



Phase Transitions in Porous Media

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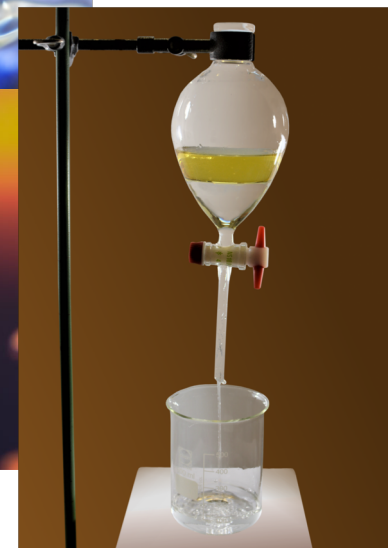
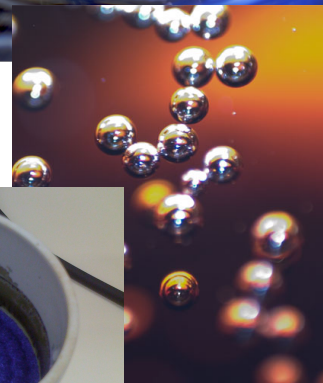


Components

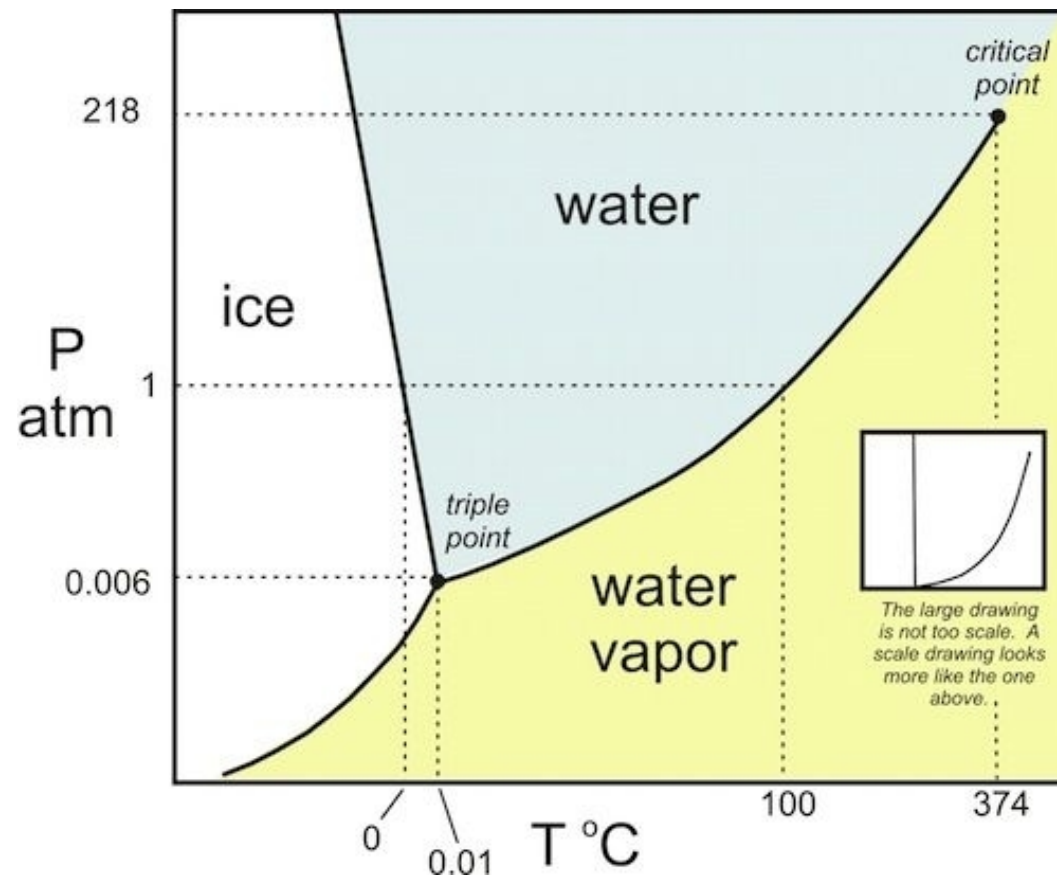
- Water
- Carbon Dioxide
- Methane
- Salt
- C7
- Nitrogen
- Oil

Phases

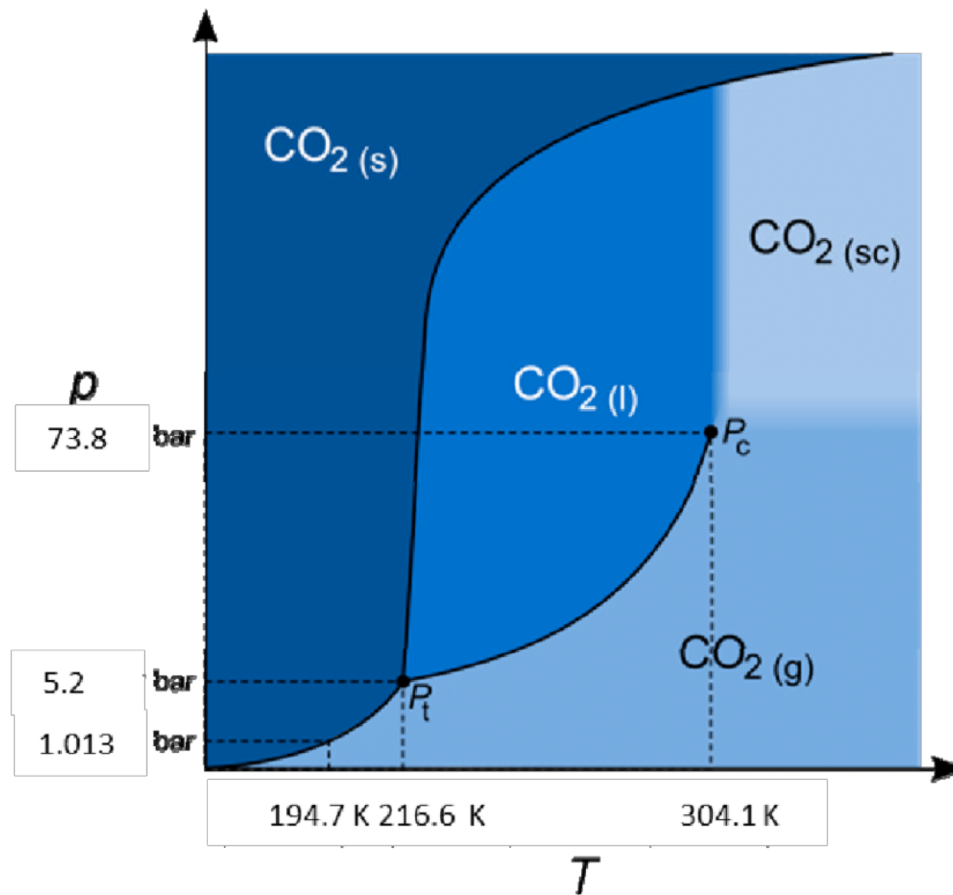
- Aqueous
- Gas
- Non-aqueous Liquid
- Hydrate
- Ice
- Precipitated Salt
- Minerals



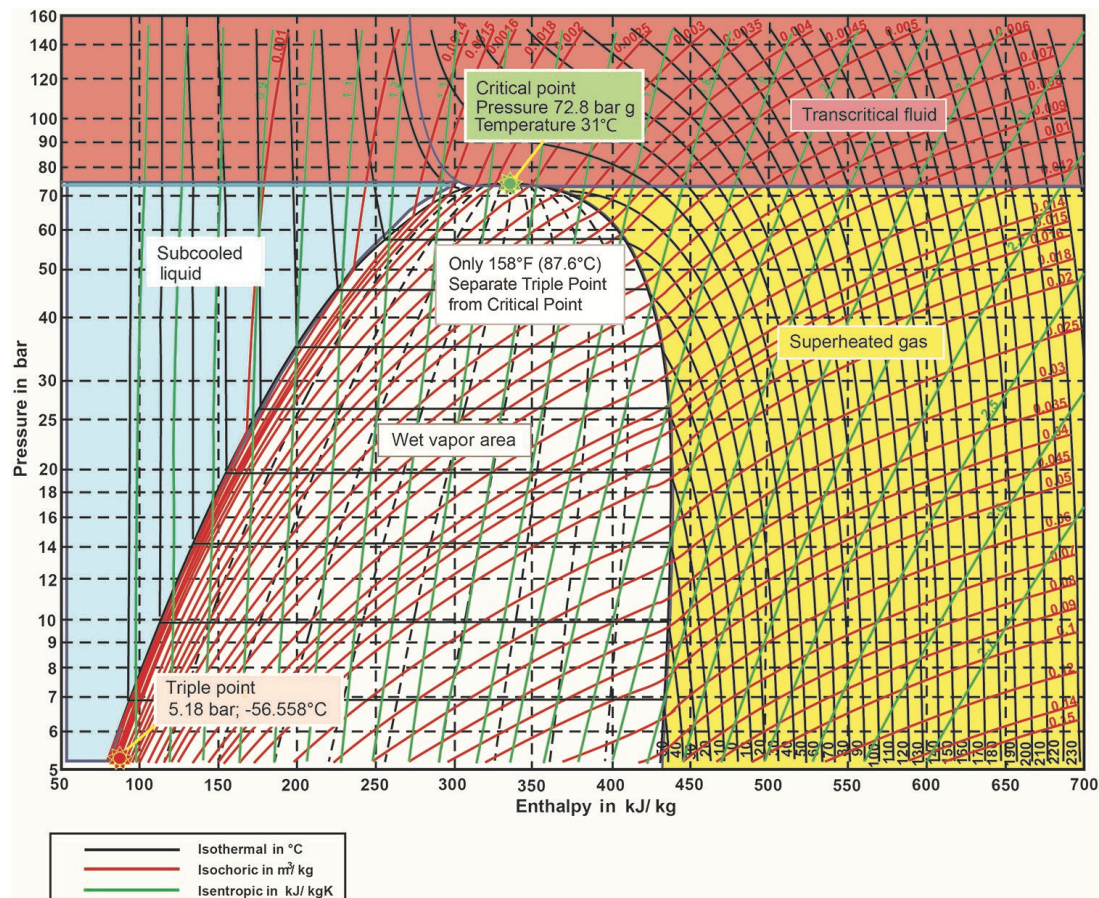
Pressure-Temperature Phase Diagram for Water



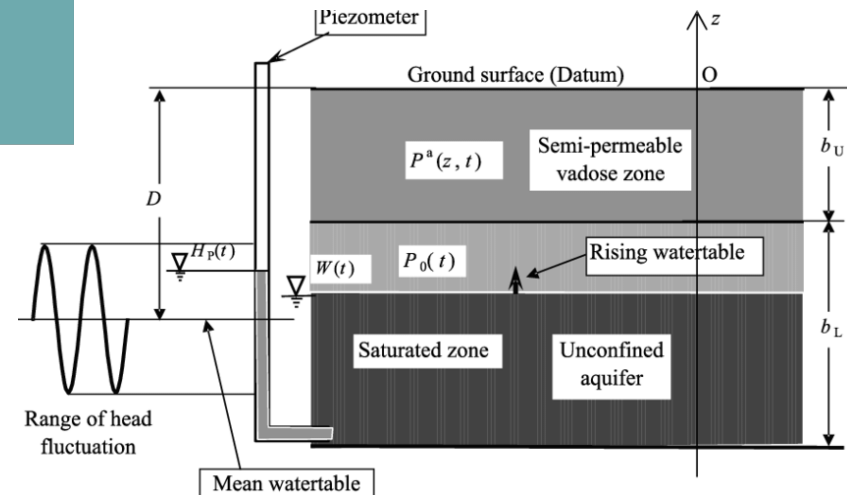
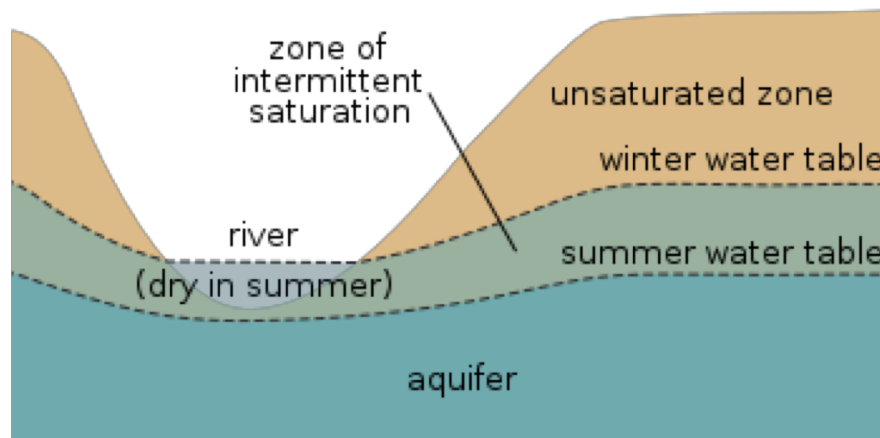
Pressure-Temperature Phase Diagram for CO₂



Pressure-Enthalpy Phase Diagram for CO₂



Phase Transitions: Fluctuating Water Table Examples



Modeling Scheme for Saturated to Unsaturated Phase Transitions

Fixed Variables

- Temperature (Isothermal)
- Gas Pressure (Passive Gas)

