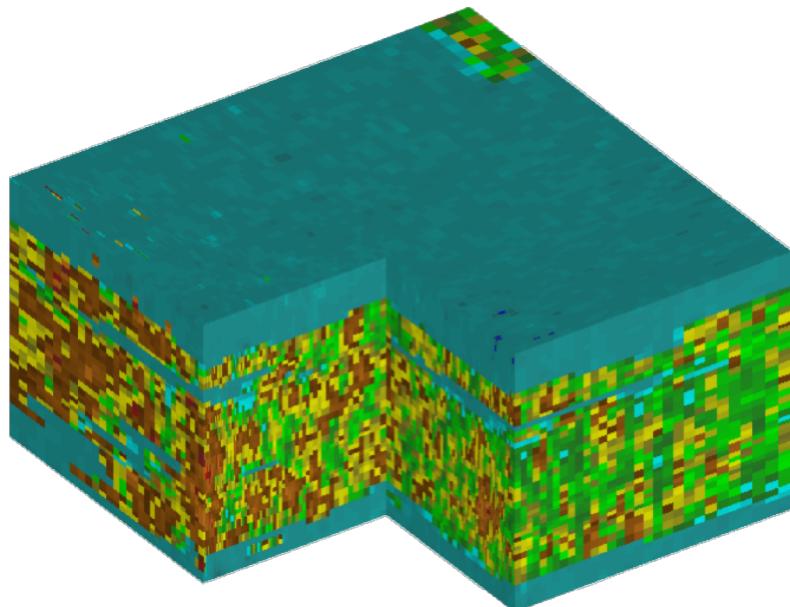


## High-Pressure CO<sub>2</sub>-Brine Systems: Example of Injection into Heterogeneous Domain



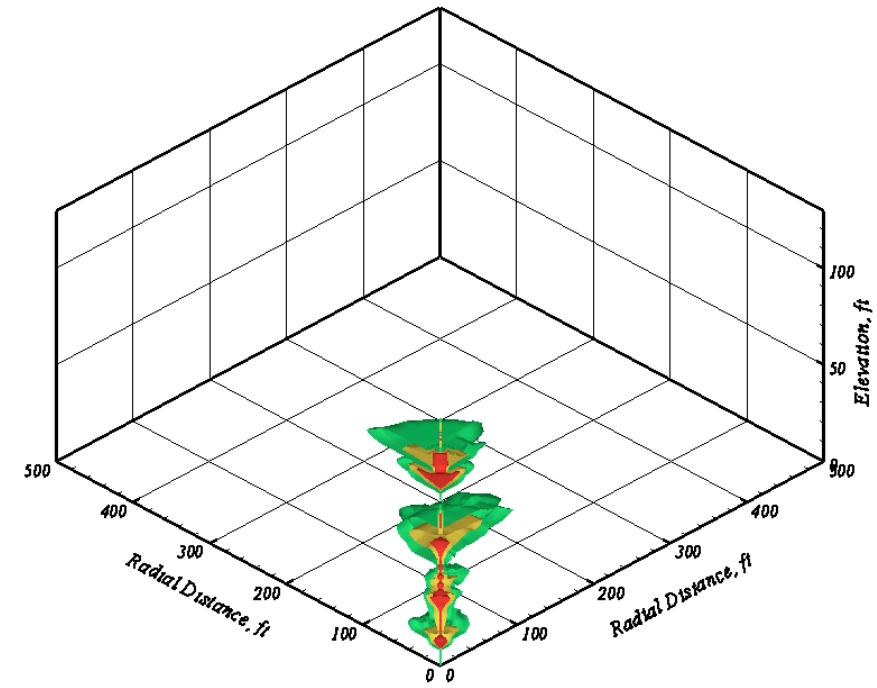
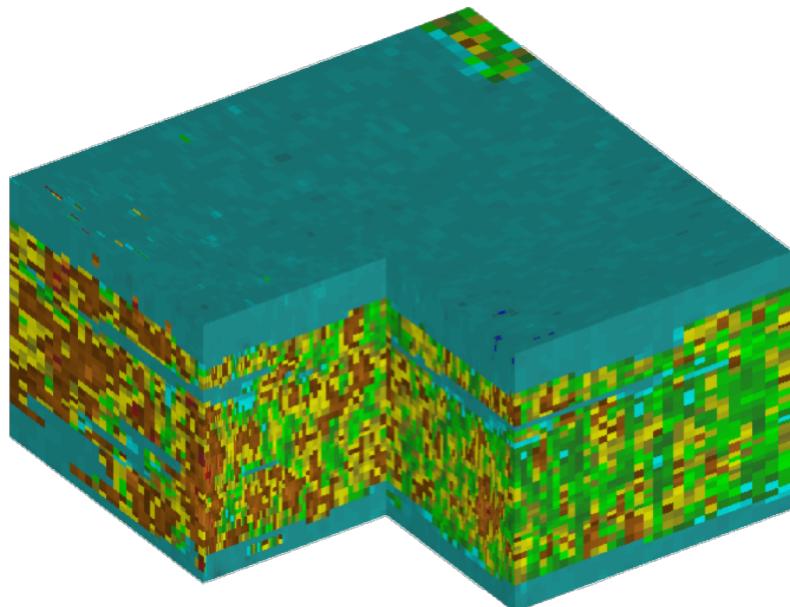


## High-Pressure CO<sub>2</sub>-Brine Systems: Example of Injection into Heterogeneous Domain



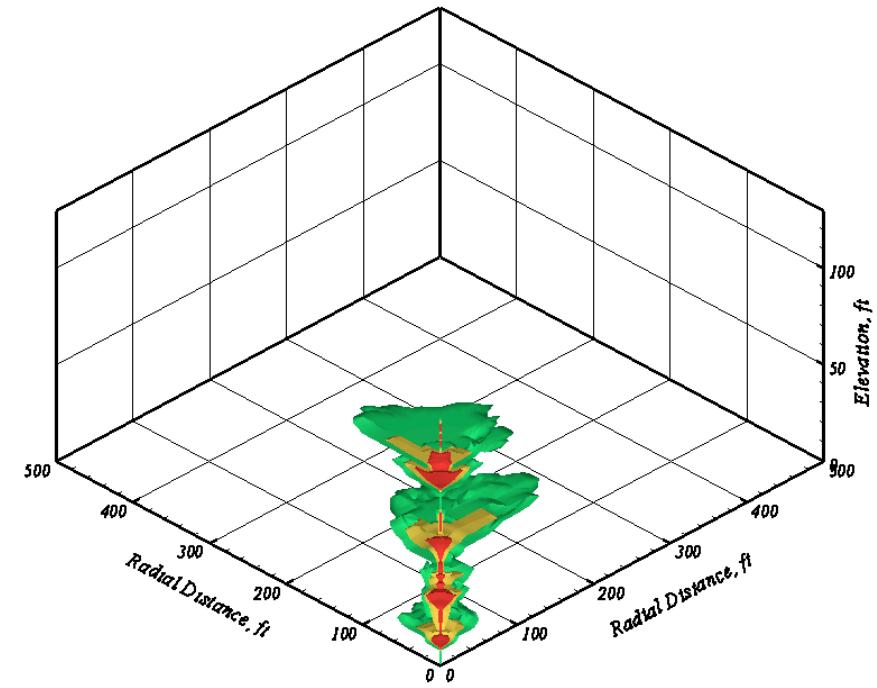
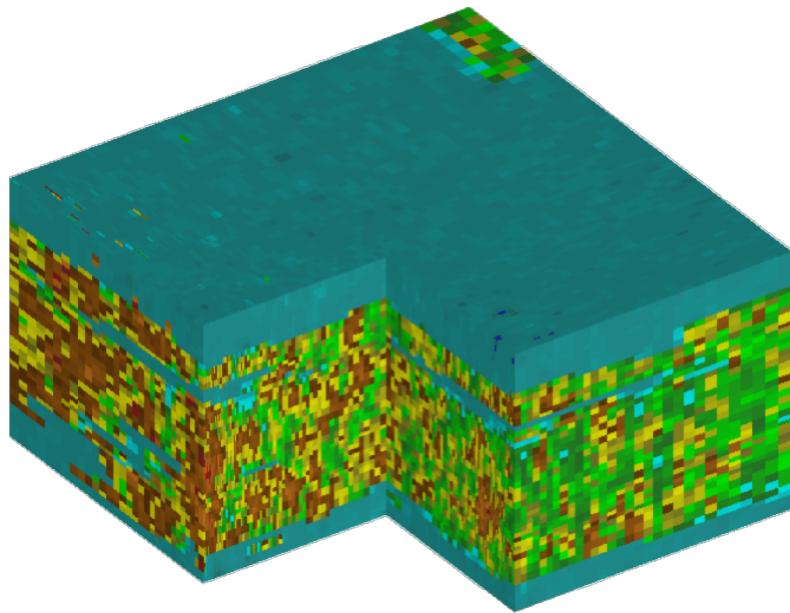


## High-Pressure CO<sub>2</sub>-Brine Systems: Example of Injection into Heterogeneous Domain



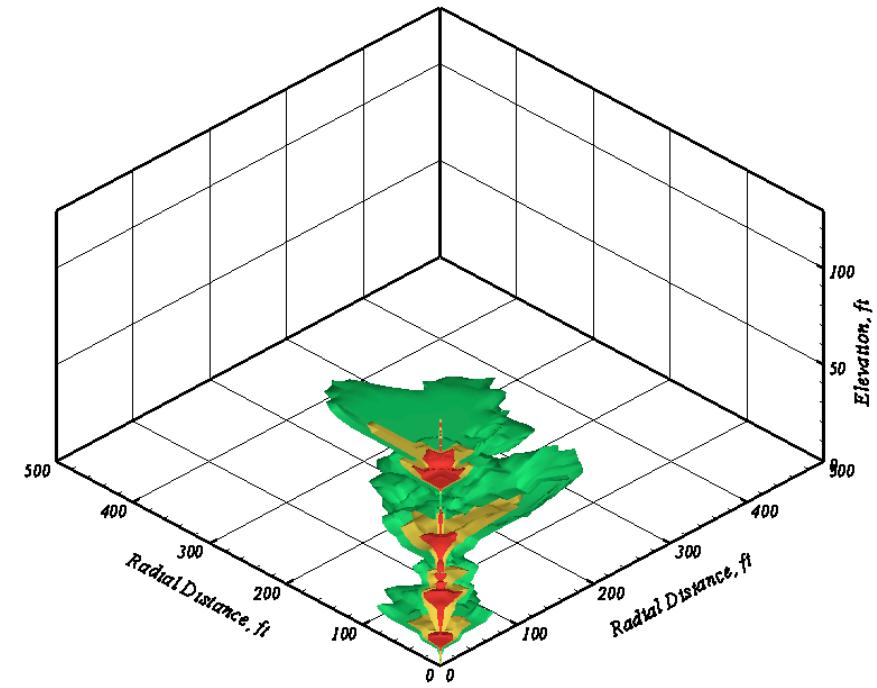
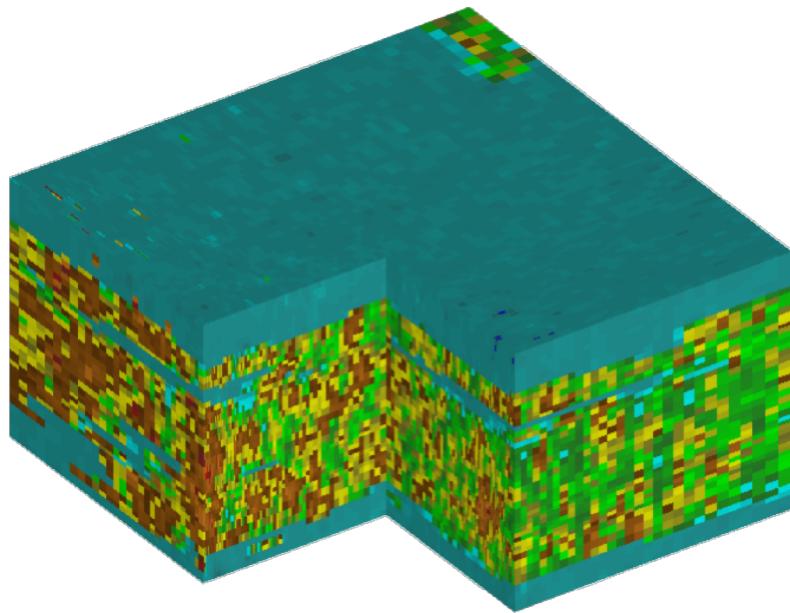


## High-Pressure CO<sub>2</sub>-Brine Systems: Example of Injection into Heterogeneous Domain



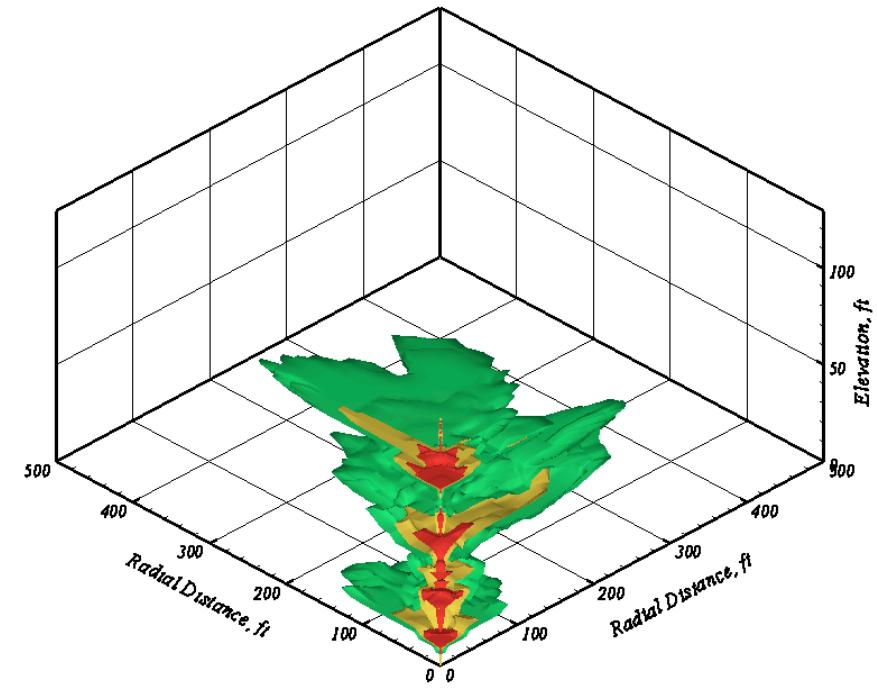
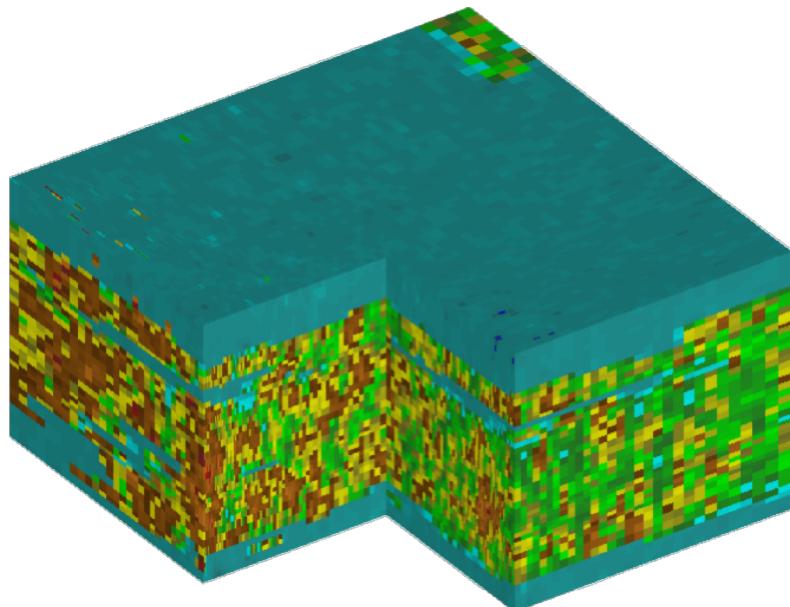