Primary Variable Options

- Aqueous Saturation
- Aqueous Pressure

Simple Relaxation Scheme

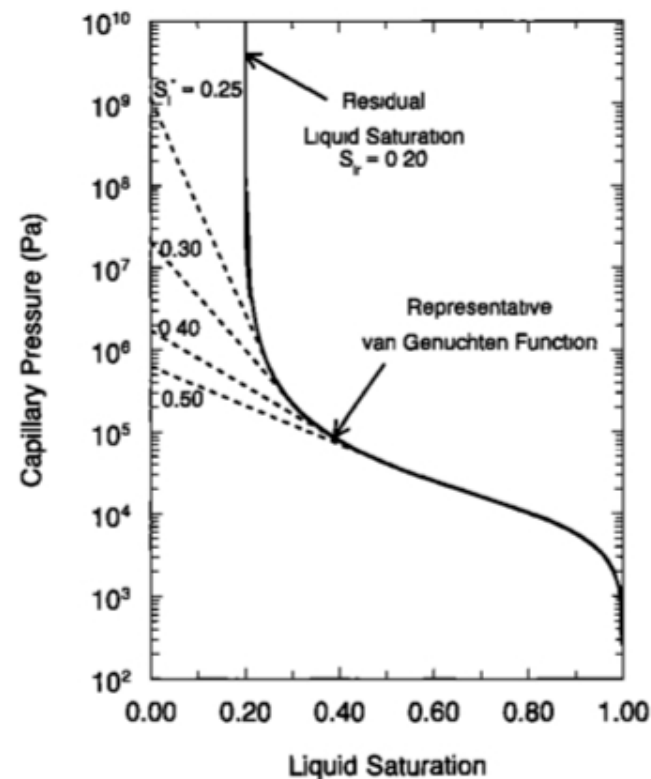
DPL – Update to Aqueous Pressure

PG(2,N) – Gas Pressure

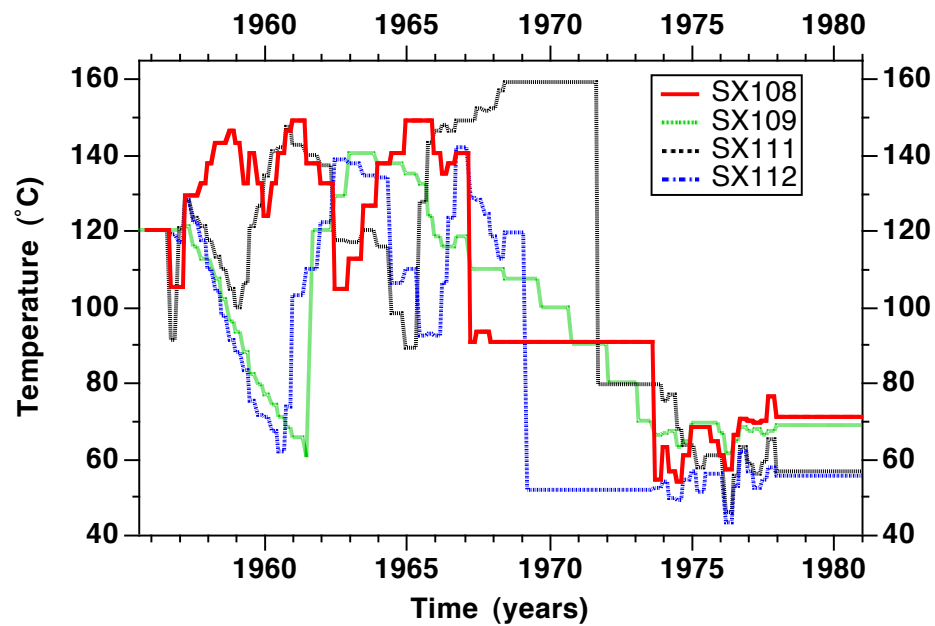
PL(2,N) – Aqueous Pressure

PAE – Air Entry Pressure

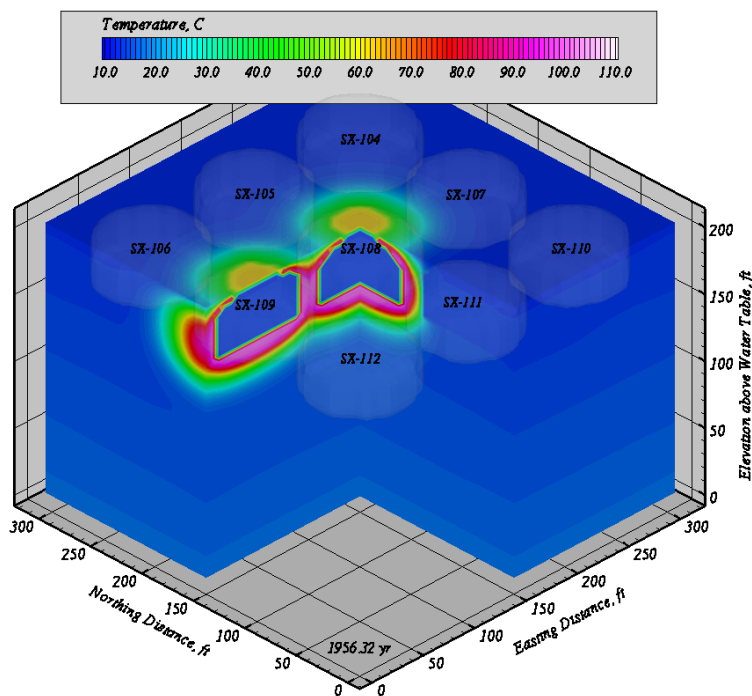
```
IF( PG(2,N)-PL(2,N)-PAE.GT.ZERO .AND.  
PG(2,N)-PL(2,N)-PAE-DPL.LT.ZERO ) DPL = 6.D-1*DPL  
PL(2,N) = PL(2,N) + DPL
```



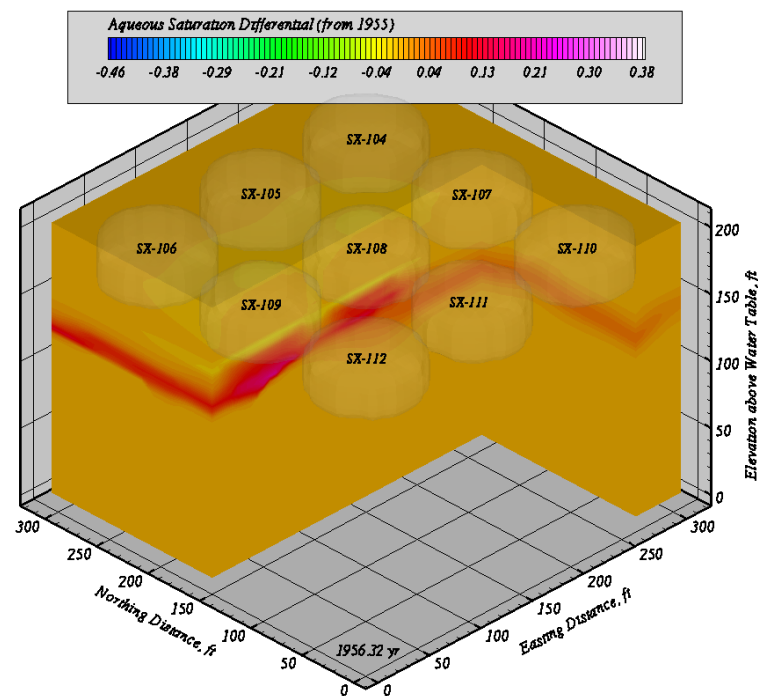
Low-Pressure Air-Water Systems: Example of Coupled Thermal and Hydraulic Environments



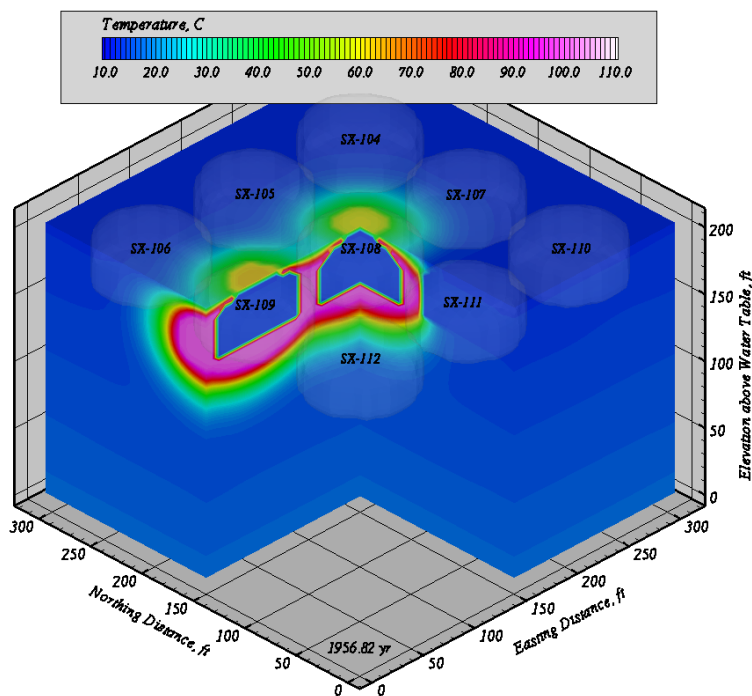
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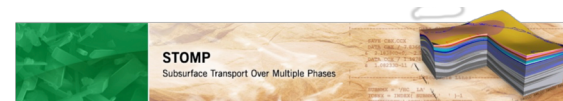
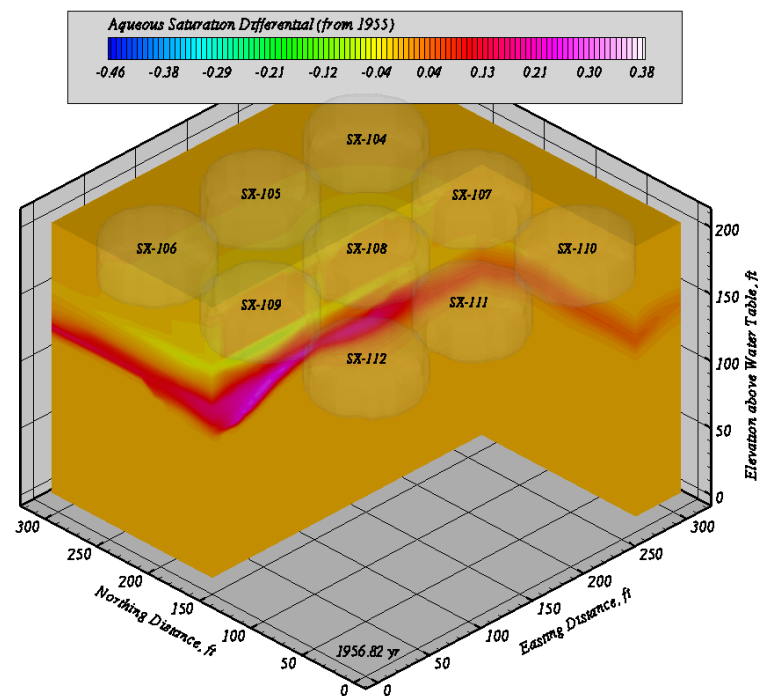
1956.32



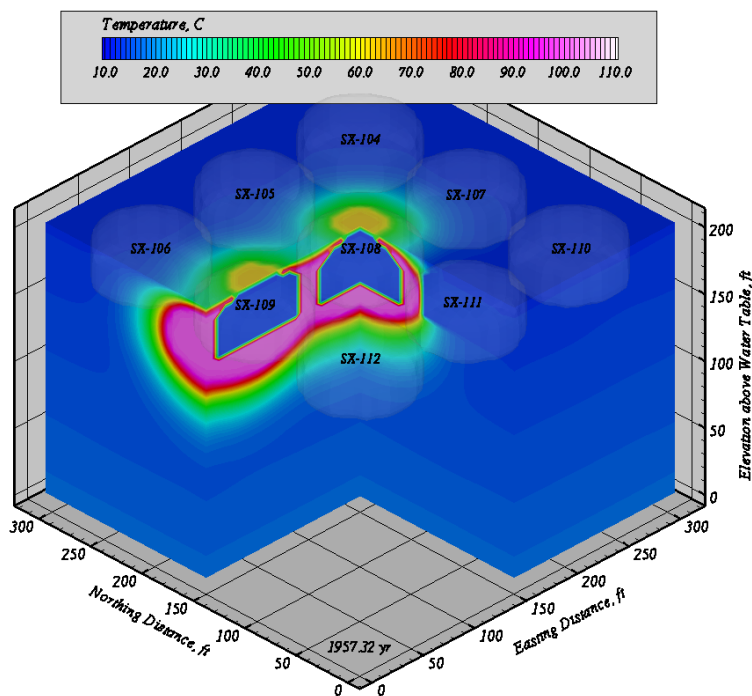
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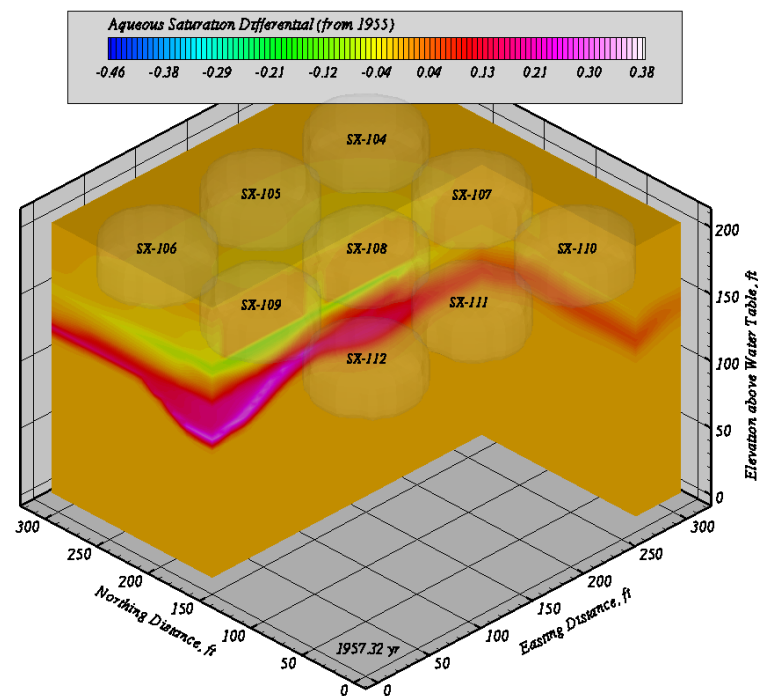
1956.82



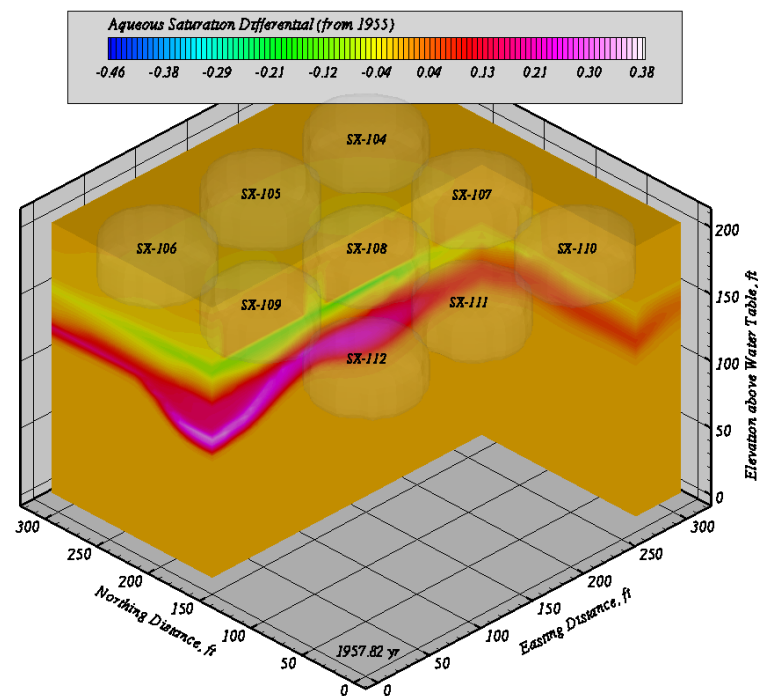
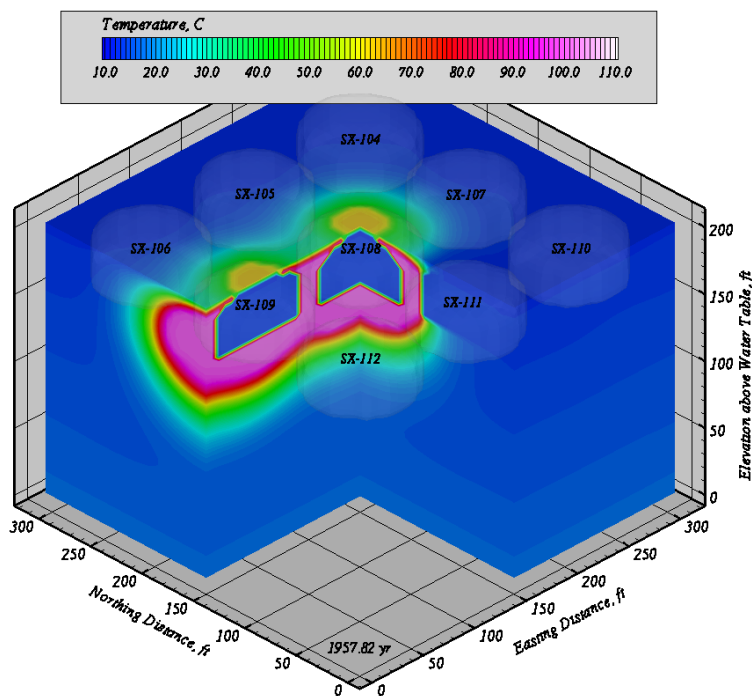
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1957.32