## High-Pressure CO<sub>2</sub>-Brine Systems: Example of Injection into Heterogeneous Domain



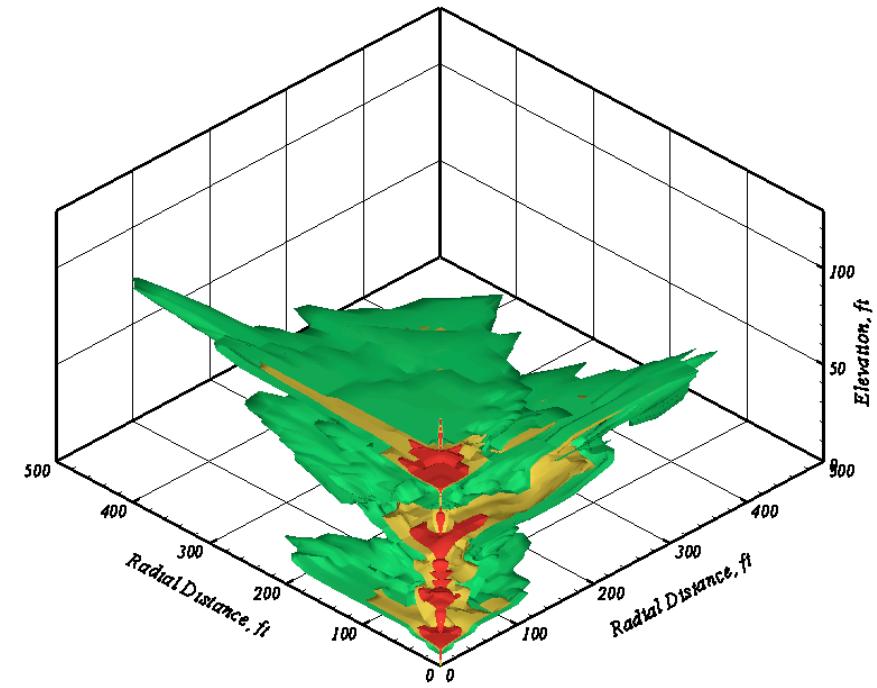
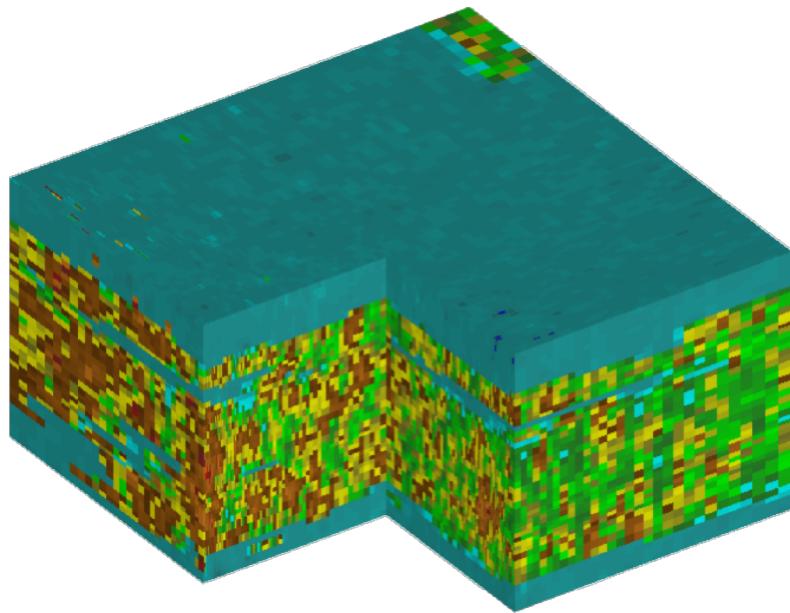


## High-Pressure CO<sub>2</sub>-Brine Systems: Example of Injection into Heterogeneous Domain



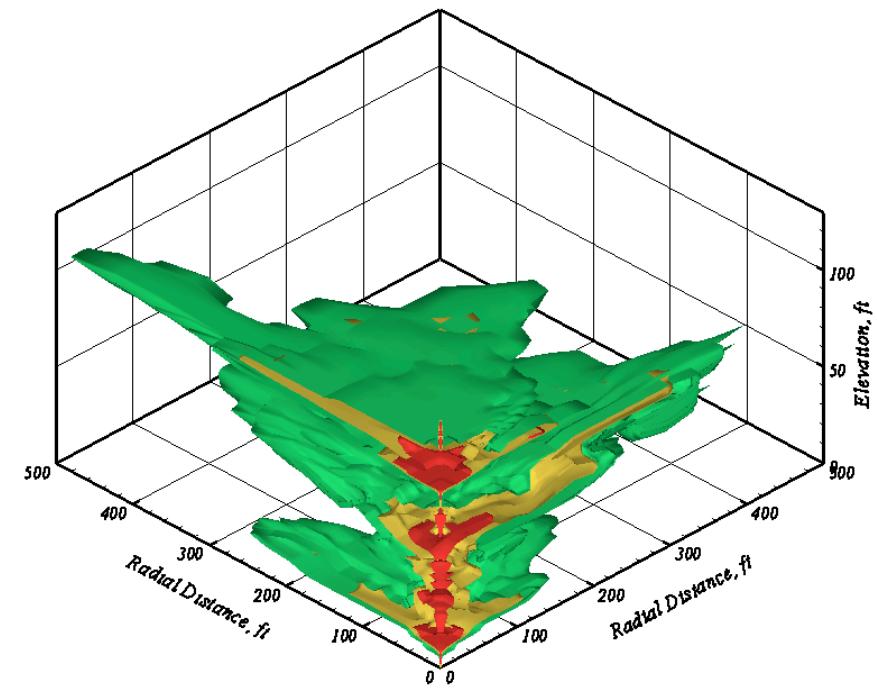
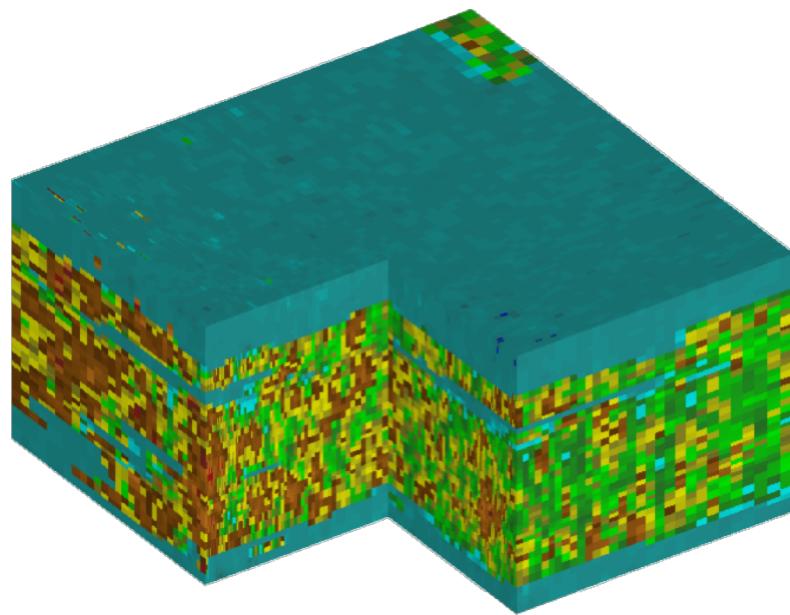


## High-Pressure CO<sub>2</sub>-Brine Systems: Example of Injection into Heterogeneous Domain





## High-Pressure CO<sub>2</sub>-Brine Systems: Example of Injection into Heterogeneous Domain

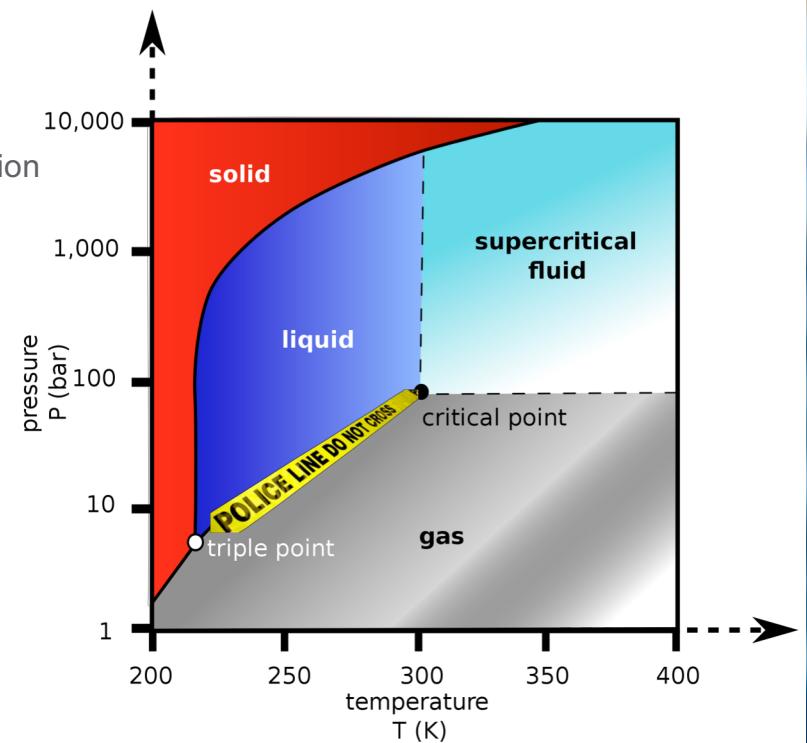


# High-Pressure CO<sub>2</sub>-Brine Systems: Phase Conditions



## Phase Conditions

1. Saturated without Trapped Gas
  - Energy – Temperature
  - Water Mass – Aqueous Pressure
  - CO<sub>2</sub> Mass – Aqueous CO<sub>2</sub> Mole Fraction
  - Salt Mass – Total Brine Mass Fraction
2. Partially Saturated
  - Energy – Temperature
  - Water Mass – Aqueous Pressure
  - CO<sub>2</sub> Mass – Gas Pressure
  - Salt Mass – Total Brine Mass Fraction
3. Saturated with Trapped Gas
  - Energy – Temperature
  - Water Mass – Aqueous Pressure
  - CO<sub>2</sub> Mass – Trapped Gas Saturation
  - Salt Mass – Total Brine Mass Fraction
4. Fully Unsaturated
  - Energy – Temperature
  - Water Mass – Water Vapor Partial Pressure
  - CO<sub>2</sub> Mass – Gas Pressure
  - Salt Mass – Salt Mass





# High-Pressure CO<sub>2</sub>-Brine Systems: Phase Conditions and Transitions

## Phase Conditions

1. Saturated without Trapped Gas
  - Energy – Temperature
  - Water Mass – Aqueous Pressure
  - CO<sub>2</sub> Mass – Aqueous CO<sub>2</sub> Mole Fraction
  - Salt Mass – Total Brine Mass Fraction
2. Partially Saturated
  - Energy – Temperature
  - Water Mass – Aqueous Pressure
  - CO<sub>2</sub> Mass – Gas Pressure
  - Salt Mass – Total Brine Mass Fraction
3. Saturated with Trapped Gas
  - Energy – Temperature
  - Water Mass – Aqueous Pressure
  - CO<sub>2</sub> Mass – Trapped Gas Saturation
  - Salt Mass – Total Brine Mass Fraction
4. Fully Unsaturated
  - Energy – Temperature
  - Water Mass – Water Vapor Partial Pressure
  - CO<sub>2</sub> Mass – Gas Pressure
  - Salt Mass – Salt Mass



PGA – CO<sub>2</sub> partial pressure  
PGW – water partial pressure  
PG – gas pressure  
PL – aqueous pressure  
SG – gas saturation  
SL – aqueous saturation

PGA = FUNC( XMLA )  
PGW = FUNC( T,PCAP )  
PG = PGW + PGA  
PCAP = PG – PL  
SL = FUNC( PCAP )  
SG = 1.D+0 – SL  
IF( SG > 1.D-3 ) NPHAZ = 2



# High-Pressure CO<sub>2</sub>-Brine Systems: Phase Conditions and Transitions

## Phase Conditions

### 1. Saturated without Trapped Gas

- Energy – Temperature
- Water Mass – Aqueous Pressure
- CO<sub>2</sub> Mass – Aqueous CO<sub>2</sub> Mole Fraction
- Salt Mass – Total Brine Mass Fraction

### 2. Partially Saturated

- Energy – Temperature
- Water Mass – Aqueous Pressure
- CO<sub>2</sub> Mass – Gas Pressure
- Salt Mass – Total Brine Mass Fraction

### 3. Saturated with Trapped Gas

- Energy – Temperature
- Water Mass – Aqueous Pressure
- CO<sub>2</sub> Mass – Trapped Gas Saturation
- Salt Mass – Total Brine Mass Fraction

### 4. Fully Unsaturated

- Energy – Temperature
- Water Mass – Water Vapor Partial Pressure
- CO<sub>2</sub> Mass – Gas Pressure
- Salt Mass – Salt Mass



PG – gas pressure

PL – aqueous pressure

ASL – apparent aqueous sat.

SGT – trapped gas sat.

PCAP = PG – PL

ASL = FUNC( PCAP )

IF( ASL == 0 && SGT == 0 )

NPHAZ = 1



# High-Pressure CO<sub>2</sub>-Brine Systems: Phase Conditions and Transitions



## Phase Conditions

1. Saturated without Trapped Gas
  - Energy – Temperature
  - Water Mass – Aqueous Pressure
  - CO<sub>2</sub> Mass – Aqueous CO<sub>2</sub> Mole Fraction
  - Salt Mass – Total Brine Mass Fraction
2. Partially Saturated
  - Energy – Temperature
  - Water Mass – Aqueous Pressure
  - CO<sub>2</sub> Mass – Gas Pressure
  - Salt Mass – Total Brine Mass Fraction
3. Saturated with Trapped Gas
  - Energy – Temperature
  - Water Mass – Aqueous Pressure
  - CO<sub>2</sub> Mass – Trapped Gas Saturation
  - Salt Mass – Total Brine Mass Fraction
4. Fully Unsaturated
  - Energy – Temperature
  - Water Mass – Water Vapor Partial Pressure
  - CO<sub>2</sub> Mass – Gas Pressure
  - Salt Mass – Salt Mass



PG – gas pressure

PL – aqueous pressure

ASL – apparent aqueous sat.

SGT – trapped gas sat.