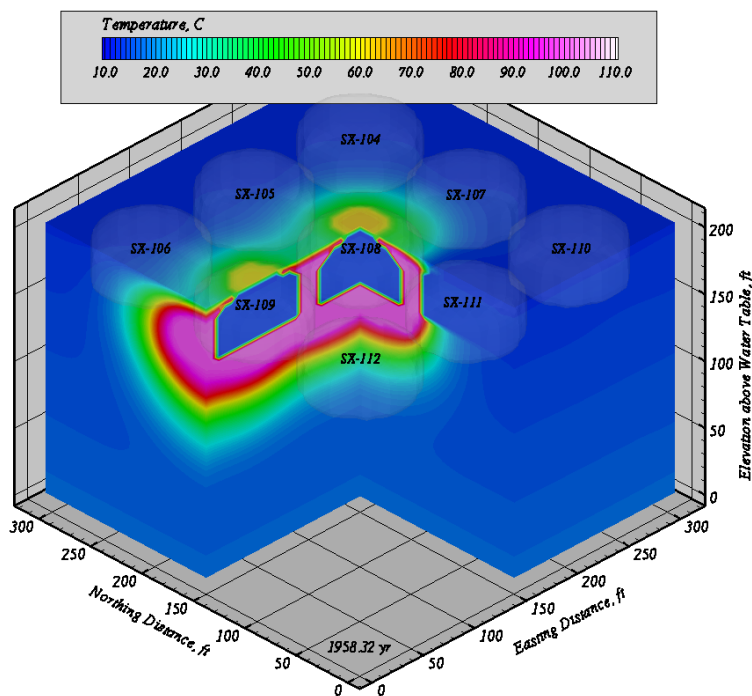
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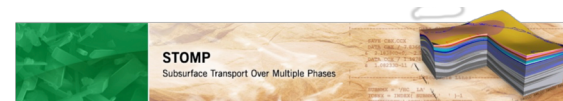
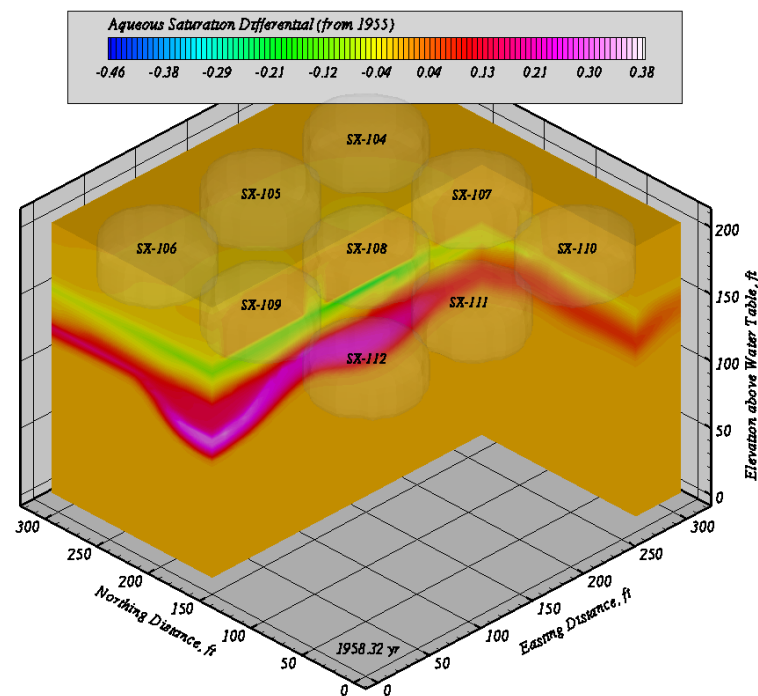
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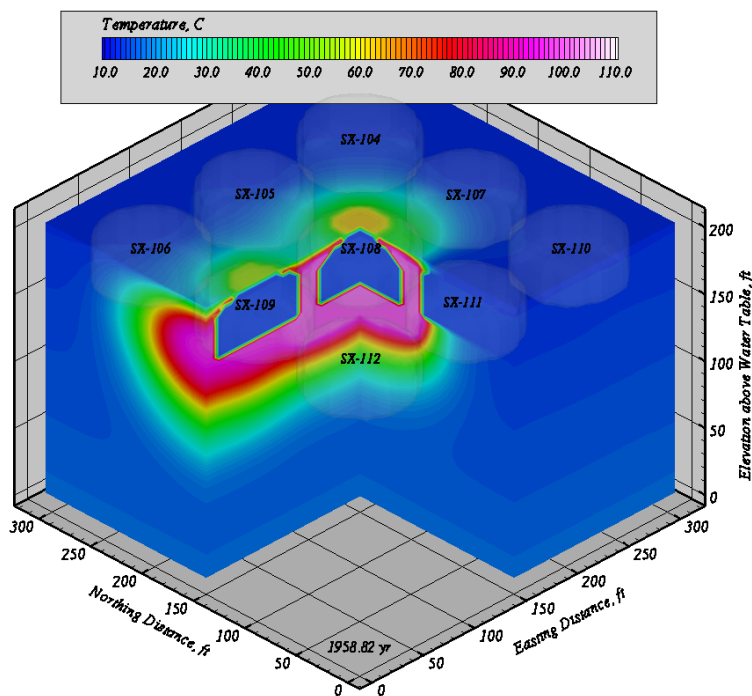
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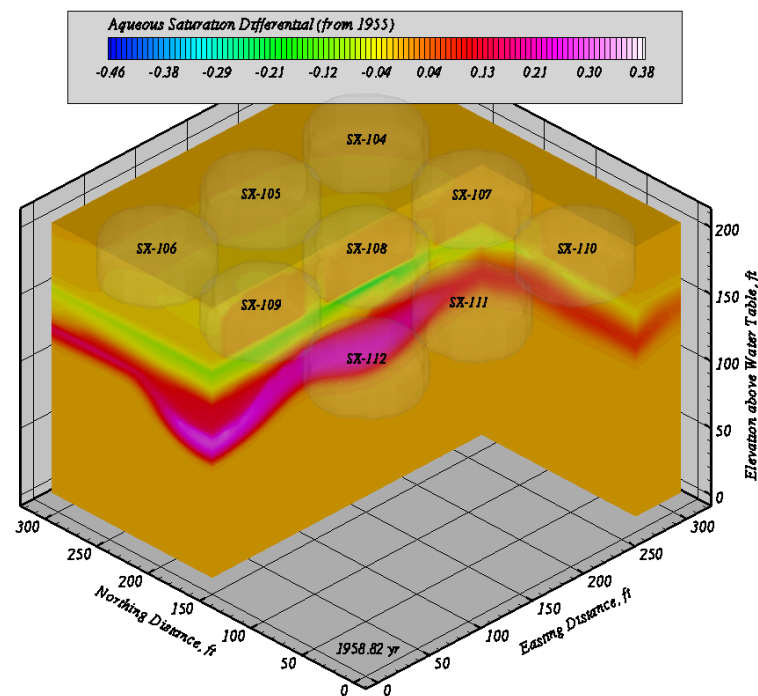
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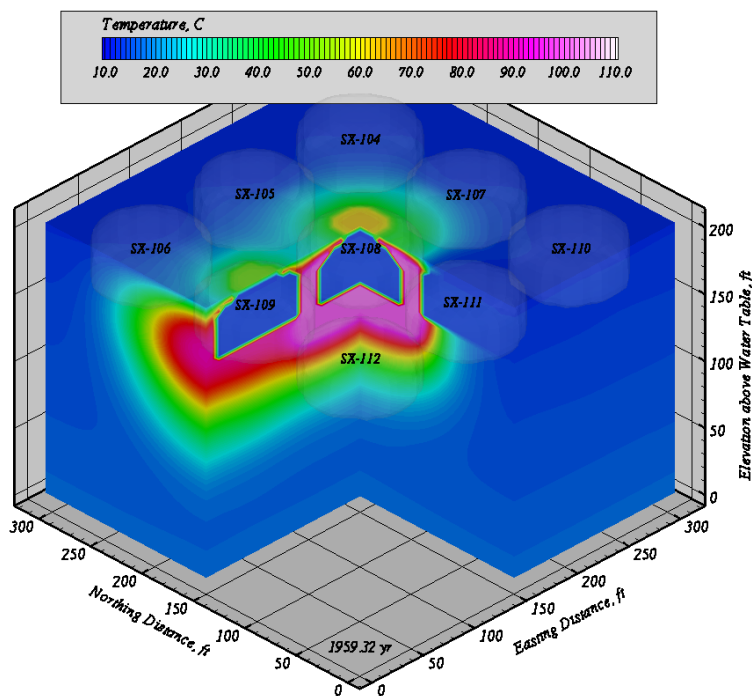
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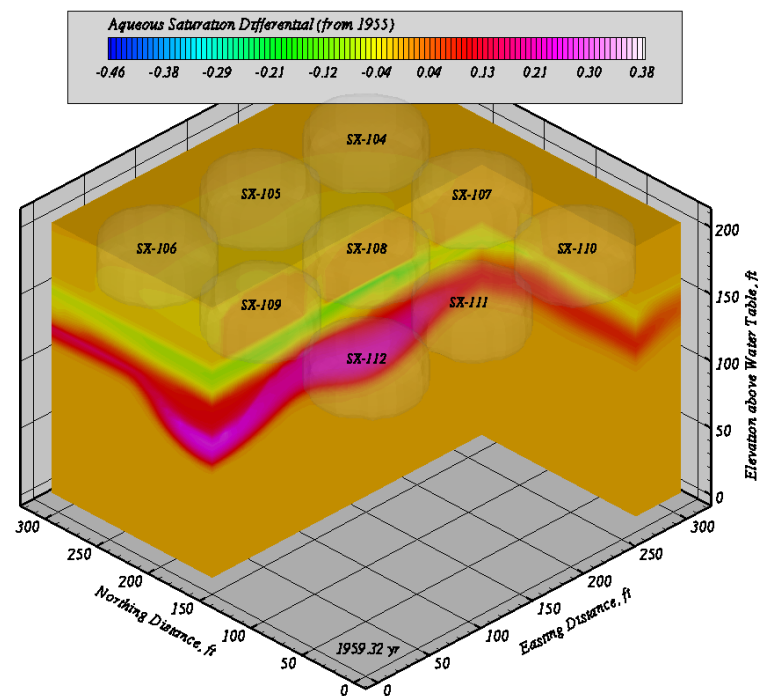
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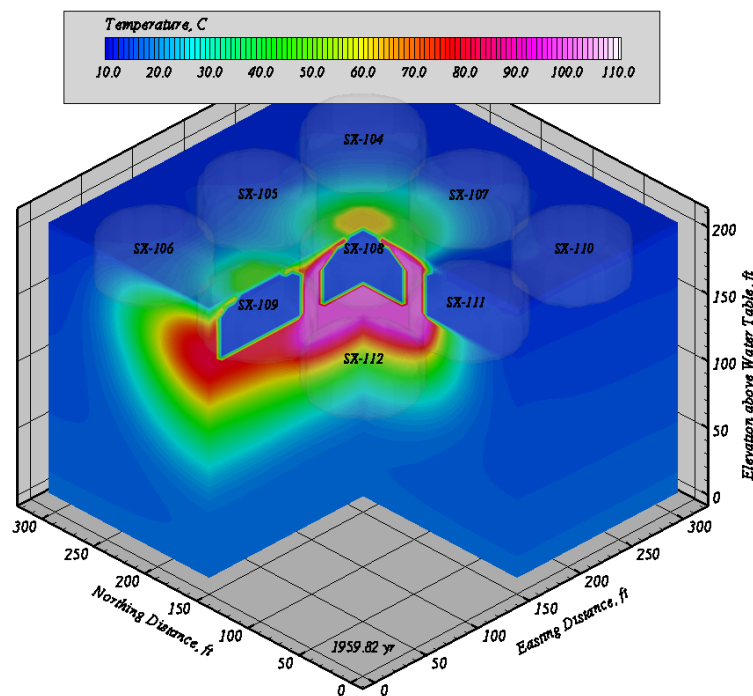
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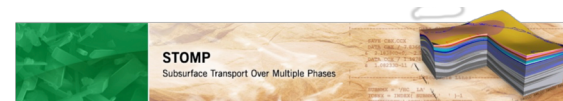
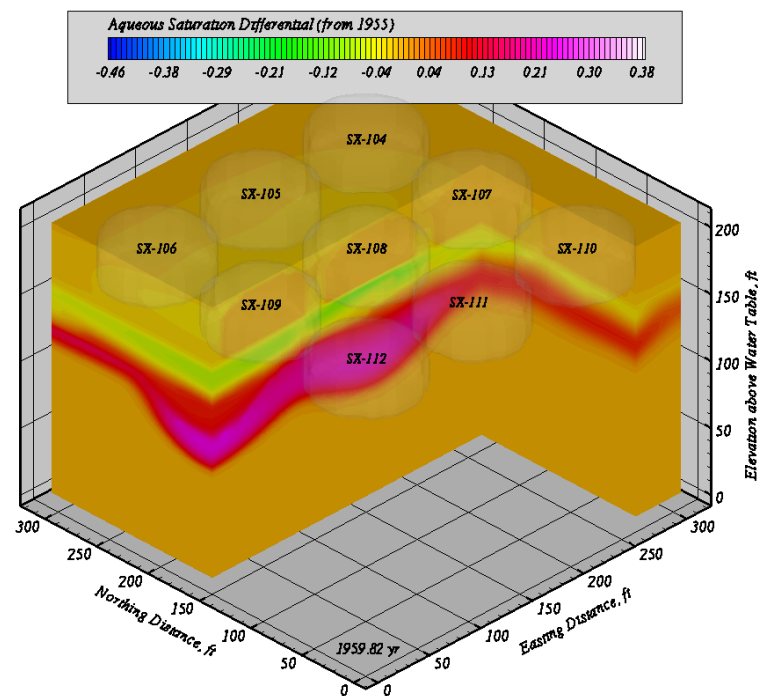
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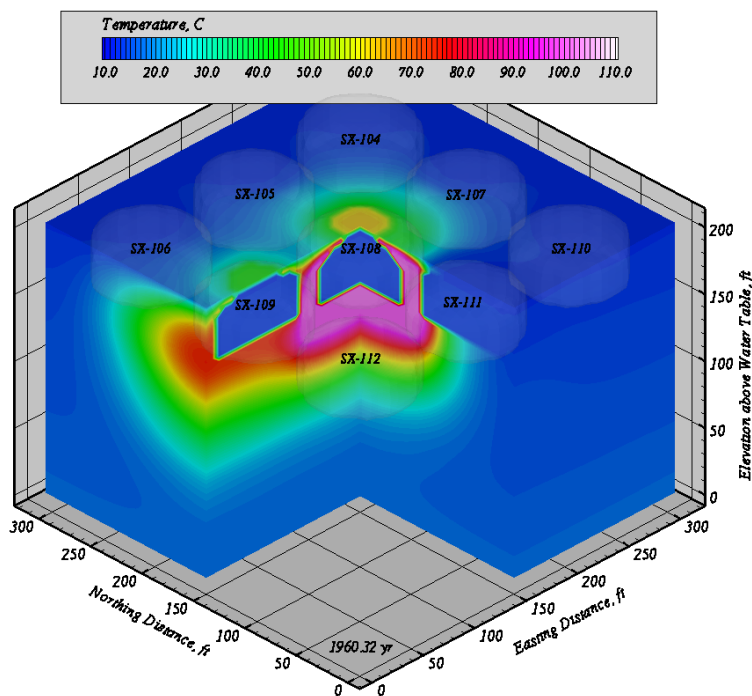
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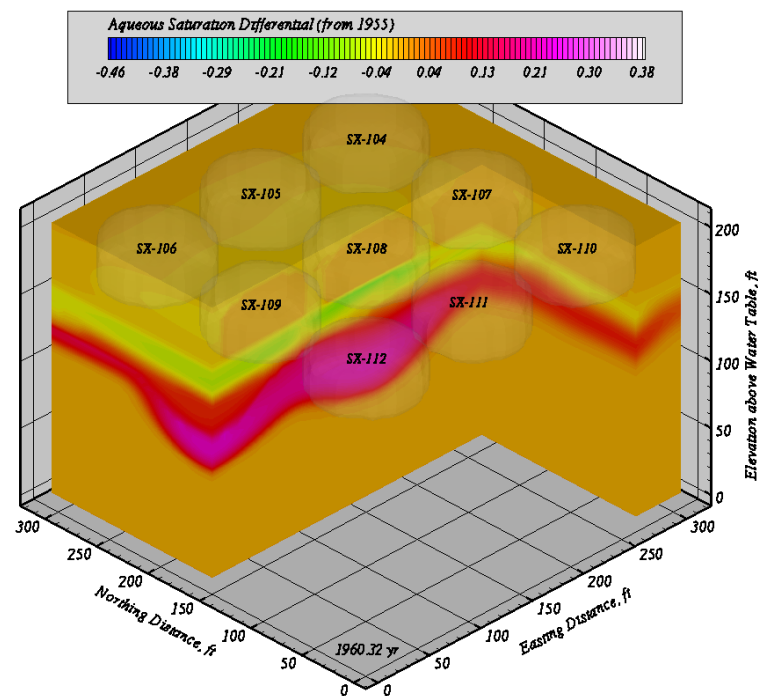
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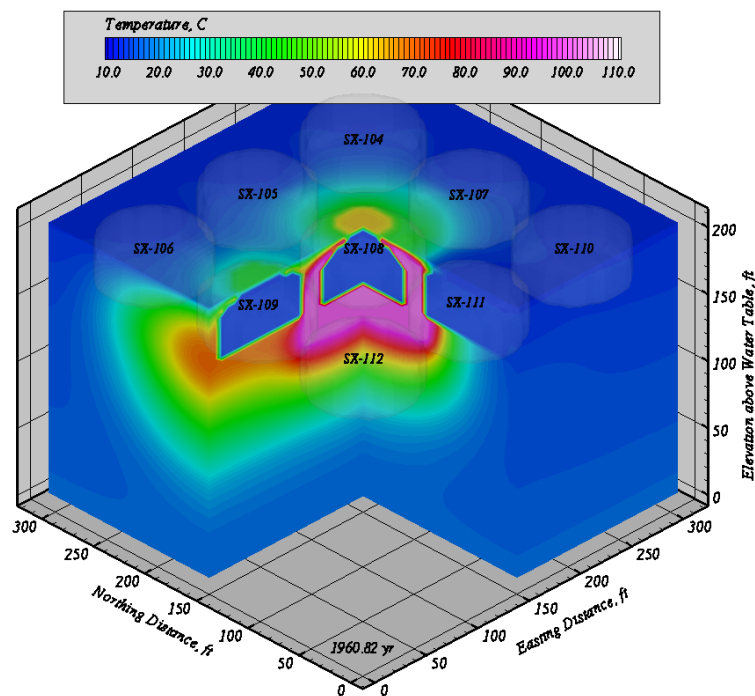
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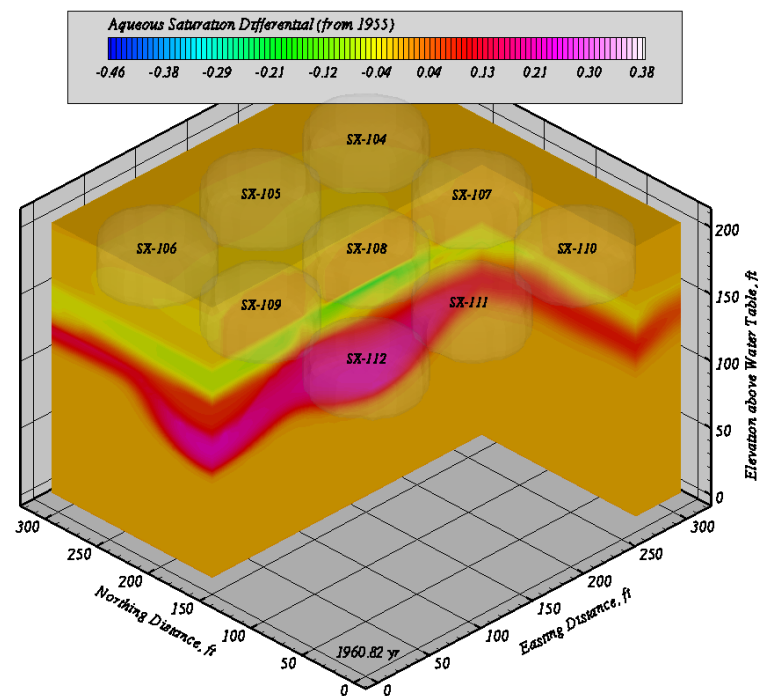
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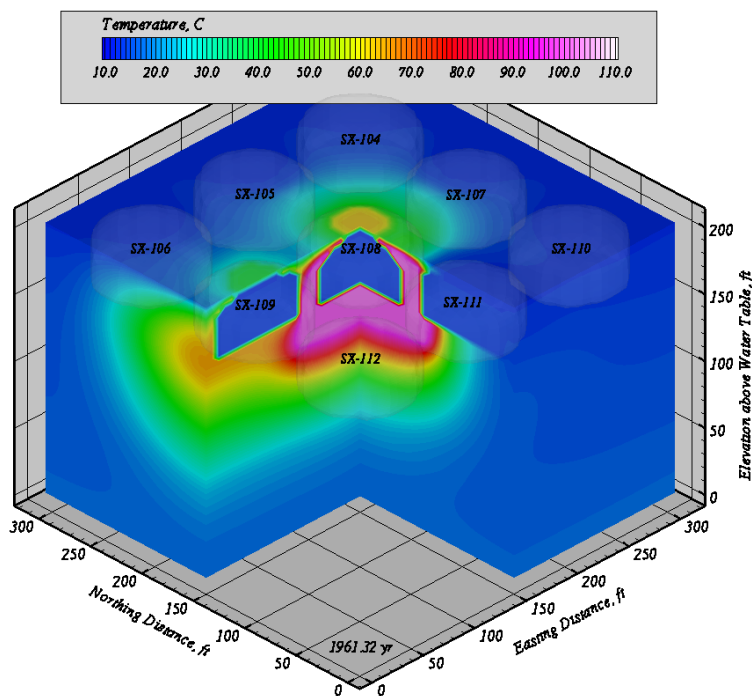
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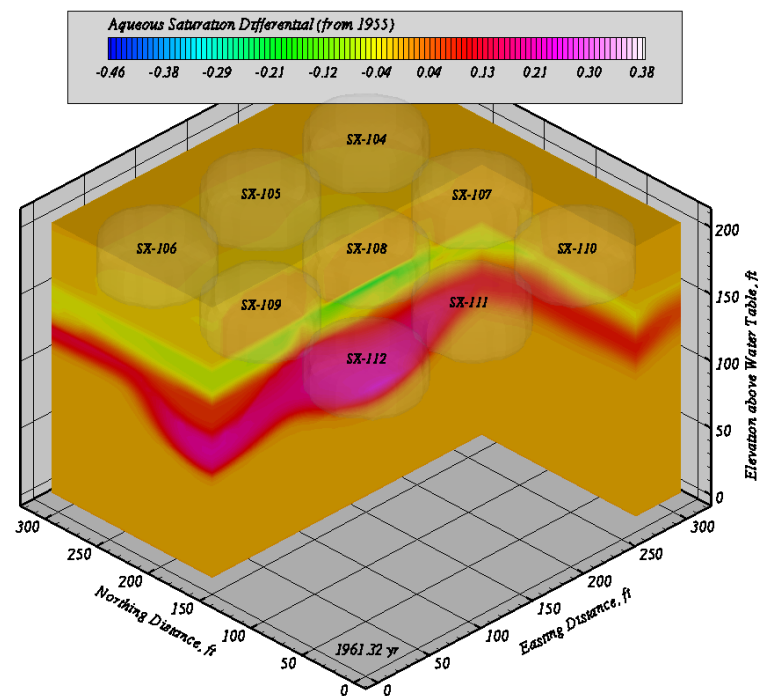
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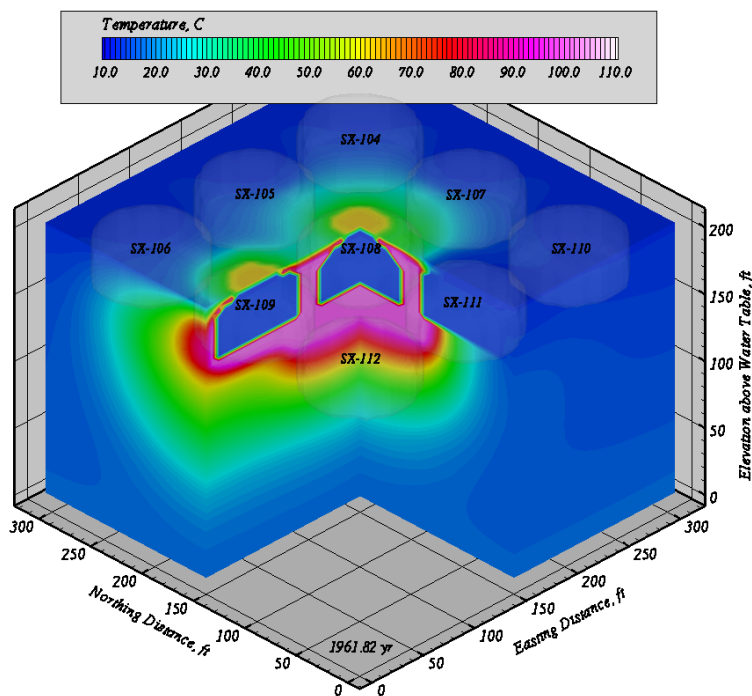
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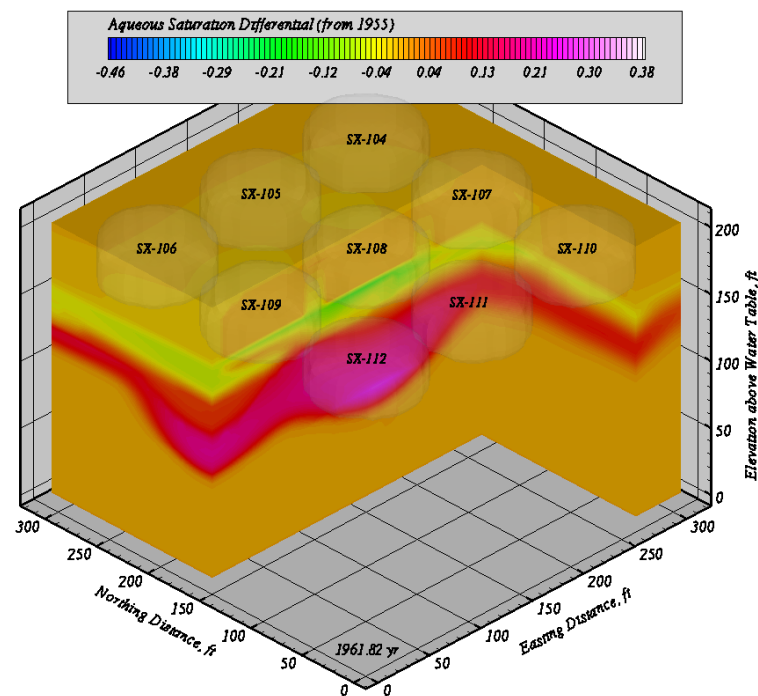
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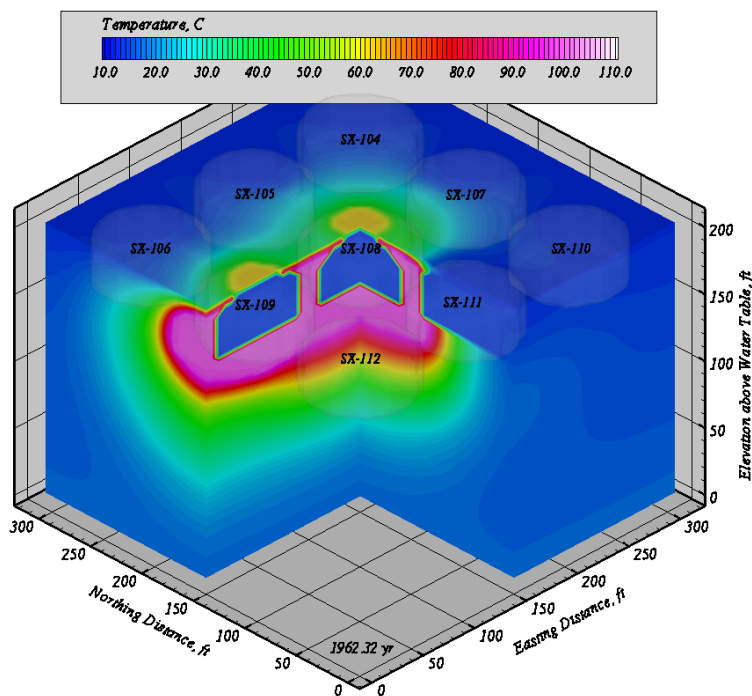
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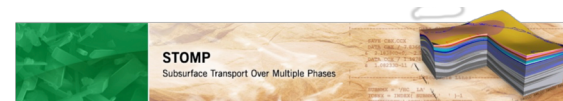
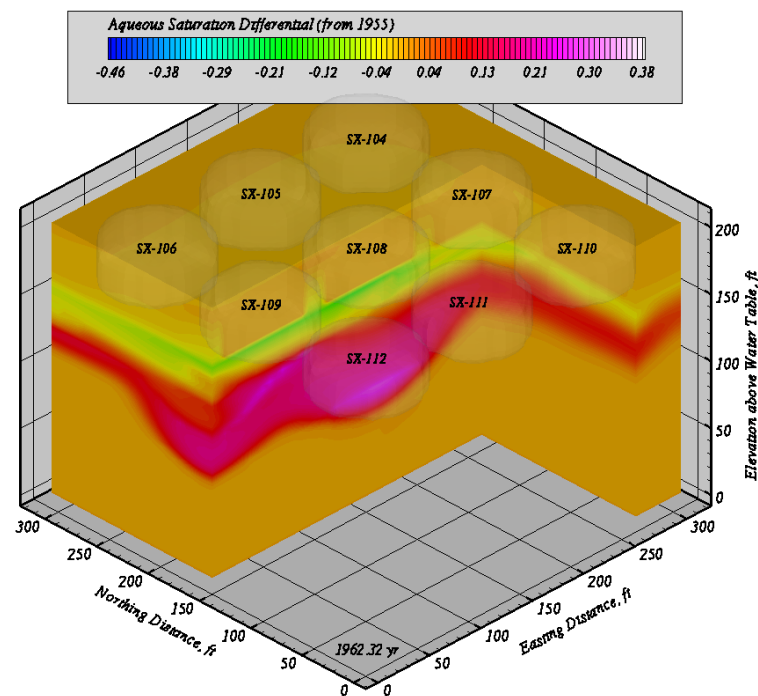
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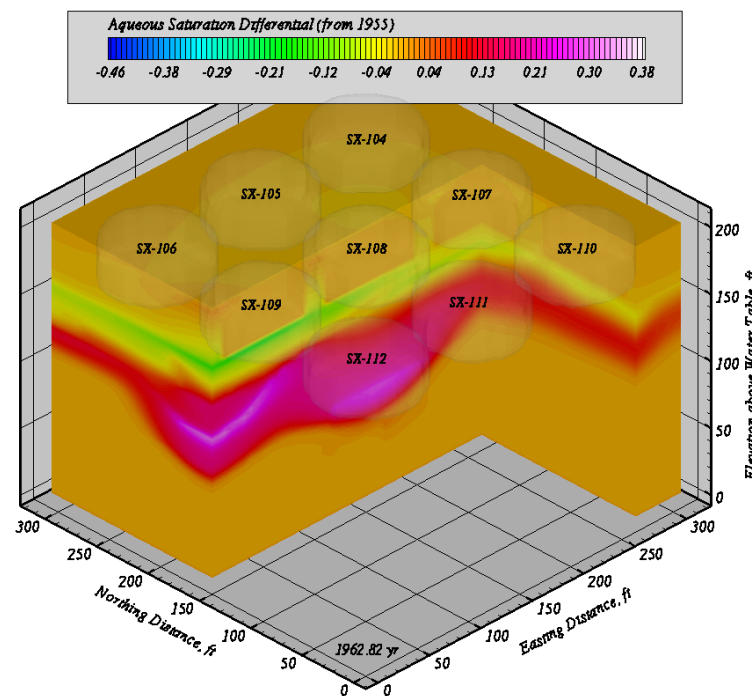
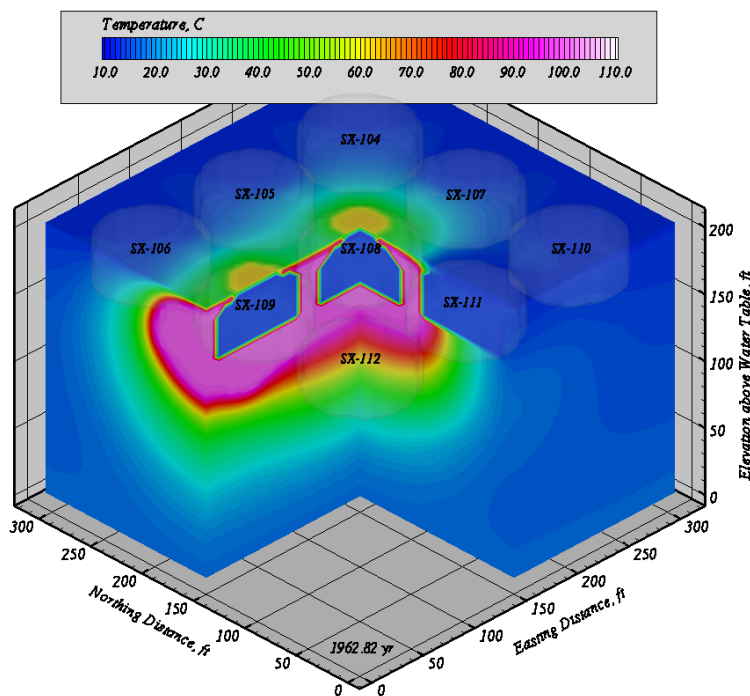
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1962.32