PCAP = PG – PL

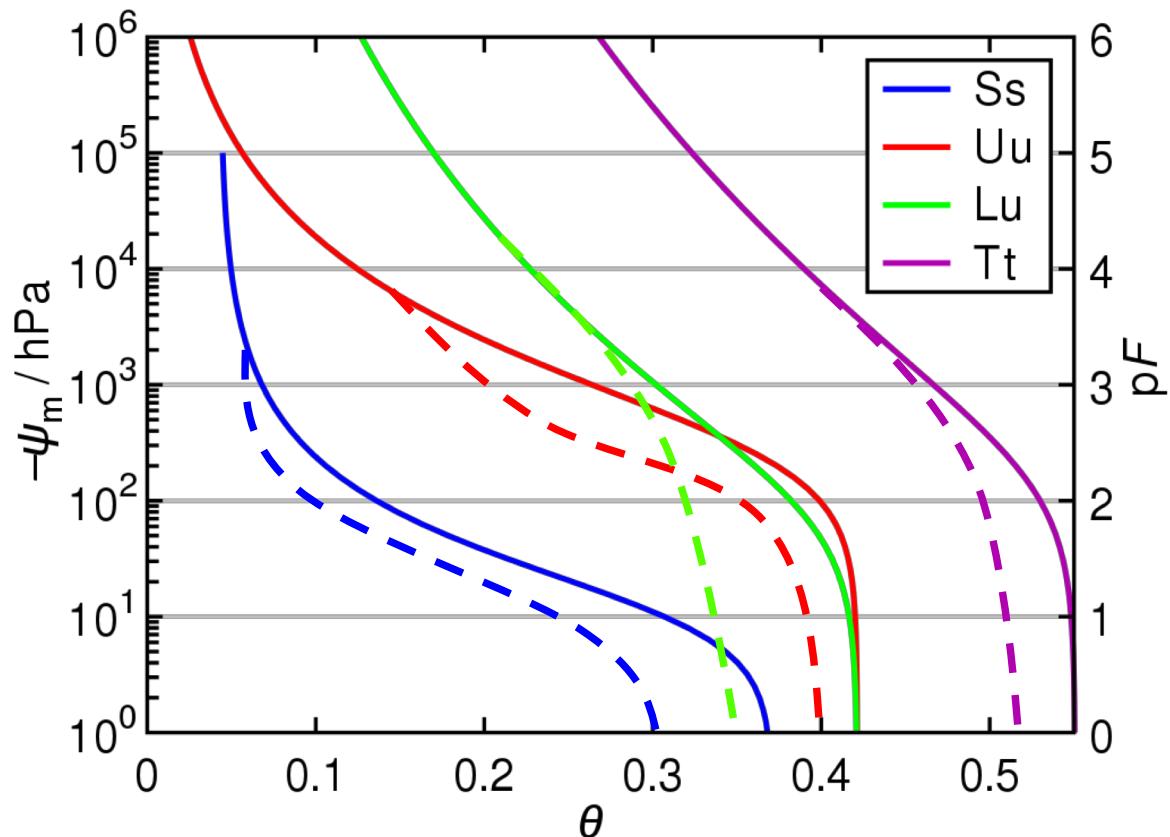
ASL = FUNC( PCAP )

IF( ASL == 0 && SGT > 0 )

NPHAZ = 3



## Low-Pressure Air-Water Systems: Phase Conditions and Transitions



Ss – sand  
Uu – silt or clay loam  
LU – loam-silt or clay  
Tt – clay or peat



# High-Pressure CO<sub>2</sub>-Brine Systems: Phase Conditions and Transitions



## Phase Conditions

1. Saturated without Trapped Gas
  - Energy – Temperature
  - Water Mass – Aqueous Pressure
  - CO<sub>2</sub> Mass – Aqueous CO<sub>2</sub> Mole Fraction
  - Salt Mass – Total Brine Mass Fraction
2. Partially Saturated
  - Energy – Temperature
  - Water Mass – Aqueous Pressure
  - CO<sub>2</sub> Mass – Gas Pressure
  - Salt Mass – Total Brine Mass Fraction
3. Saturated with Trapped Gas
  - Energy – Temperature
  - Water Mass – Aqueous Pressure
  - CO<sub>2</sub> Mass – Trapped Gas Saturation
  - Salt Mass – Total Brine Mass Fraction
4. Fully Unsaturated
  - Energy – Temperature
  - Water Mass – Water Vapor Partial Pressure
  - CO<sub>2</sub> Mass – Gas Pressure
  - Salt Mass – Salt Mass



PG – gas pressure

PL – aqueous pressure

ASL – apparent aqueous sat.

SL – aqueous saturation

SGT – trapped gas sat.

PCAP = PG – PL

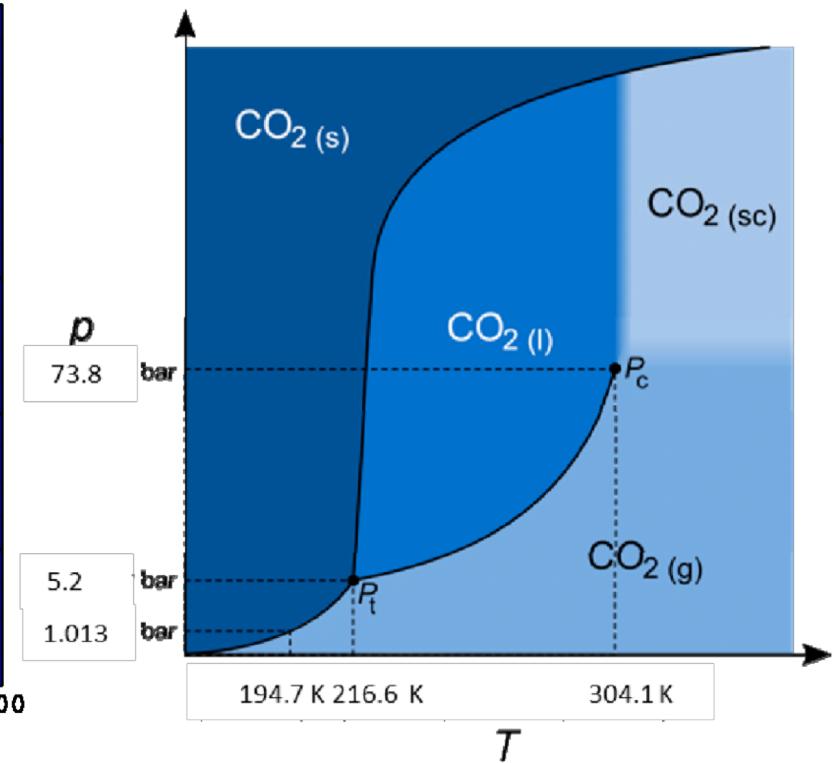
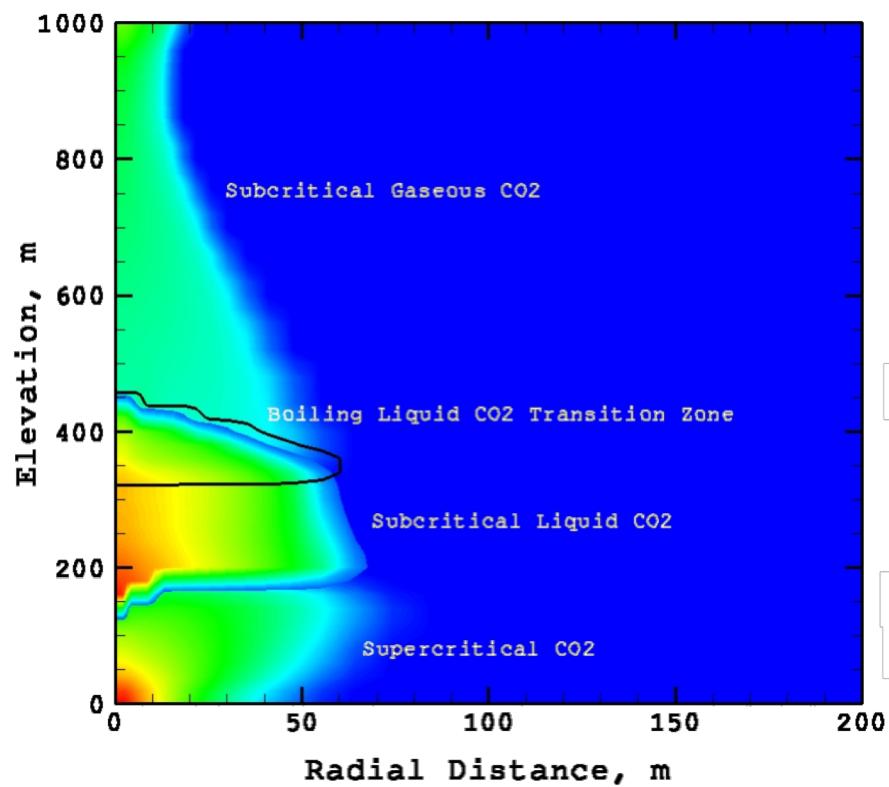
ASL = FUNC( PCAP )

SL = ASL – SGT

IF( SL == 0 ) NPHAZ = 4

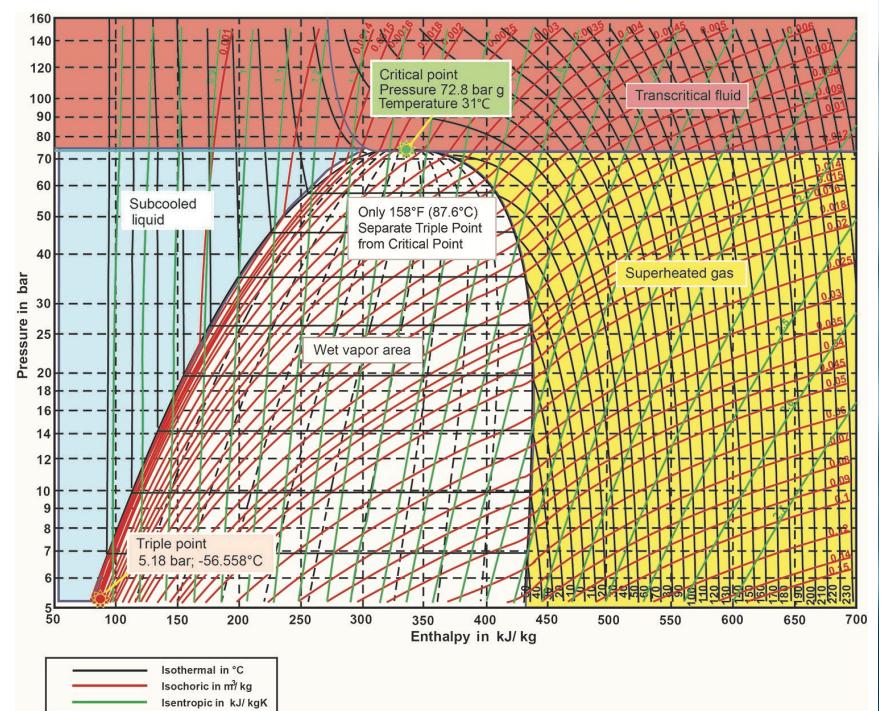
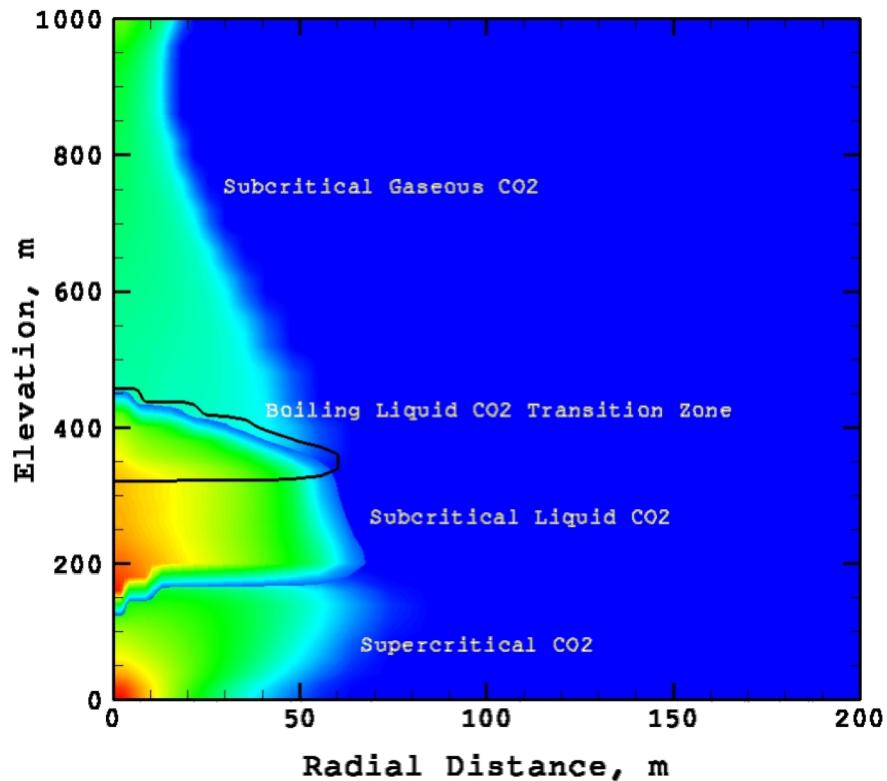


## Leakage of CO<sub>2</sub> from Deep Reservoirs to the Ground Surface



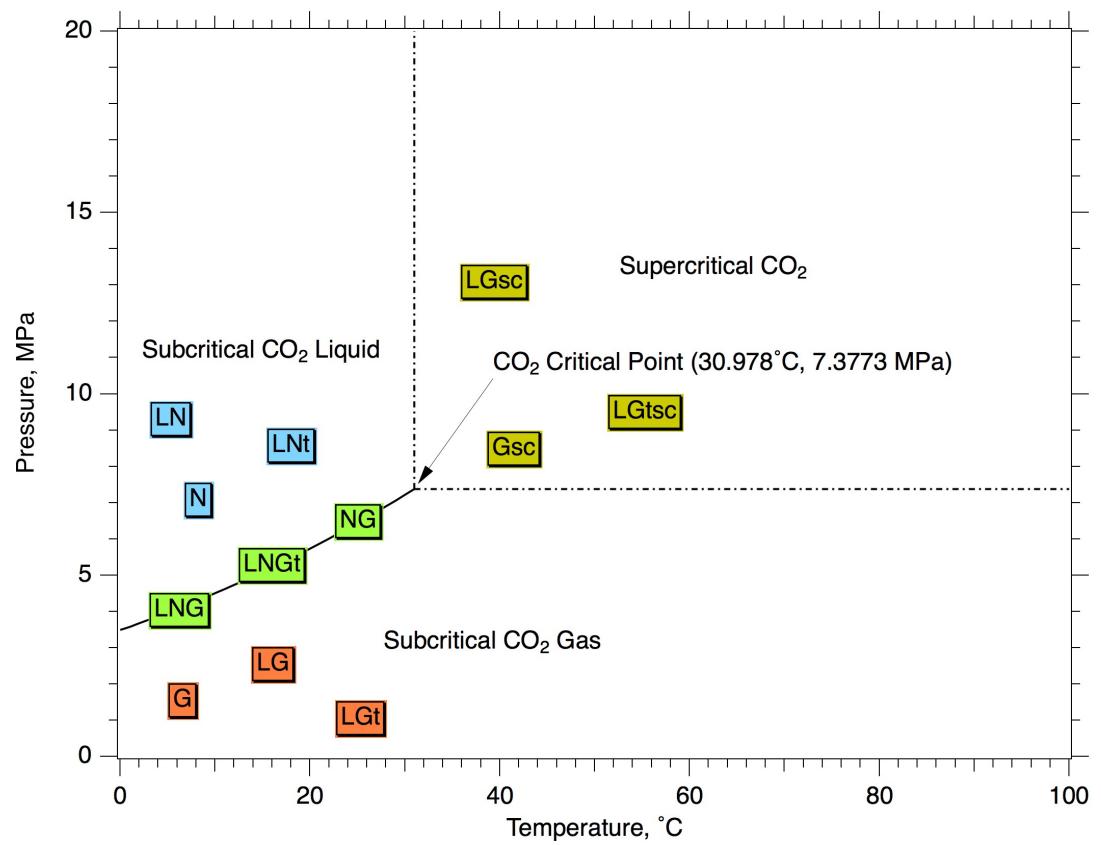
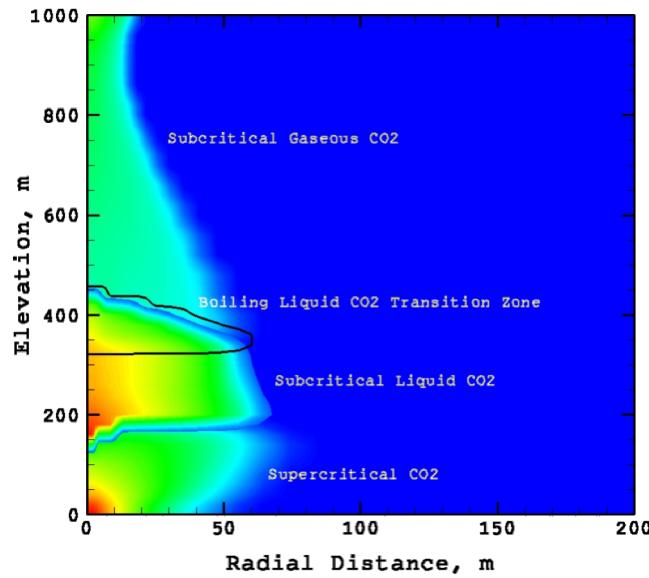