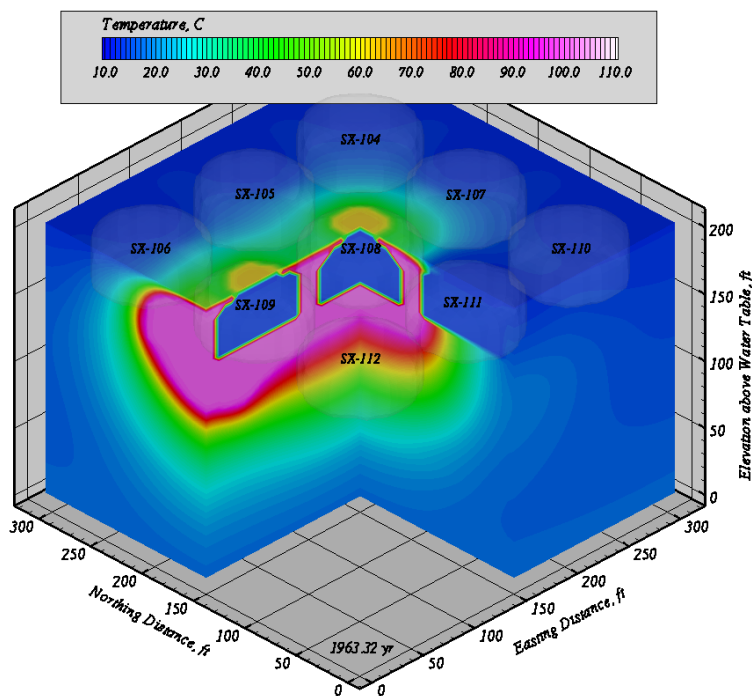
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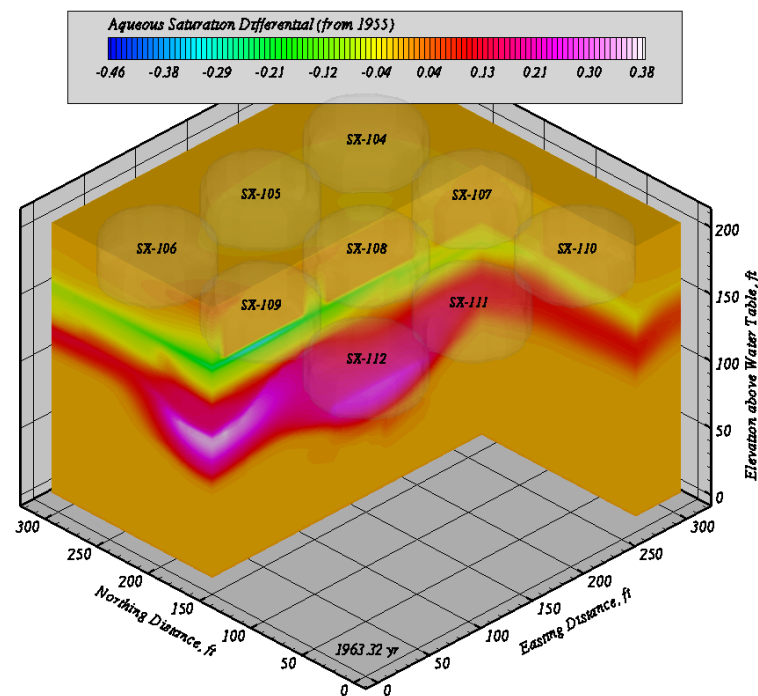
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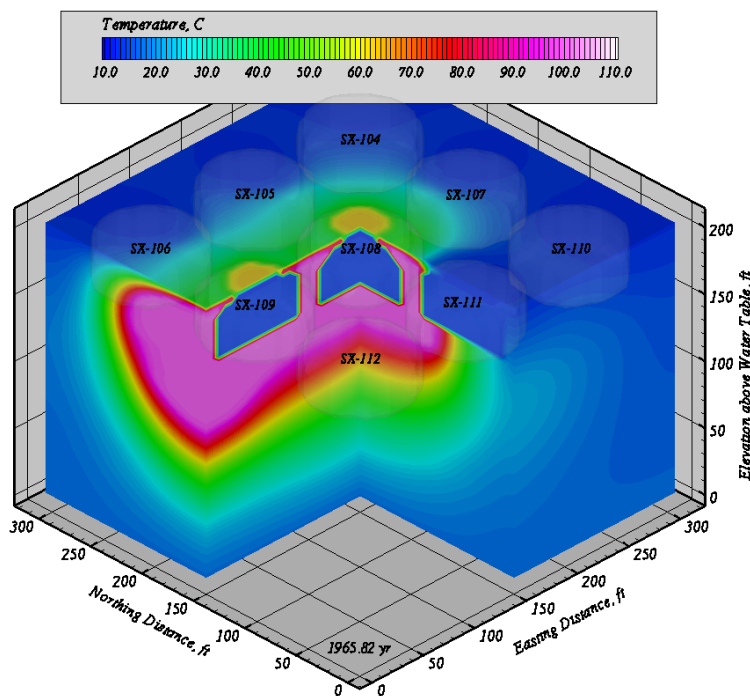
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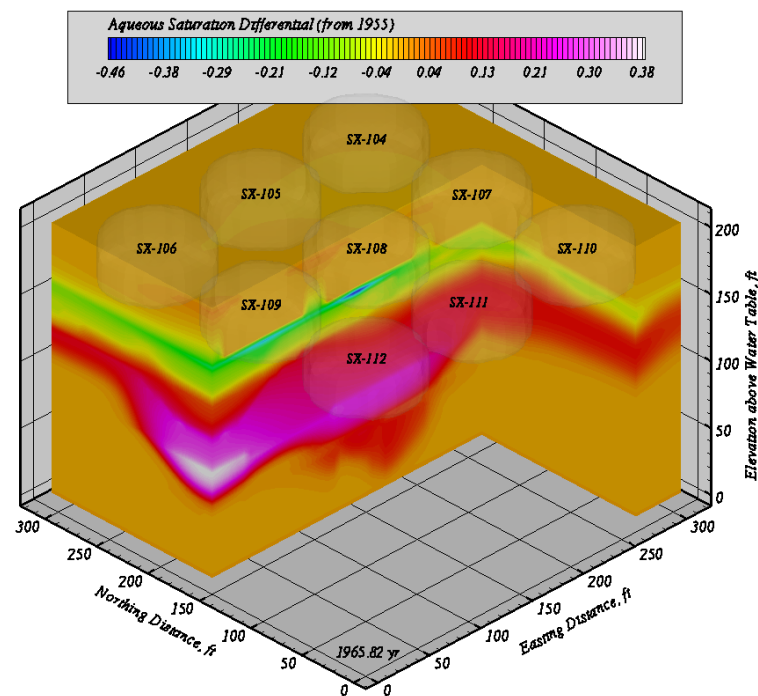
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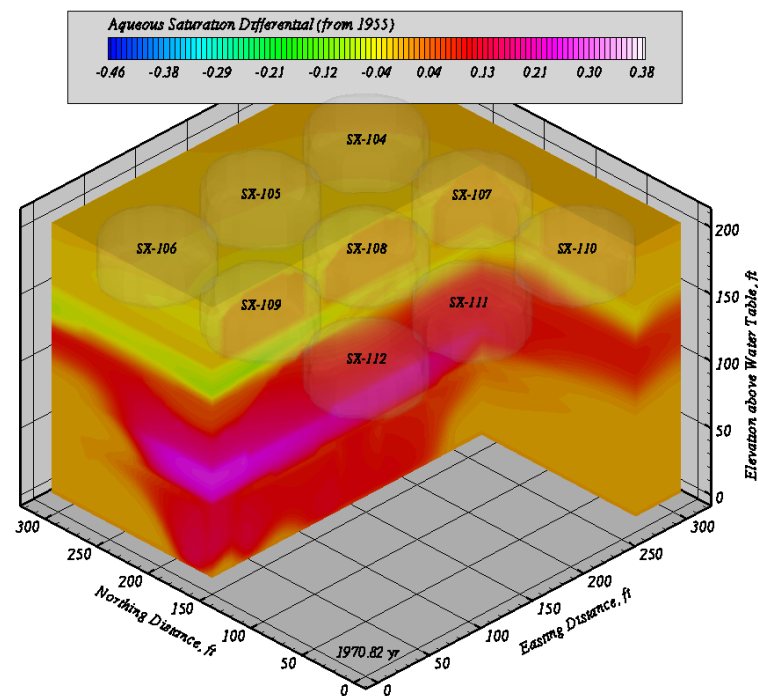
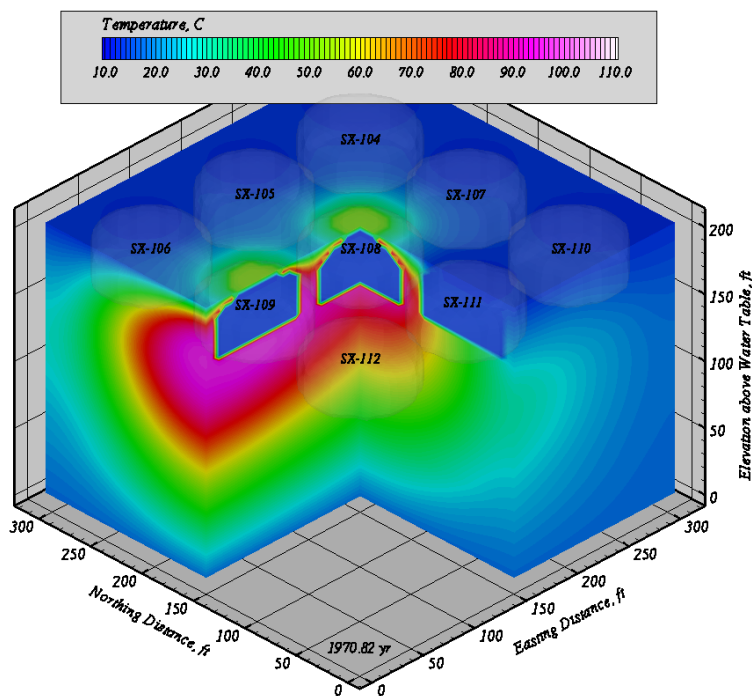
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1965.82



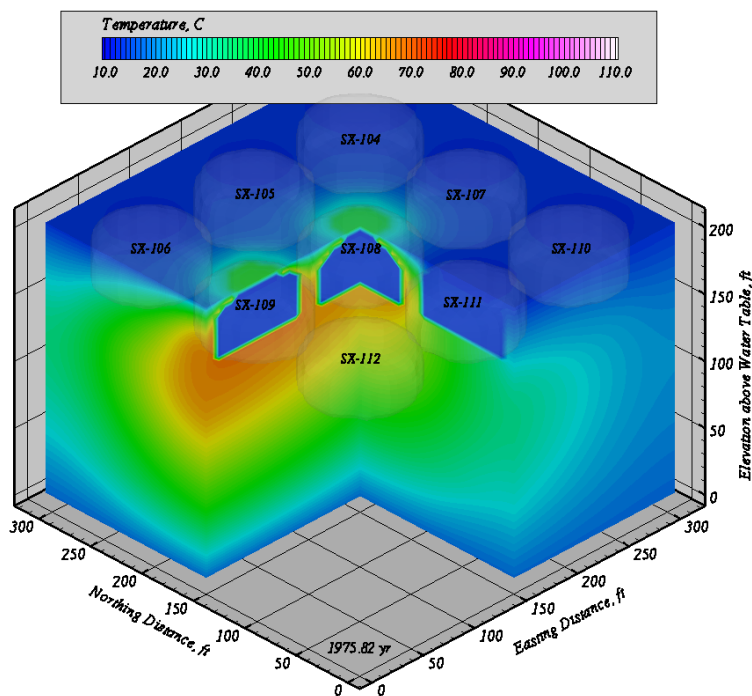
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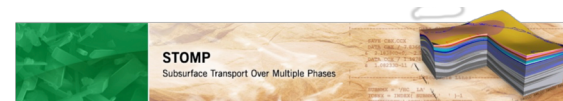
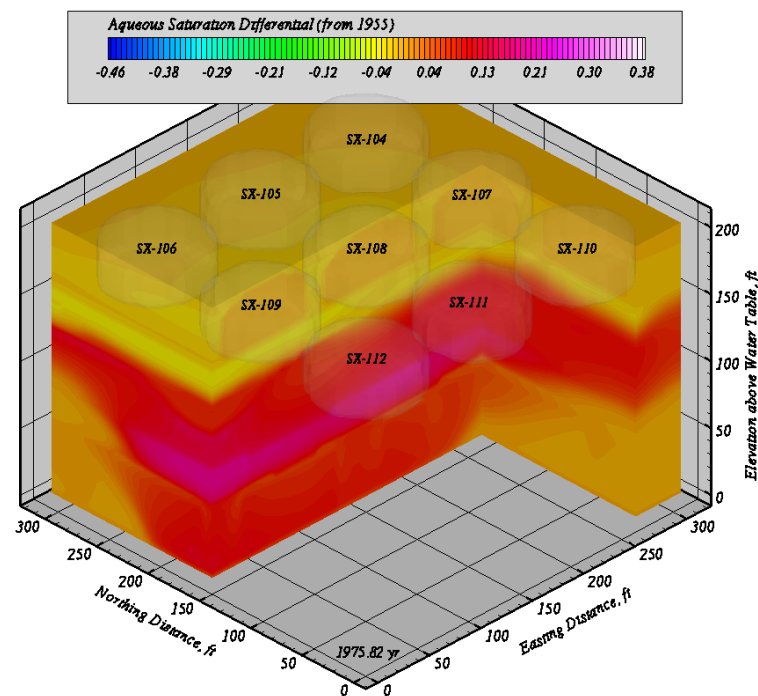
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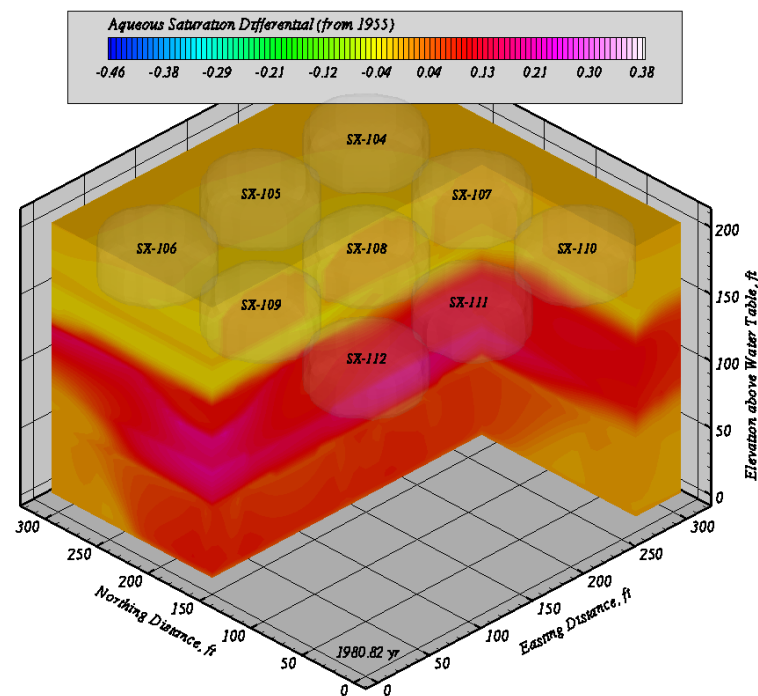
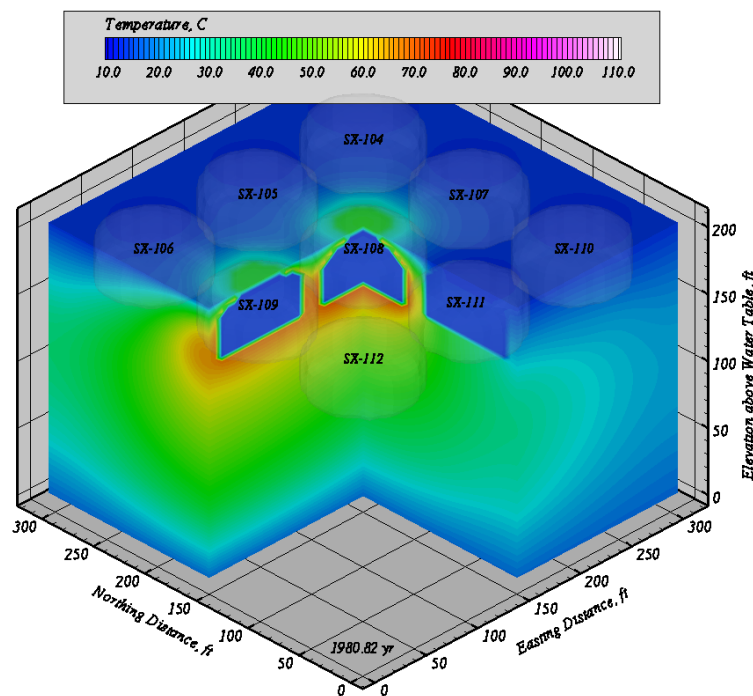
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1975.82