# Leakage of CO<sub>2</sub> from Deep Reservoirs to the Ground Surface





# Three-Phase System for CO<sub>2</sub> Migration through the Subsurface: Phase Condition Mapping



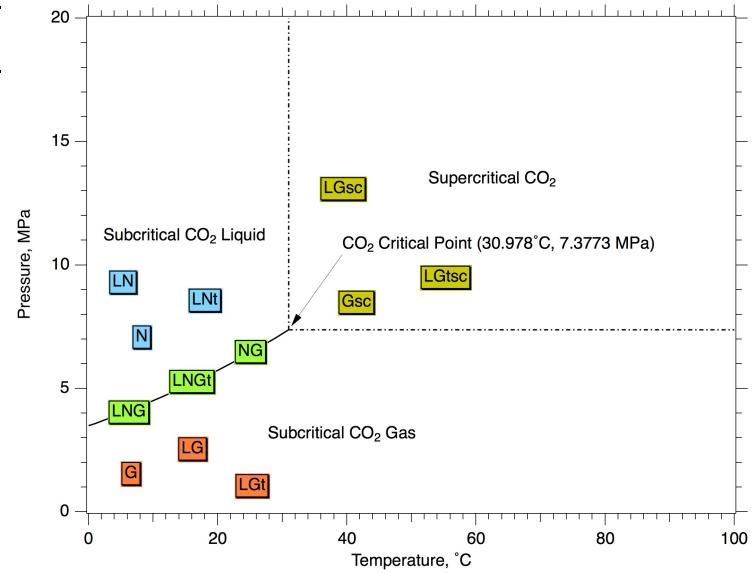


# Three-Phase System for CO<sub>2</sub> Migration through the Subsurface: Phase Conditions and Primary Variables



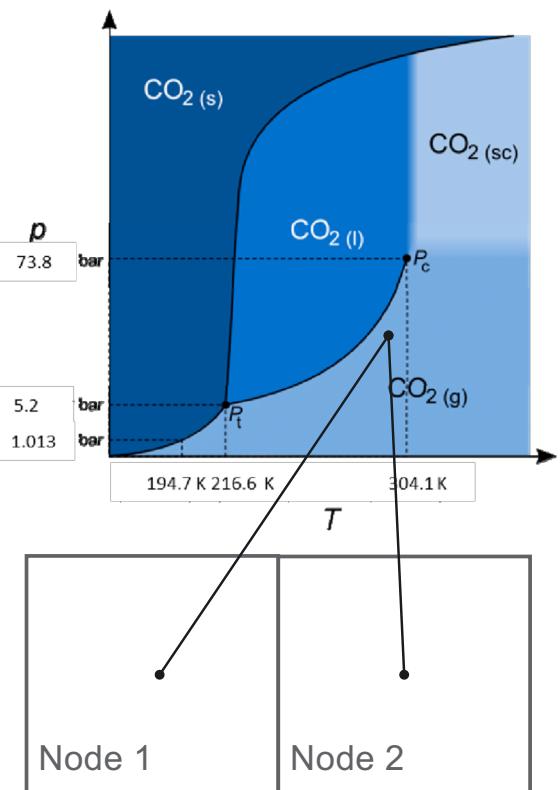
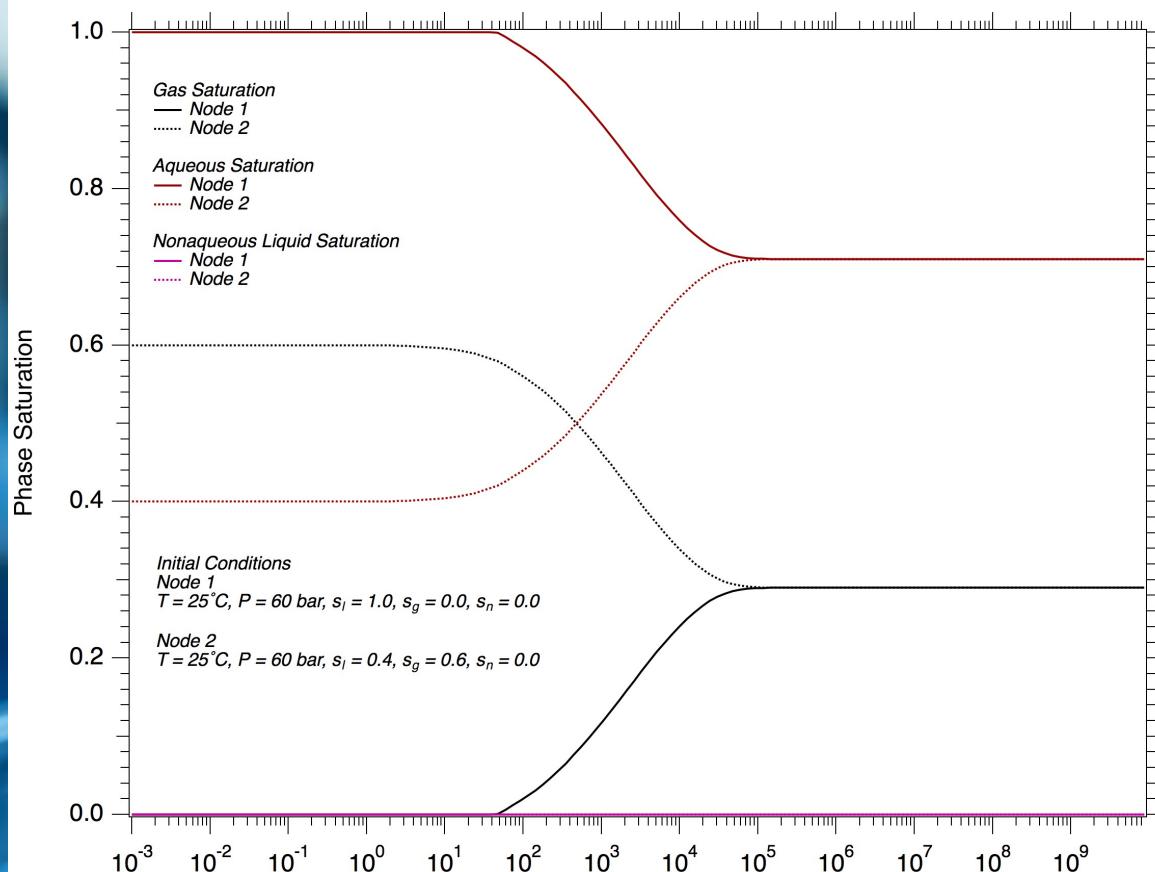
Table 1. STOMP-SEQ primary variable switching scheme.

Phase Condition	Energy Equation	Water Mass Equation	CO <sub>2</sub> Mass Equation	Salt Mass Equation
L	$T$	$P_\ell$	$\omega_\ell^C$	$y_\ell^S$
G	$T$	$P_v^W$	$P_g$	$T_m^S$
Gsc	$T$	$P_v^W$	$P_g$	$T_m^S$
N	$T$	$P_v^W$	$P_n$	$T_m^S$
LG	$T$	$P_\ell$	$P_g$	$y_\ell^S$
LGt	$T$	$P_\ell$	$s_{gt}$	$y_\ell^S$
LGsc	$T$	$P_\ell$	$P_g$	$y_\ell^S$
LGtsc	$T$	$P_\ell$	$s_{gt}$	$y_\ell^S$
LN	$T$	$P_\ell$	$P_n$	$y_\ell^S$
LNt	$T$	$P_\ell$	$s_{nt}$	$y_\ell^S$
NG	$T$	$P_v^W$	$\beta$	$T_m^S$
LNG	$T$	$P_\ell$	$\beta$	$y_\ell^S$
LNGt	$T$	$s_{gt} + s_{nt}$	$\beta$	$y_\ell^S$



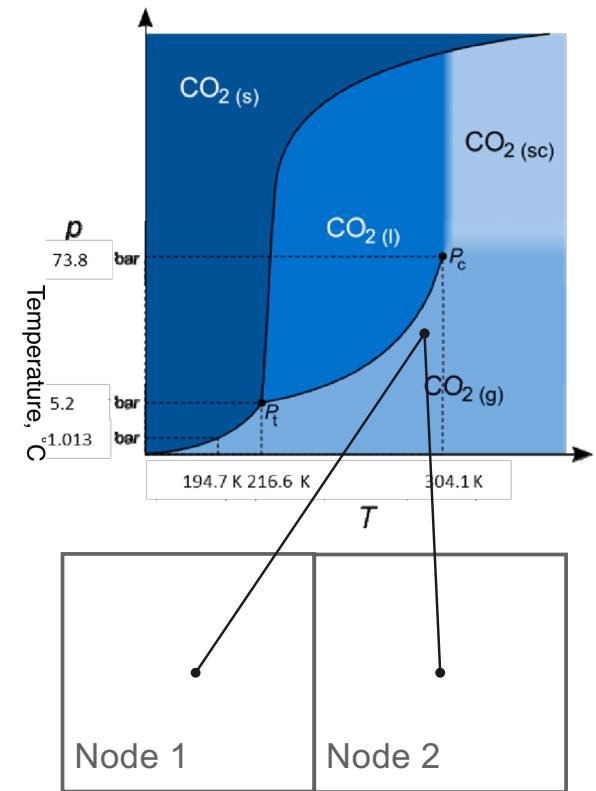
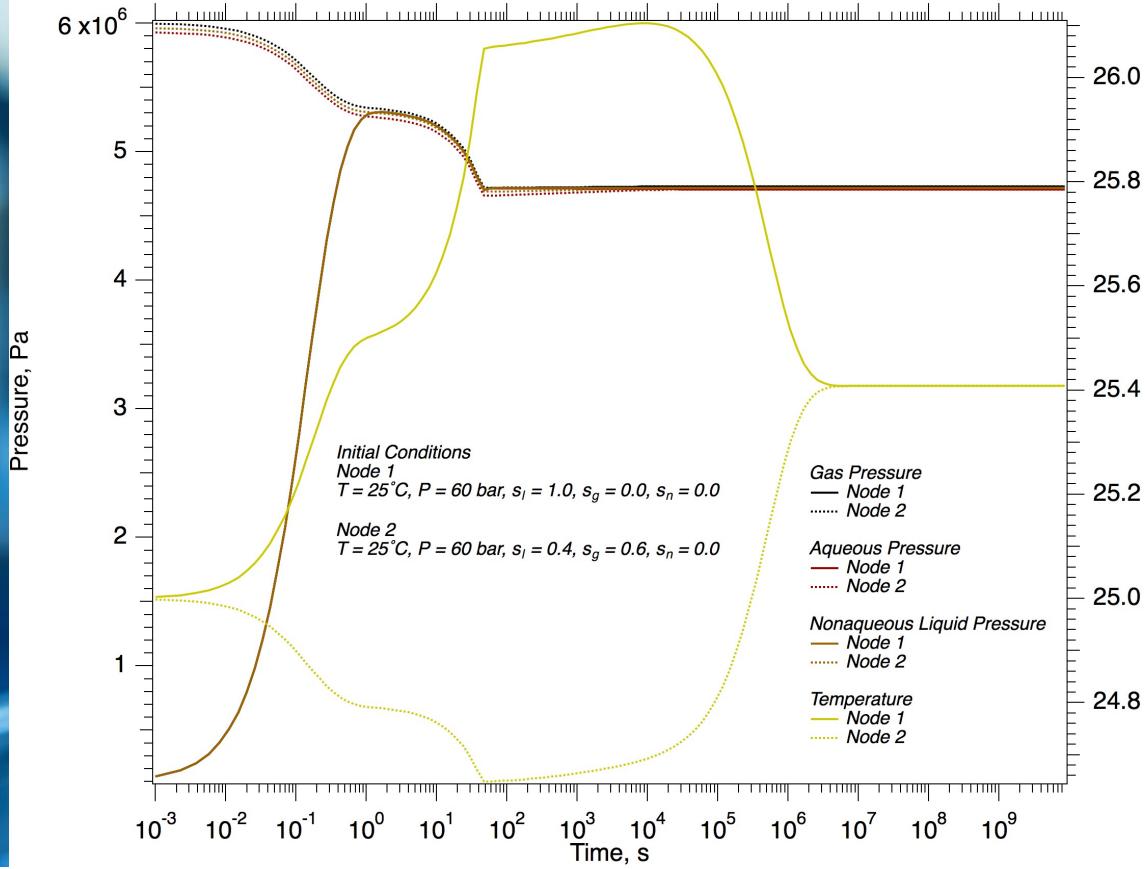


## Code Validation via False Transients to Equilibrium Conditions



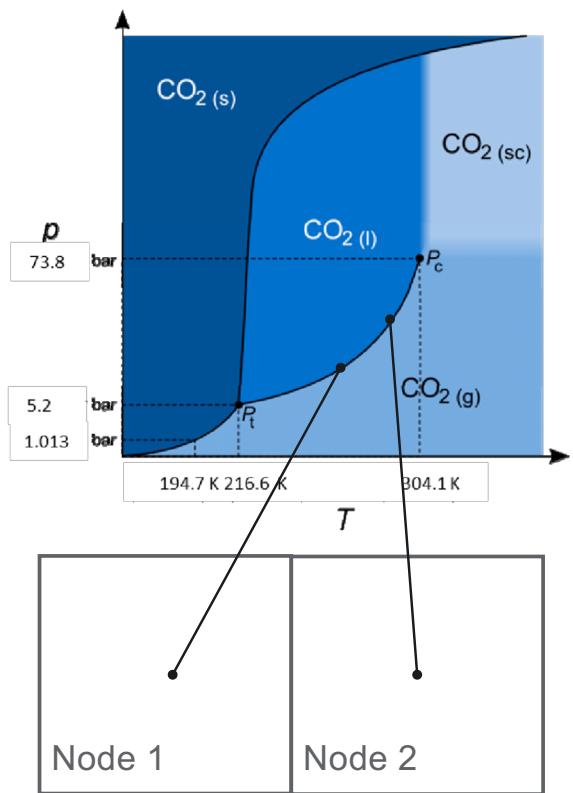
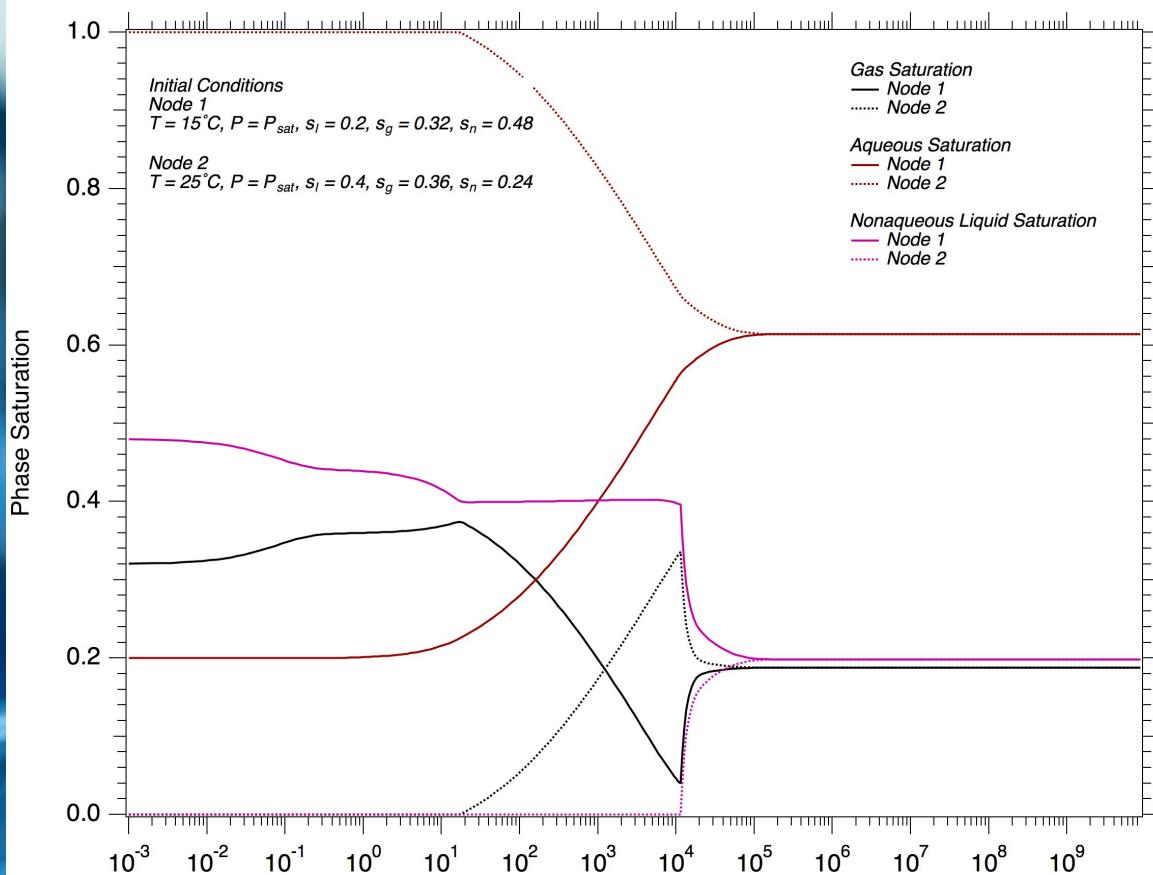


## Code Validation via False Transients to Equilibrium Conditions



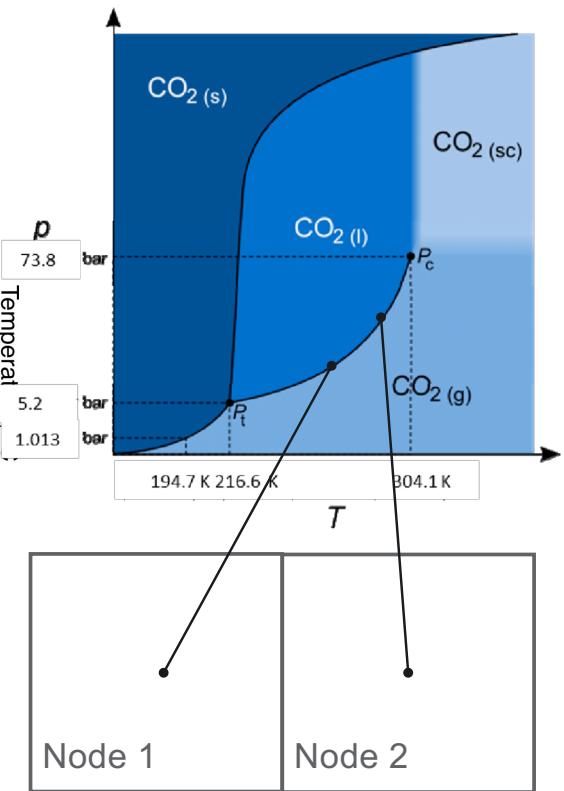
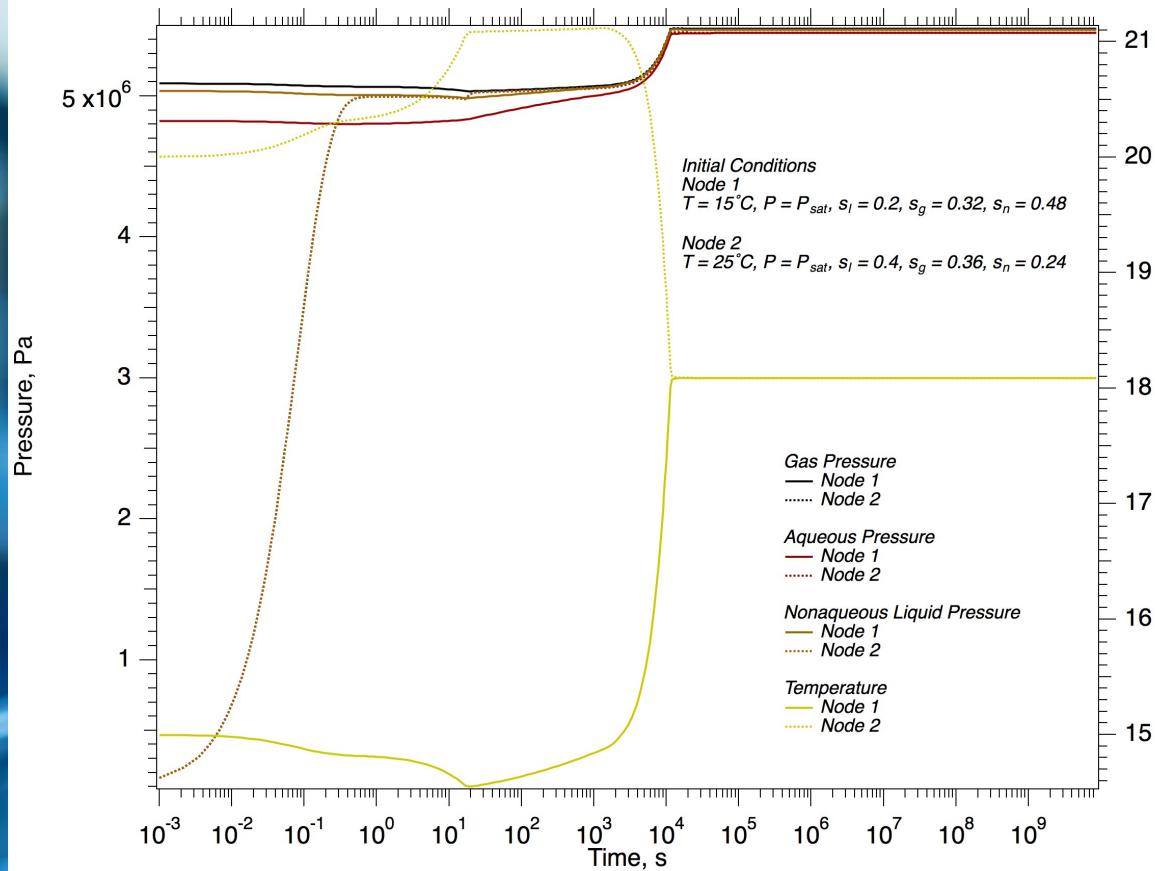


## Code Validation via False Transients to Equilibrium Conditions





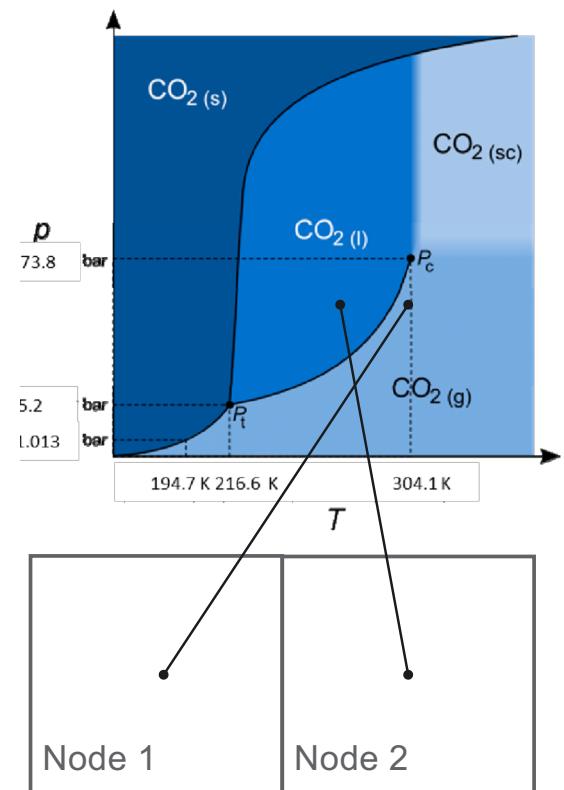
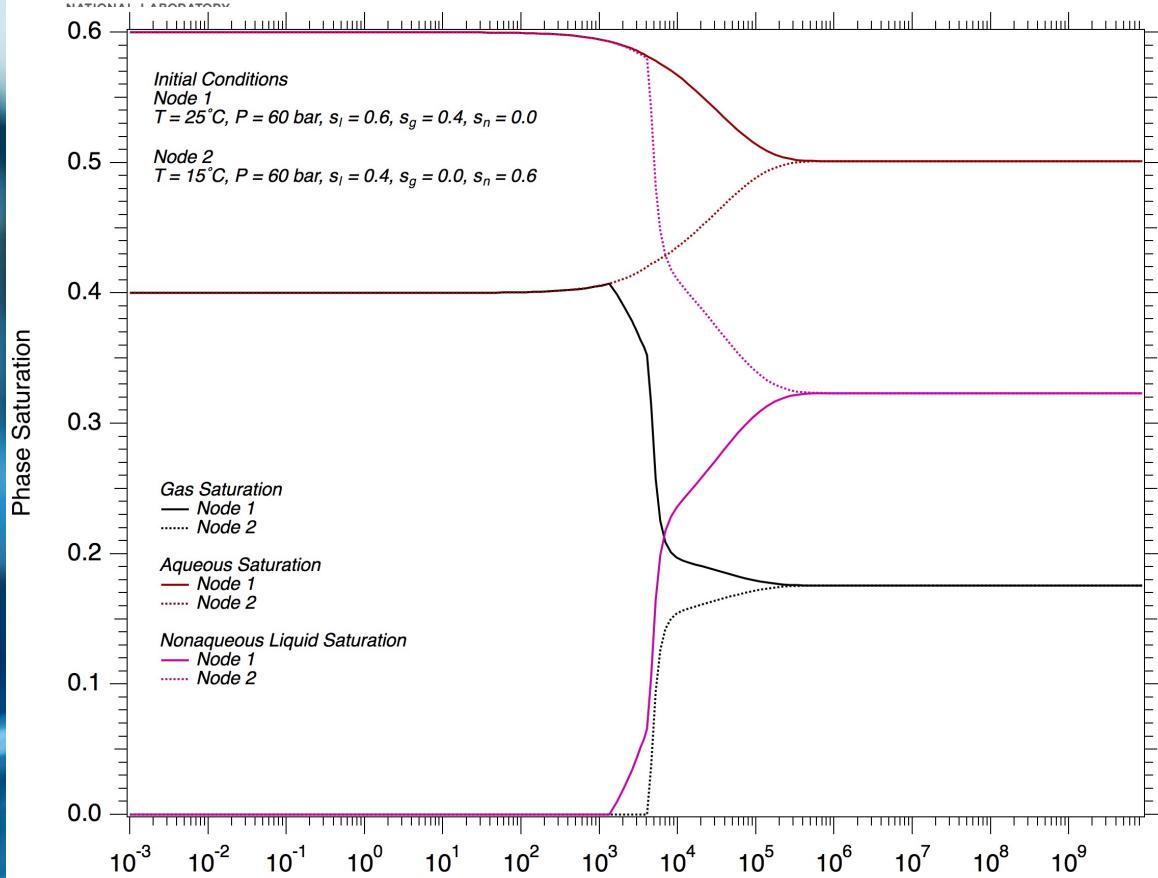
## Code Validation via False Transients to Equilibrium Conditions





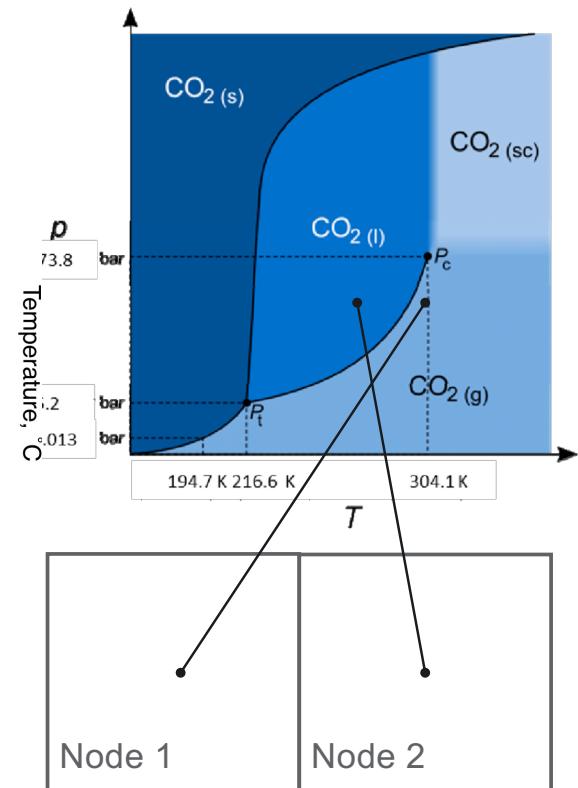
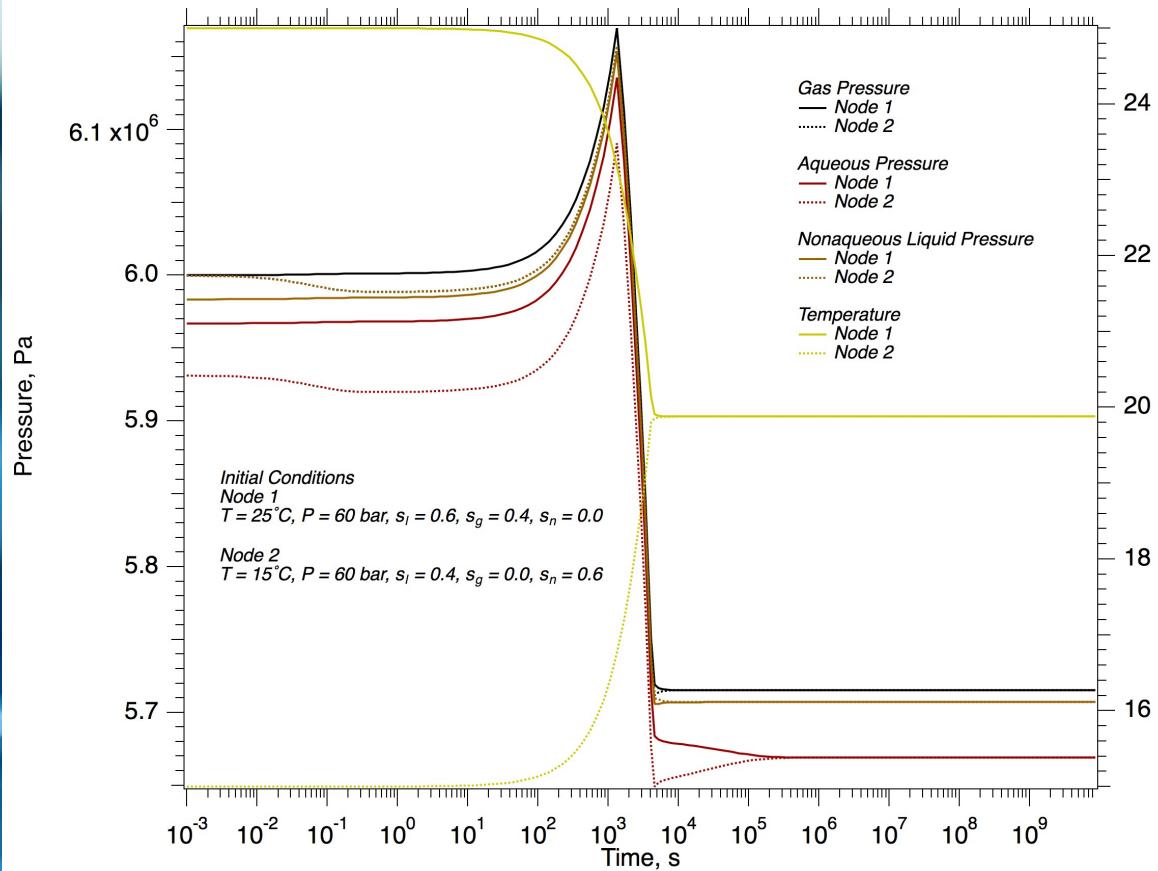
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## Code Validation via False Transients to Equilibrium Conditions