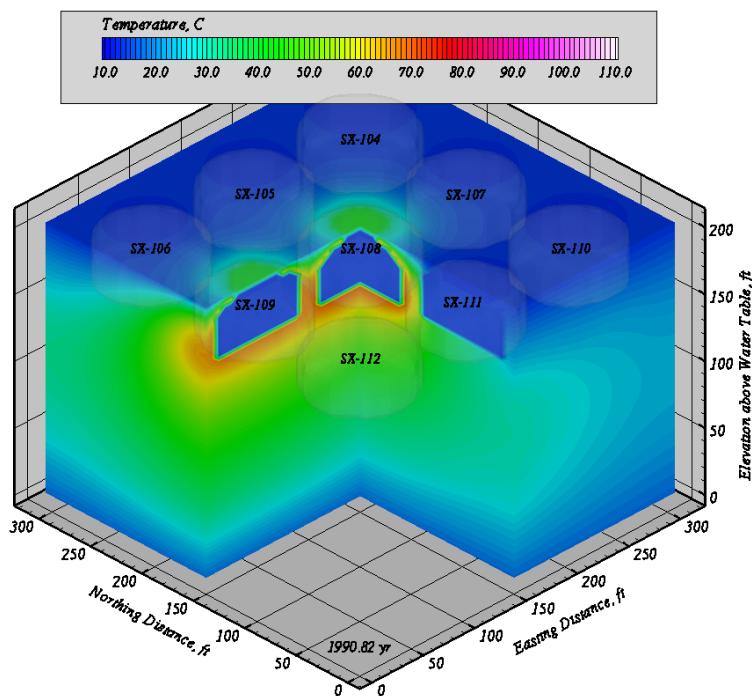
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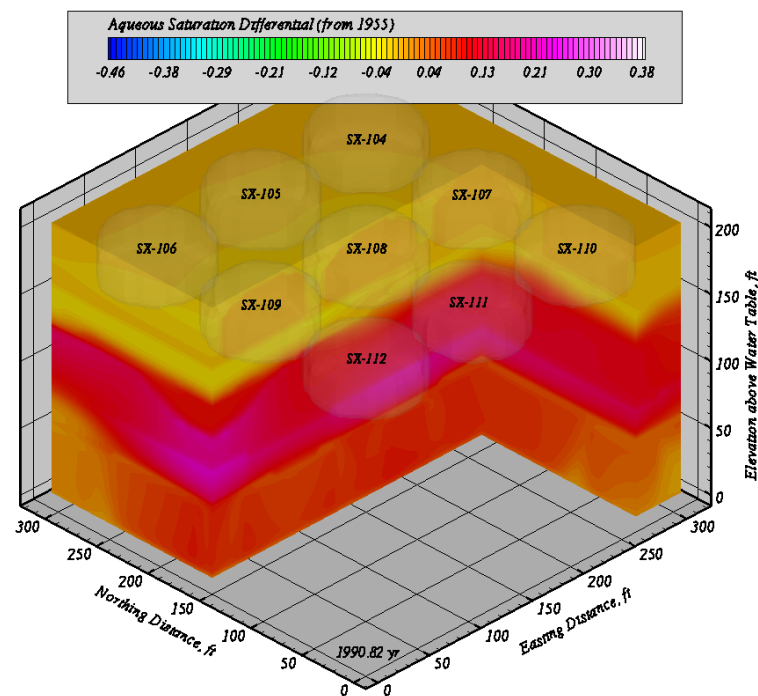
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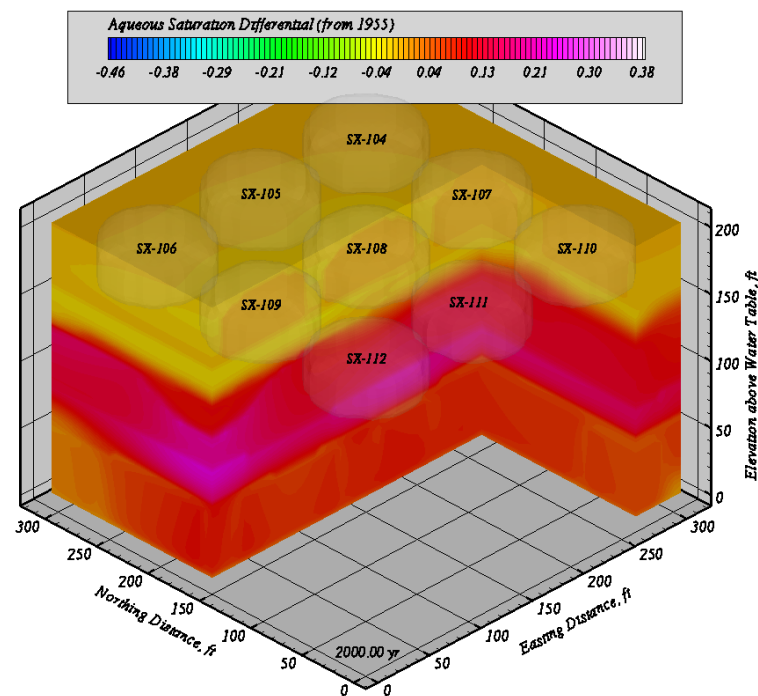
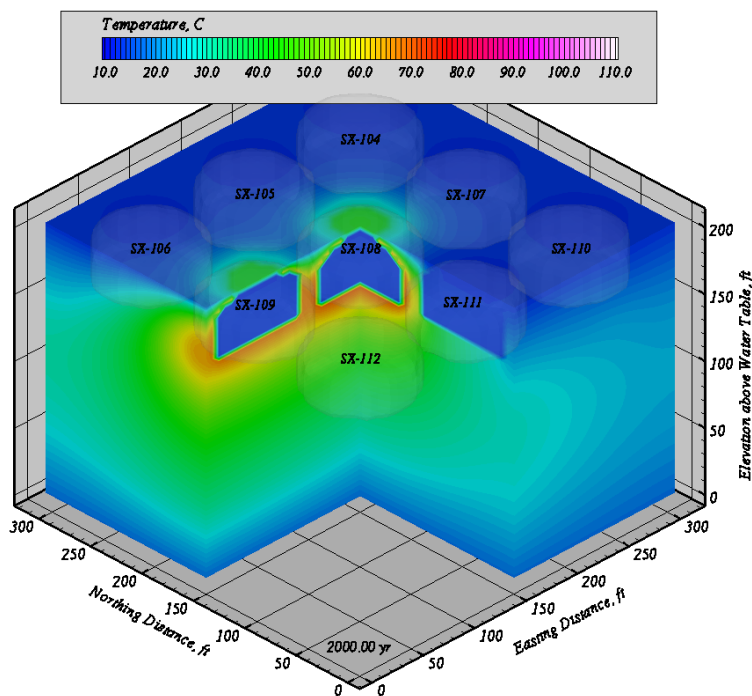
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1990.82



Low-Pressure Air-Water Systems: Example of Coupled Thermal and Hydraulic Environments



2000.00



Low-Pressure Air-Water Systems: Phase Conditions and Transitions

Phase Conditions

1. Saturated without Trapped Gas

- Energy – Temperature
- Water Mass – Aqueous Pressure
- Air Mass – Aqueous Air Mole Fraction
- Salt Mass – Total Brine Mass Fraction

2. Partially Saturated

- Energy – Temperature
- Water Mass – Aqueous Pressure
- Air Mass – Gas Pressure
- Salt Mass – Total Brine Mass Fraction

3. Saturated with Trapped Gas

- Energy – Temperature
- Water Mass – Aqueous Pressure
- Air Mass – Trapped Gas Saturation
- Salt Mass – Total Brine Mass Fraction

4. Fully Unsaturated

- Energy – Temperature
- Water Mass – Water Vapor Partial Pressure
- Air Mass – Gas Pressure
- Salt Mass – Salt Mass



Low-Pressure Water Systems: Phase Conditions and Transitions



Phase Conditions

1. Saturated without Trapped Gas

- Energy – Temperature
- Water Mass – Aqueous Pressure
- Salt Mass – Total Brine Mass Fraction

2. Partially Saturated

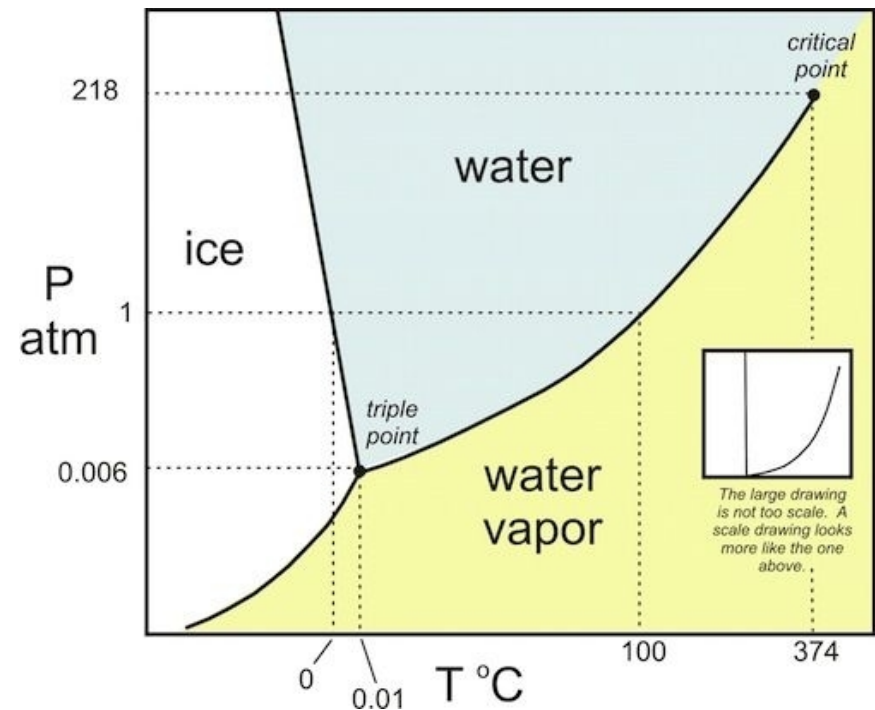
- Energy – Temperature
- Water Mass – Beta Factor
- Salt Mass – Total Brine Mass Fraction

3. Saturated with Trapped Gas

- Energy – Temperature
- Water Mass – Trapped Gas Saturation
- Salt Mass – Total Brine Mass Fraction