## Code Validation via False Transients to Equilibrium Conditions

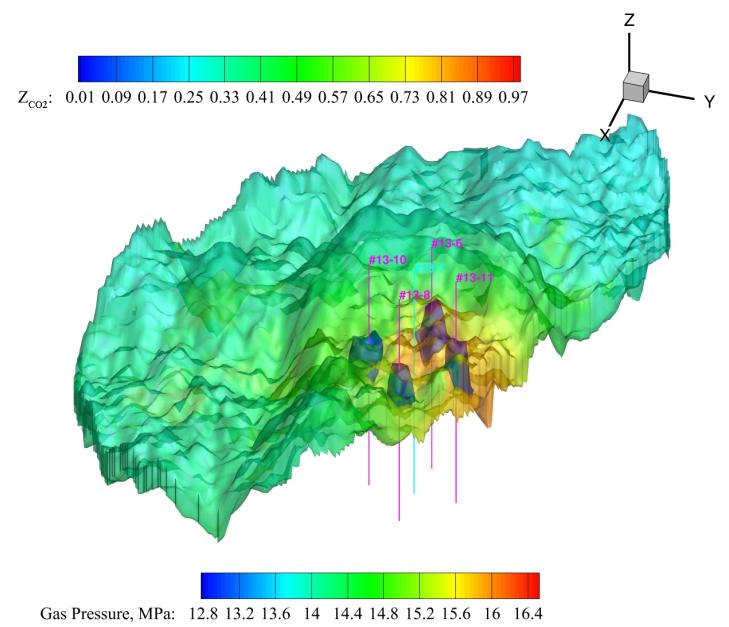




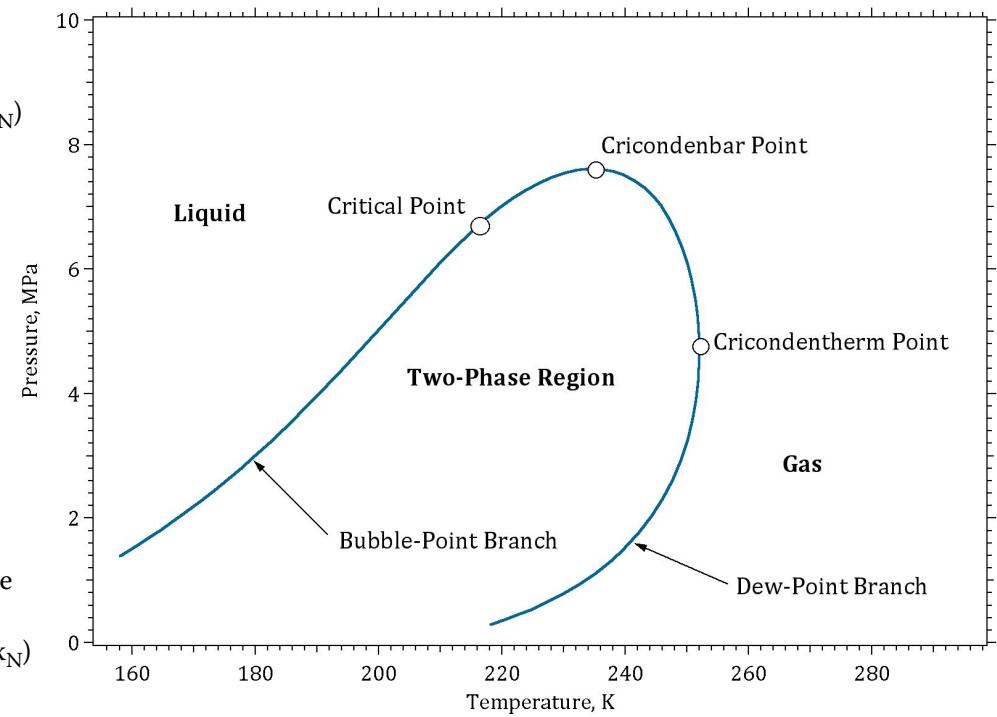
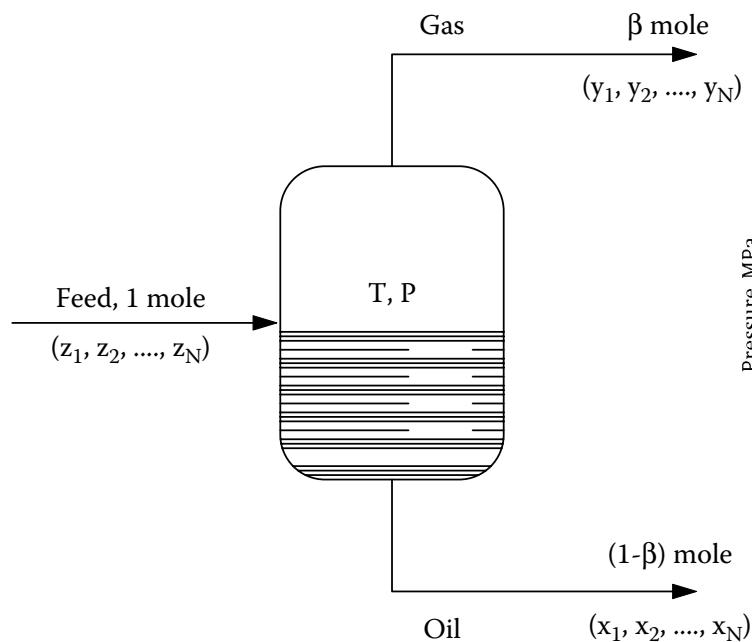
# Three-Phase System for Enhanced Oil Recovery: Basics



- Mobile phases
  - Aqueous (water, CO<sub>2</sub>, salt)
  - Nonaqueous liquid (CO<sub>2</sub>, CH<sub>4</sub>, n-petroleum components)
  - Gas (CO<sub>2</sub>, CH<sub>4</sub>, n-petroleum components)
- Phase equilibria from cubic equation of state
  - Peng-Robinson
  - Soave-Redlich-Kwong
- Phase properties
  - Cubic equation of state
  - Corresponding state method
  - Empirical correlations

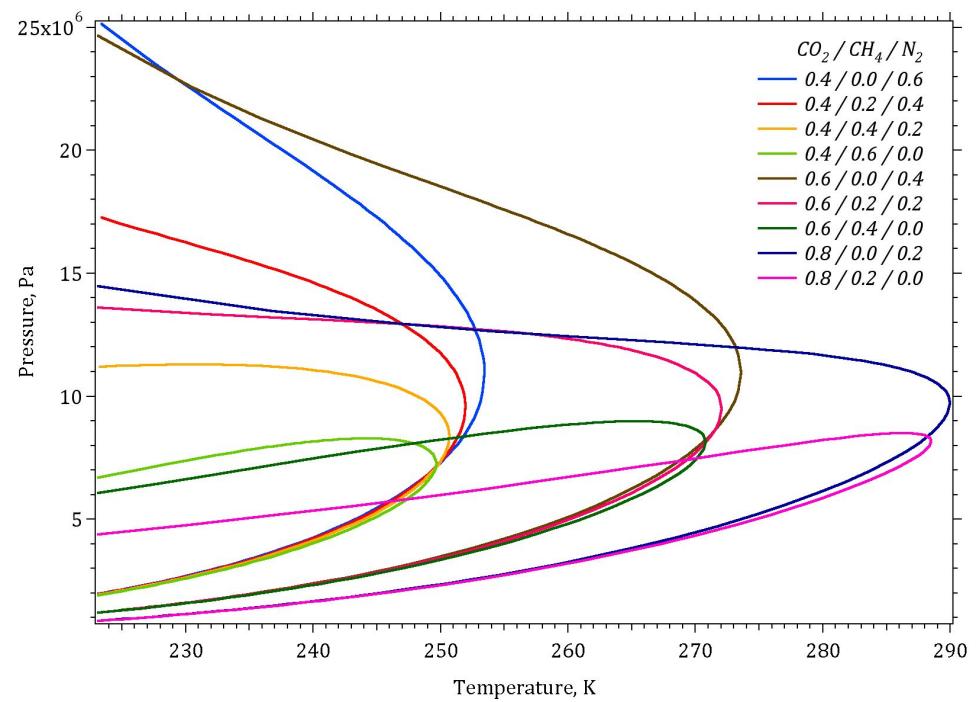
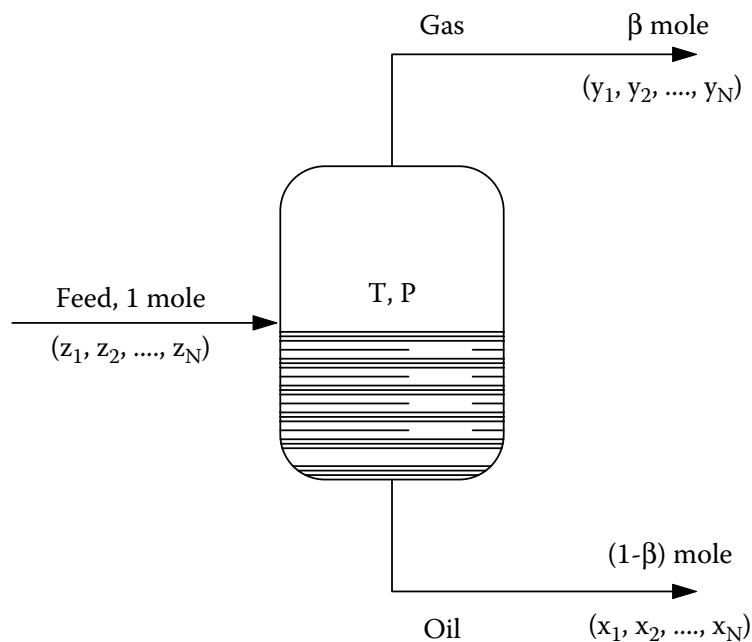


## Three-Phase System for Enhanced Oil Recovery: Phase Equilibria



Source: Pedersen, K. S., and P. L. Christensen. 2007. *Phase Behavior of Petroleum Reservoir Fluids*. CRC Taylor & Francis, New York.

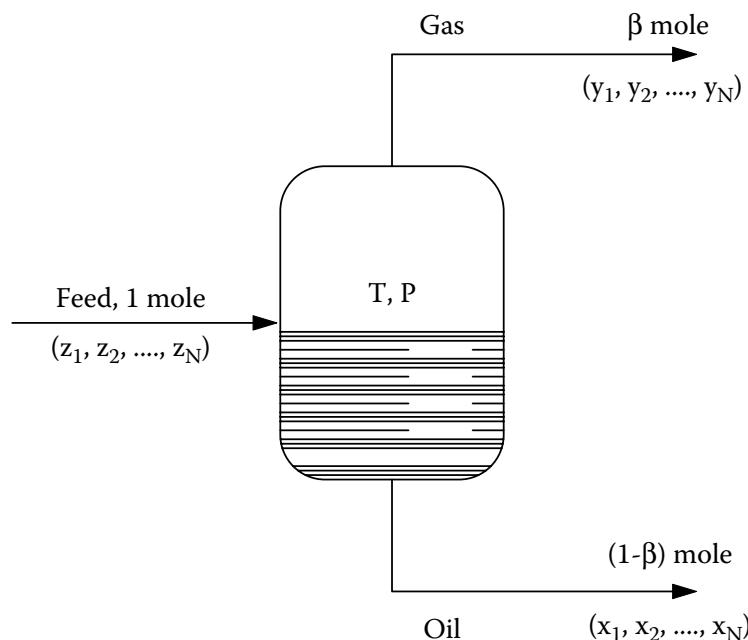
## Three-Phase System for Enhanced Oil Recovery: Phase Equilibria



Source: Pedersen, K. S., and P. L. Christensen. 2007. *Phase Behavior of Petroleum Reservoir Fluids*. CRC Taylor & Francis, New York.



## Three-Phase System for Enhanced Oil Recovery: Michelsen Reference



Source: Pedersen, K. S., and P. L. Christensen. 2007. *Phase Behavior of Petroleum Reservoir Fluids*. CRC Taylor & Francis, New York.



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Volume 16, Supplement 1, May 1992, Pages S19-S29



Phase equilibrium calculations. What is easy and what is difficult?

Michael L. Michelsen

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### Abstract

Calculation of phase equilibrium for a mixture of given composition requires specification of two process variables, typically chosen among the following: Temperature, pressure, vapour fraction, enthalpy, entropy or volume. The difficulties associated with solving the equilibrium equations are strongly related to the chosen selection of these process variables. The aim of the present paper is to outline the characteristics associated with the different types of specification in order to provide guidelines for efficient and robust solution algorithms.



## Three-Phase System for Enhanced Oil Recovery: Phase Conditions and Primary Variables

- State #1 (aqueous saturated)

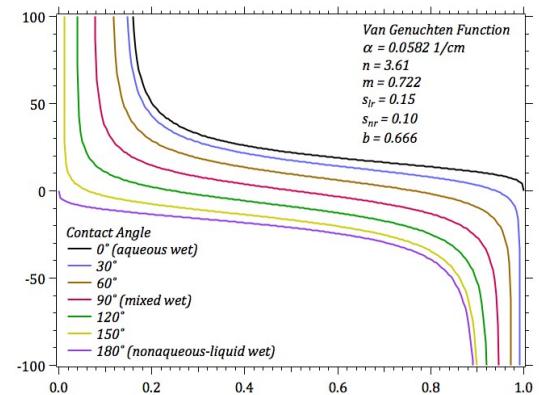
$$T, P_I, \omega_I^{CO_2}, m^{CH_4}, m^i, \omega_I^{salt} \text{ for } i = 3, n$$

- State #2 (aqueous + nonaqueous)

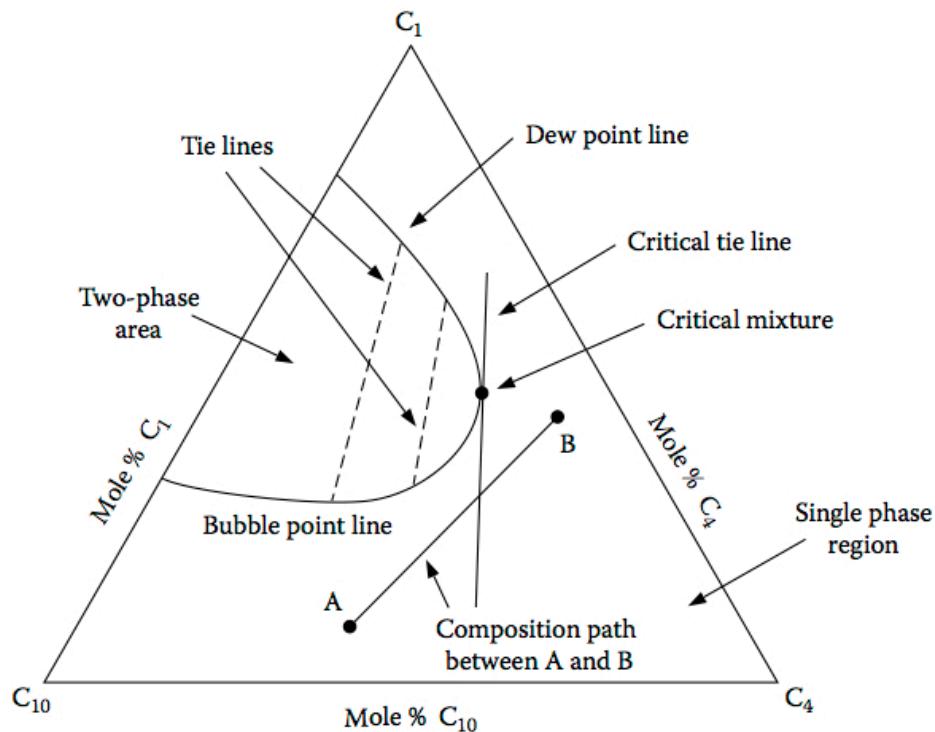
$$T, P_I, P_{ng}, \chi_t^{CO_2}, \chi_t^{CH_4}, \chi_t^i, \omega_I^{salt} \text{ for } i = 3, n-1$$

- State #3 (nonaqueous saturated)

$$T, m^{water}, P_{ng}, \chi_t^{CO_2}, \chi_t^{CH_4}, \chi_t^i, m^{salt} \text{ for } i = 3, n-1$$



# Three-Phase System for Enhanced Oil Recovery – First Contact



Source: Pedersen, K. S., and P. L. Christensen. 2007. *Phase Behavior of Petroleum Reservoir Fluids*. CRC Taylor & Francis, New York.

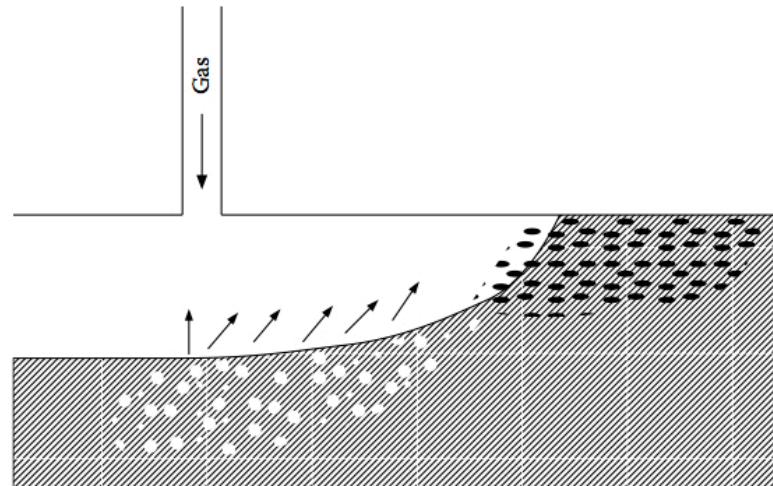
A – Composition of Oil

B – Composition of Gas

Fixed temperature & pressure



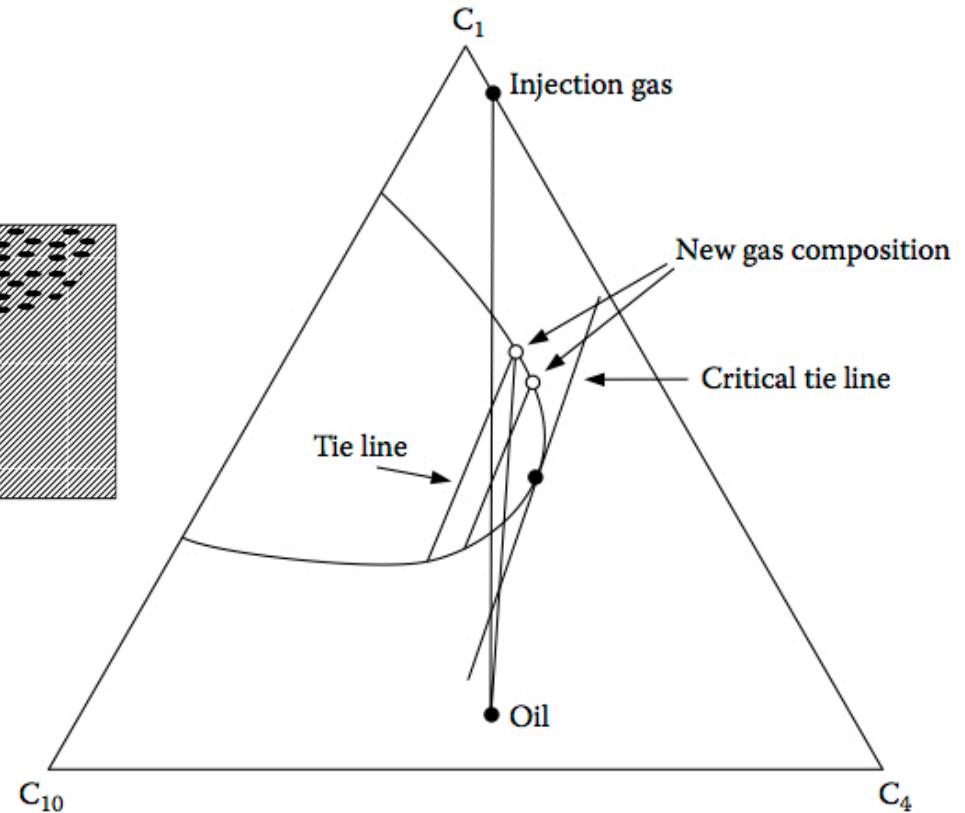
## Three-Phase System for Enhanced Oil Recovery – Vaporization Drive



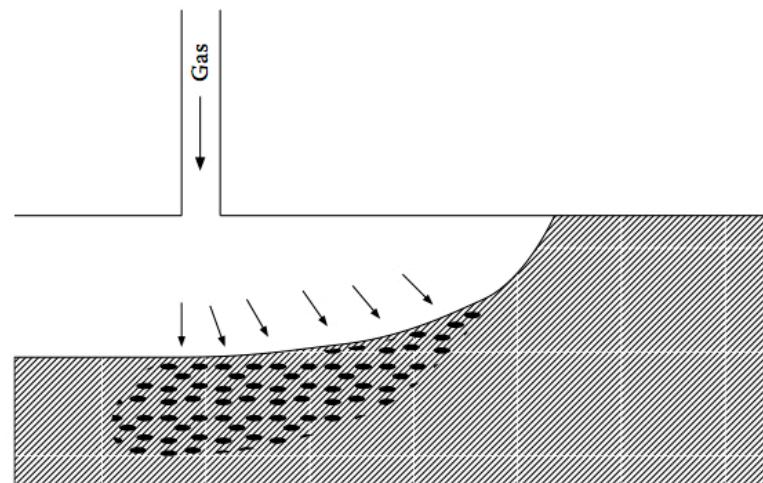
A – Composition of Oil

B – Composition of Gas

Fixed temperature & pressure



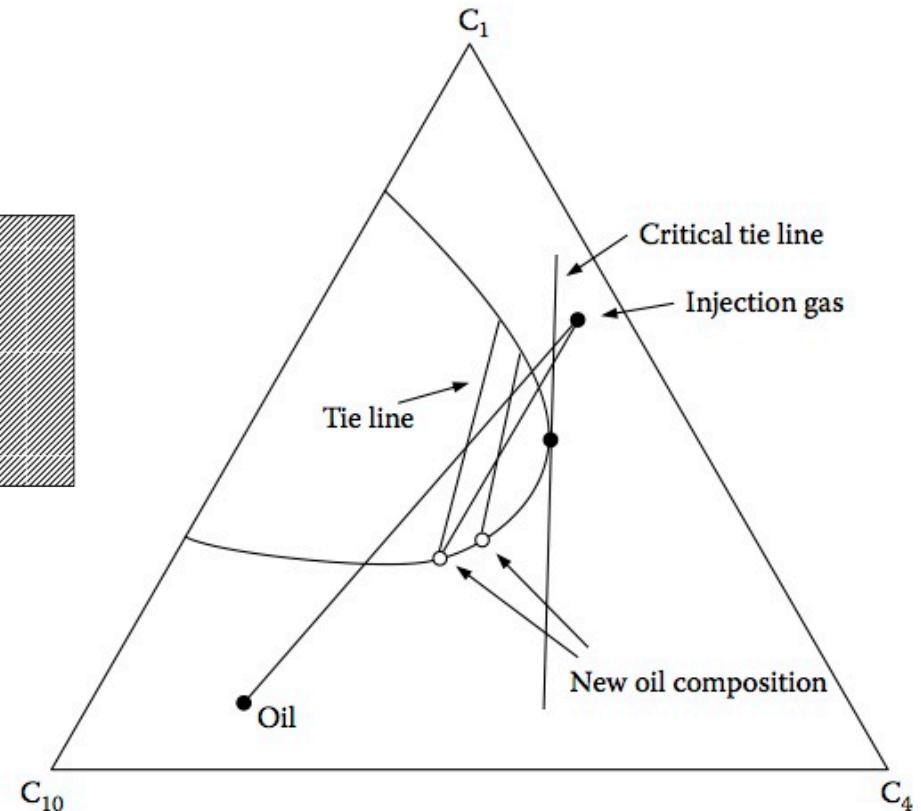
## Three-Phase System for Enhanced Oil Recovery – Condensing Drive



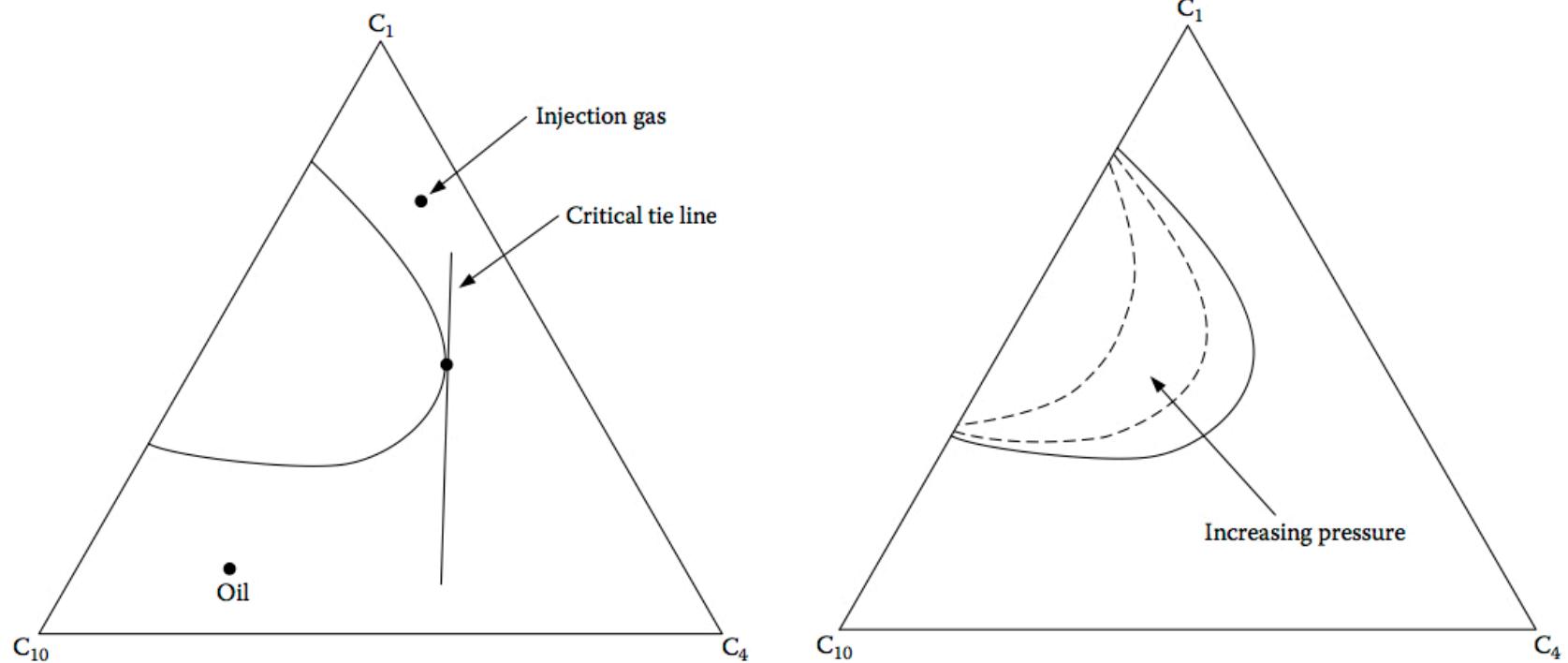
A – Composition of Oil

B – Composition of Gas

Fixed temperature & pressure



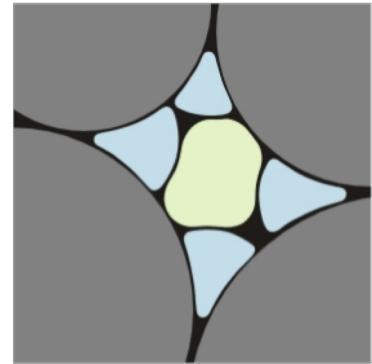
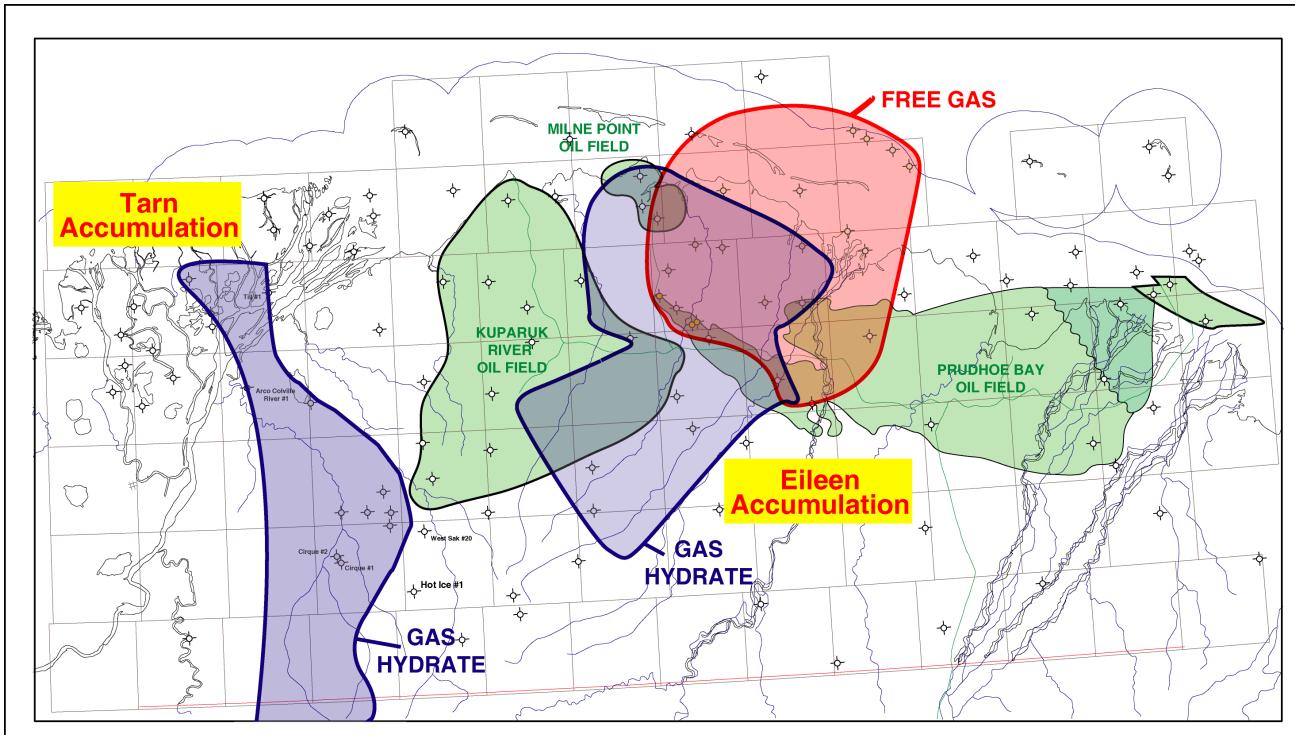
## Three-Phase System for Enhanced Oil Recovery – Miscibility & Pressure





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# Gas Hydrate Systems

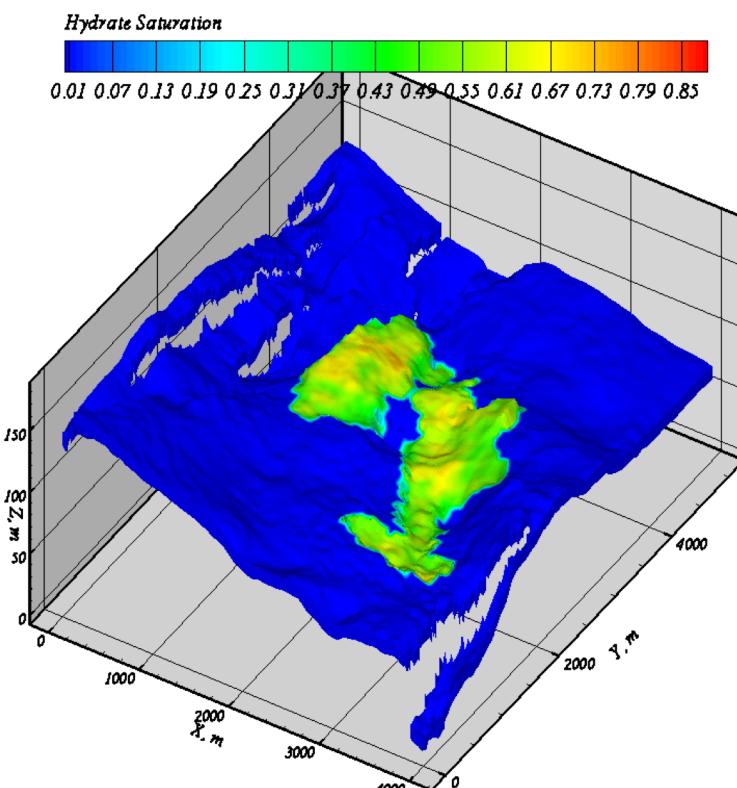
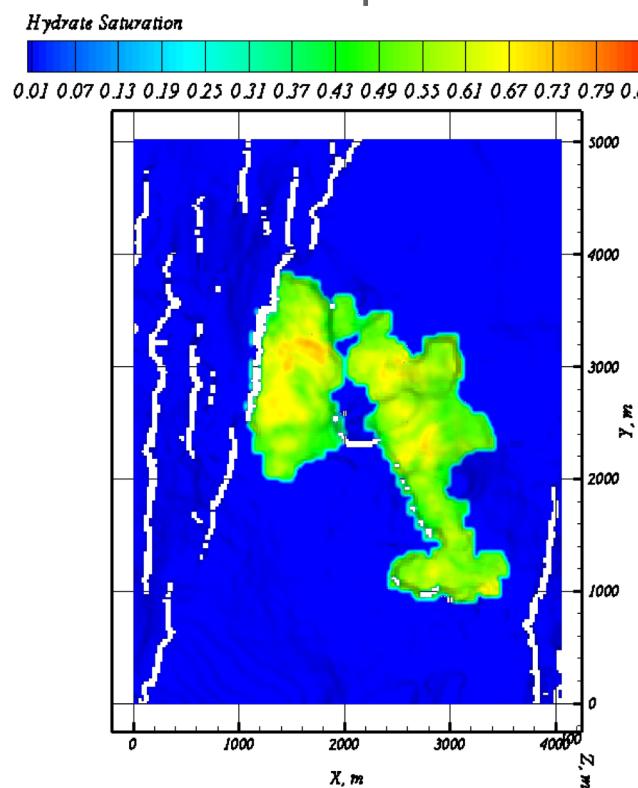


Gas Hydrate      Grain  
Gas                      Aqueous



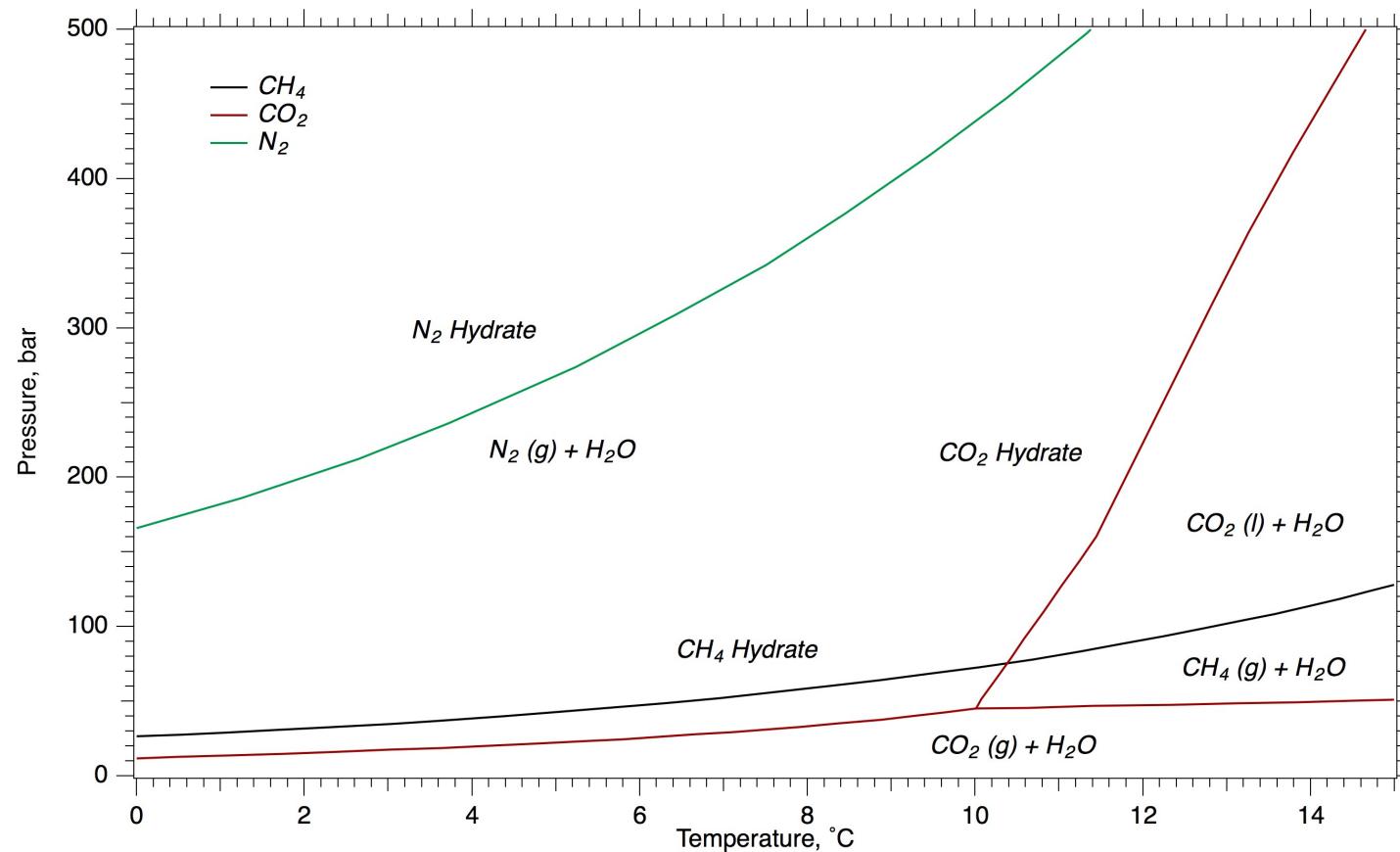


## Gas Hydrate Systems: Hydrate Distributions on the Alaska Northslope



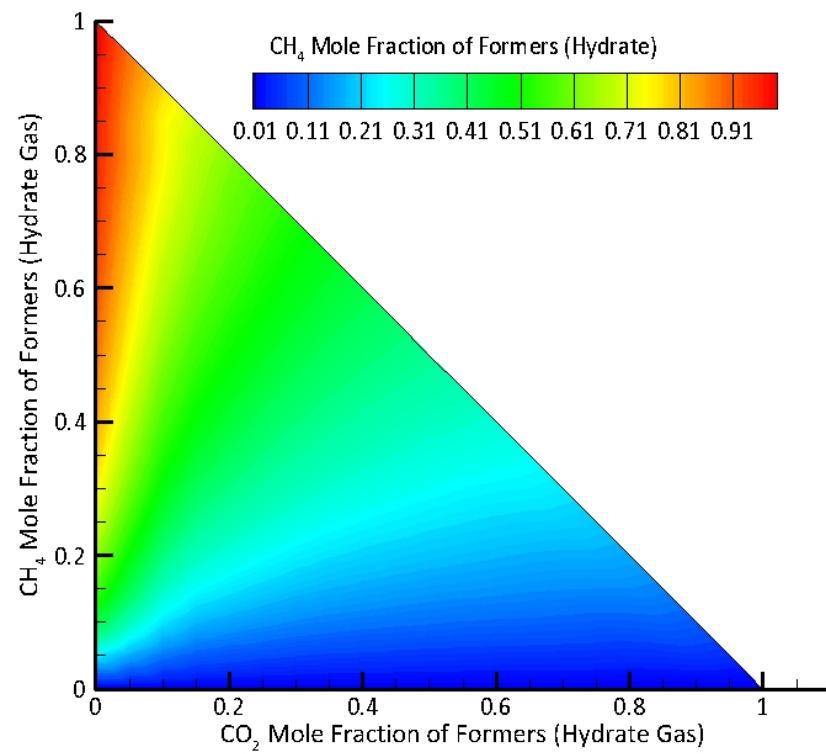
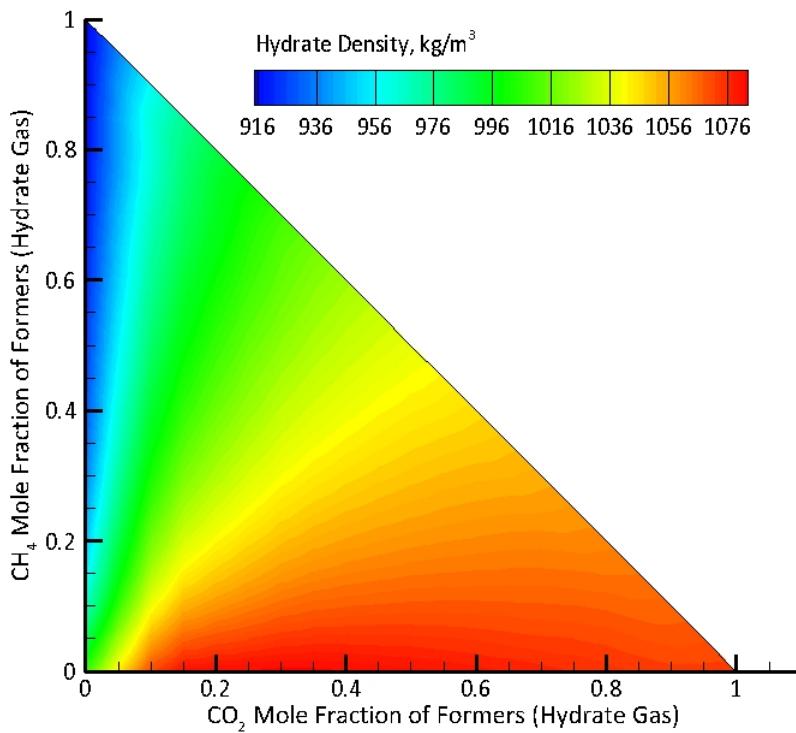


# Gas Hydrate Systems – Hydrate Phase Equilibria





## Gas Hydrate Systems – Ternary Hydrate Properties from Tables





## Gas Hydrate Systems – Phase Conditions and Primary Variables



Phase Condition #10 Series  $s_h = 0.0, s_n + s_g = 0.0, s_\ell + s_i = 1.0$

Energy	$T$	Temperature
Water Mass	$P$	Pressure
Mobile CO <sub>2</sub> Mass	$P_v^{CO_2}$	CO <sub>2</sub> Vapor Pressure
Mobile CH <sub>4</sub> Mass	$P_v^{CH_4}$	CH <sub>4</sub> Vapor Pressure
Mobile N <sub>2</sub> Mass	$P_v^{N_2}$	N <sub>2</sub> Vapor Pressure
Hydrate CO <sub>2</sub> Mass	$M_h^{CO_2}$	Hydrate CO <sub>2</sub> Mass
Hydrate CH <sub>4</sub> Mass	$M_h^{CH_4}$	Hydrate CO <sub>2</sub> Mass
Hydrate N <sub>2</sub> Mass	$M_h^{N_2}$	Hydrate CO <sub>2</sub> Mass
Salt	$y_\ell^s$	Brine Mass Fraction of Total Salt



## Gas Hydrate Systems – Phase Conditions and Primary Variables



Phase Condition #20 Series  $s_h = 0.0, s_n + s_g > 0.0, s_\ell + s_i < 1.0$

Energy	$T$	Temperature
Water Mass	$s_\ell + s_i$	Aqueous + Ice Saturation
Mobile CO <sub>2</sub> Mass	$z_m^{CO_2}$ or $P$	CO <sub>2</sub> Mole Fraction or Pressure
Mobile CH <sub>4</sub> Mass	$z_m^{CH_4}$ or $P$	CH <sub>4</sub> Mole Fraction or Pressure
Mobile N <sub>2</sub> Mass	$z_m^{N_2}$ or $P$	N <sub>2</sub> Mole Fraction or Pressure
Hydrate CO <sub>2</sub> Mass	$M_h^{CO_2}$	Hydrate CO <sub>2</sub> Mass
Hydrate CH <sub>4</sub> Mass	$M_h^{CH_4}$	Hydrate CO <sub>2</sub> Mass
Hydrate N <sub>2</sub> Mass	$M_h^{N_2}$	Hydrate CO <sub>2</sub> Mass
Salt	$y_\ell^s$	Brine Mass Fraction of Total Salt



## Gas Hydrate Systems – Phase Conditions and Primary Variables



Phase Condition #30 Series  $s_h > 0.0, s_n + s_g > 0.0, s_\ell + s_i < 1.0$

Energy	$T$	Temperature
Water Mass	$s_\ell + s_i$	Aqueous + Ice Saturation
Mobile CO <sub>2</sub> Mass	$z_m^{CO_2}$ or $P$	CO <sub>2</sub> Mole Fraction or Pressure
Mobile CH <sub>4</sub> Mass	$z_m^{CH_4}$ or $P$	CH <sub>4</sub> Mole Fraction or Pressure
Mobile N <sub>2</sub> Mass	$z_m^{N_2}$ or $P$	N <sub>2</sub> Mole Fraction or Pressure
Hydrate CO <sub>2</sub> Mass	$\psi_h^{CO_2}$ or $s_h$	CO <sub>2</sub> Mole Fraction of Former
Hydrate CH <sub>4</sub> Mass	$\psi_h^{CH_4}$ or $s_h$	CH <sub>4</sub> Mole Fraction of Former
Hydrate N <sub>2</sub> Mass	$\psi_h^{N_2}$ or $s_h$	N <sub>2</sub> Mole Fraction of Former
Salt	$y_\ell^s$	Brine Mass Fraction of Total Salt



## Gas Hydrate Systems – Phase Conditions and Primary Variables



Phase Condition #40 Series  $s_h > 0.0, s_n + s_g = 0.0, s_\ell + s_i < 1.0$

Energy	$T$	Temperature
Water Mass	$P$	Pressure
Mobile CO <sub>2</sub> Mass	$P_v^{CO_2}$	CO <sub>2</sub> Vapor Pressure
Mobile CH <sub>4</sub> Mass	$P_v^{CH_4}$	CH <sub>4</sub> Vapor Pressure
Mobile N <sub>2</sub> Mass	$P_v^{N_2}$	N <sub>2</sub> Vapor Pressure
Hydrate CO <sub>2</sub> Mass	$\psi_h^{CO_2}$ or $s_h$	CO <sub>2</sub> Mole Fraction of Former
Hydrate CH <sub>4</sub> Mass	$\psi_h^{CH_4}$ or $s_h$	CH <sub>4</sub> Mole Fraction of Former
Hydrate N <sub>2</sub> Mass	$\psi_h^{N_2}$ or $s_h$	N <sub>2</sub> Mole Fraction of Former
Salt	$y_\ell^s$	Brine Mass Fraction of Total Salt



## Gas Hydrate Systems – Phase Transitions



Phase Condition #10 Series  $s_h = 0.0, s_n + s_g = 0.0, s_\ell + s_i = 1.0$

- Assume a hydrate phase exists (common approach!)
- Compute a hydrate equilibrium pressure  $P_h^{eq} = \text{func}[T, \psi_h^{CO_2}, \psi_h^{CH_4}, \psi_h^{N_2}]$
- Compute the vapor pressure of formers  $P_v = P_v^{CO_2} + P_v^{CH_4} + P_v^{N_2}$
- Compute the total gas pressure  $P_g = P_v^{CO_2} + P_v^{CH_4} + P_v^{N_2} + P_v^{H_2O}$
- *if*  $(P_v > P_h^{eq})$  *then* hydrate forms
- *if*  $(P_g > P_\ell + P_{entry})$  *then* hydrate forms

Phase Condition #30 Series  $s_h > 0.0, s_n + s_g > 0.0, s_\ell + s_i < 1.0$



## Takeaways / Conclusions

- Primary variable switching is an effective scheme for modeling phase transitions
- Select primary variables that yield direct calculations of all secondary variables
- Phase equilibria calculations are harder than they appear
- Discontinuities slow convergence
- Be creative in defining primary variables and phase conditions





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Thank you