4. Fully Unsaturated

- Energy – Temperature
- Water Mass – Water Vapor Partial Pressure
- Salt Mass – Salt Mass



Low-Pressure Air-Water Systems: Phase Conditions and Transitions

Phase Conditions

1. Saturated without Trapped Gas

- Energy – Temperature
- Water Mass – Aqueous Pressure
- Air Mass – Aqueous Air Mole Fraction
- Salt Mass – Total Brine Mass Fraction

2. Partially Saturated

- Energy – Temperature
- Water Mass – Aqueous Pressure
- Air Mass – Gas Pressure
- Salt Mass – Total Brine Mass Fraction

3. Saturated with Trapped Gas

- Energy – Temperature
- Water Mass – Aqueous Pressure
- Air Mass – Trapped Gas Saturation
- Salt Mass – Total Brine Mass Fraction

4. Fully Unsaturated

- Energy – Temperature
- Water Mass – Water Vapor Partial Pressure
- Air Mass – Gas Pressure
- Salt Mass – Salt Mass



PGA – air partial pressure
 PGW – water partial pressure
 PG – gas pressure
 PL – aqueous pressure
 SG – gas saturation
 SL – aqueous saturation

```
PGA = FUNC( XMLA )
PGW = FUNC( T, PCAP )
PG = PGW + PGA
PCAP = PG - PL
SL = FUNC( PCAP )
SG = 1.D+0 - SL
IF( SG > 1.D-3 ) NPHAZ = 2
```

Low-Pressure Air-Water Systems: Phase Conditions and Transitions

Phase Conditions

1. Saturated without Trapped Gas

- Energy – Temperature
- Water Mass – Aqueous Pressure
- Air Mass – Aqueous Air Mole Fraction
- Salt Mass – Total Brine Mass Fraction

2. Partially Saturated

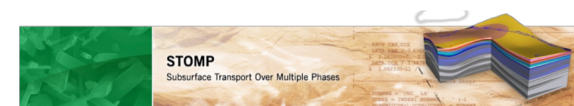
- Energy – Temperature
- Water Mass – Aqueous Pressure
- Air Mass – Gas Pressure
- Salt Mass – Total Brine Mass Fraction

3. Saturated with Trapped Gas

- Energy – Temperature
- Water Mass – Aqueous Pressure
- Air Mass – Trapped Gas Saturation
- Salt Mass – Total Brine Mass Fraction

4. Fully Unsaturated

- Energy – Temperature
- Water Mass – Water Vapor Partial Pressure
- Air Mass – Gas Pressure
- Salt Mass – Salt Mass



PG – gas pressure
 PL – aqueous pressure
 ASL – apparent aqueous sat.
 SGT – trapped gas sat.

PCAP = PG – PL
 ASL = FUNC(PCAP)
 IF(ASL == 0 && SGT == 0)
 NPHAZ = 1

Low-Pressure Air-Water Systems: Phase Conditions and Transitions

Phase Conditions

1. Saturated without Trapped Gas

- Energy – Temperature
- Water Mass – Aqueous Pressure
- Air Mass – Aqueous Air Mole Fraction
- Salt Mass – Total Brine Mass Fraction

2. Partially Saturated

- Energy – Temperature
- Water Mass – Aqueous Pressure
- Air Mass – Gas Pressure
- Salt Mass – Total Brine Mass Fraction

3. Saturated with Trapped Gas

- Energy – Temperature
- Water Mass – Aqueous Pressure
- Air Mass – Trapped Gas Saturation
- Salt Mass – Total Brine Mass Fraction

4. Fully Unsaturated

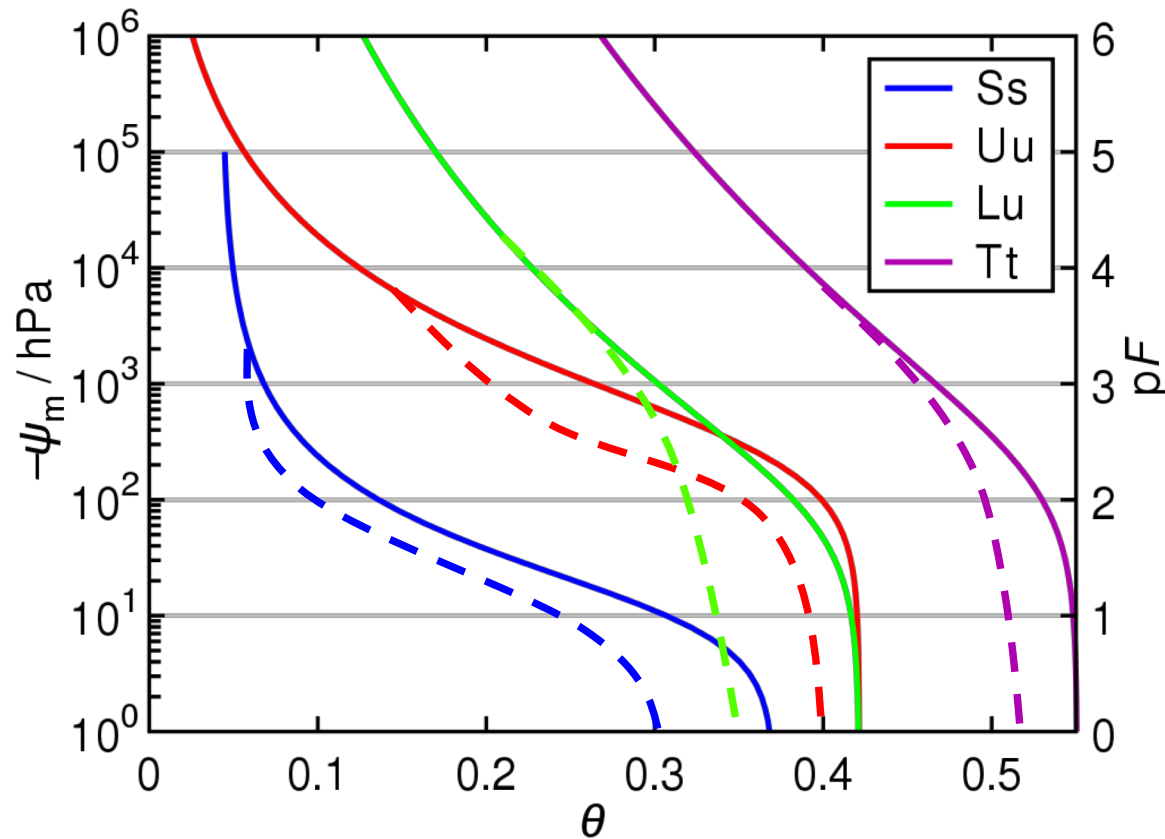
- Energy – Temperature
- Water Mass – Water Vapor Partial Pressure
- Air Mass – Gas Pressure
- Salt Mass – Salt Mass



PG – gas pressure
 PL – aqueous pressure
 ASL – apparent aqueous sat.
 SGT – trapped gas sat.

PCAP = PG – PL
 ASL = FUNC(PCAP)
 IF(ASL == 0 && SGT > 0)
 NPHAZ = 3

Low-Pressure Air-Water Systems: Phase Conditions and Transitions



Ss – sand

Uu – silt or clay loam

LU – loam-silt or clay

Tt – clay or peat

Low-Pressure Air-Water Systems: Phase Conditions and Transitions

Phase Conditions

1. Saturated without Trapped Gas

- Energy – Temperature
- Water Mass – Aqueous Pressure
- Air Mass – Aqueous Air Mole Fraction
- Salt Mass – Total Brine Mass Fraction

2. Partially Saturated

- Energy – Temperature
- Water Mass – Aqueous Pressure
- Air Mass – Gas Pressure
- Salt Mass – Total Brine Mass Fraction

3. Saturated with Trapped Gas

- Energy – Temperature
- Water Mass – Aqueous Pressure
- Air Mass – Trapped Gas Saturation
- Salt Mass – Total Brine Mass Fraction

4. Fully Unsaturated

- Energy – Temperature
- Water Mass – Water Vapor Partial Pressure
- Air Mass – Gas Pressure
- Salt Mass – Salt Mass



PG – gas pressure
 PL – aqueous pressure
 ASL – apparent aqueous sat.
 SL – aqueous saturation
 SGT – trapped gas sat.

PCAP = PG – PL
 ASL = FUNC(PCAP)
 SL = ASL – SGT
 IF(SL == 0) NPHAZ = 4

Guidance on Primary Variables

- Direct Solution Path Between Primary and Secondary Variables
- Equation Residual is Sensitive to Primary Variable
- Think Creatively ... y_ℓ^s - brine mass fraction of total salt

Differential Form

$$\frac{\partial}{\partial t} \left[\sum_{\gamma=l,n,g,h,i,p} (\phi_D \rho_\gamma s_\gamma u_\gamma) + (1-\phi_T) \rho_s u_s + (\phi_T - \phi_D) \rho_l u_l \right] =$$

$$- \sum_{\gamma=l,n,g} \nabla (\rho_\gamma h_\gamma \mathbf{v}_\gamma) - \sum_{i=w,a,o} \nabla (h_g^i \mathbf{J}_g^i) + \nabla (\mathbf{k}_e \nabla T) + \sum_{\gamma=l,n,g} (h_\gamma m_\gamma) + q$$

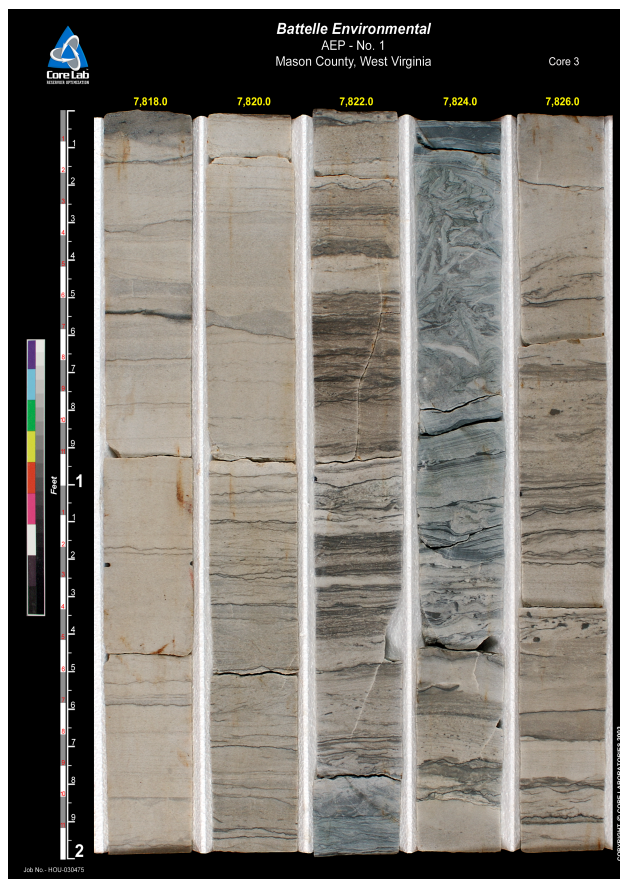
$$\mathbf{v}_\gamma = -\frac{k_{r\gamma} \mathbf{k}}{\mu_\gamma} (\nabla P_\gamma + \rho_\gamma g \mathbf{z}_g)$$

$$\mathbf{J}_g^i = -\phi_D \rho_g s_g \frac{M^i}{M_g} \left(\tau_g D_g^i + \mathbf{D}_{h_g} \right) \nabla \chi_g^i$$

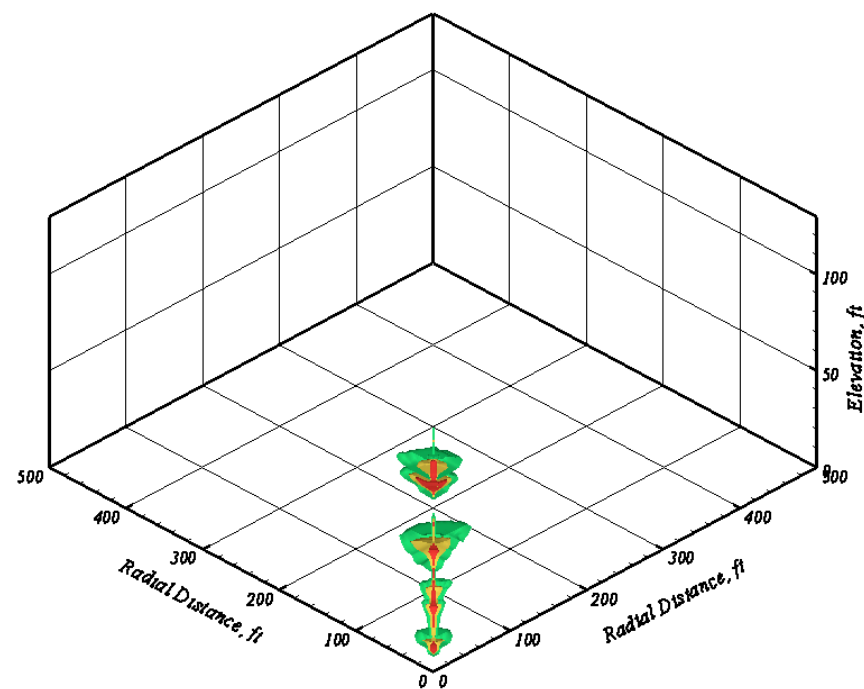
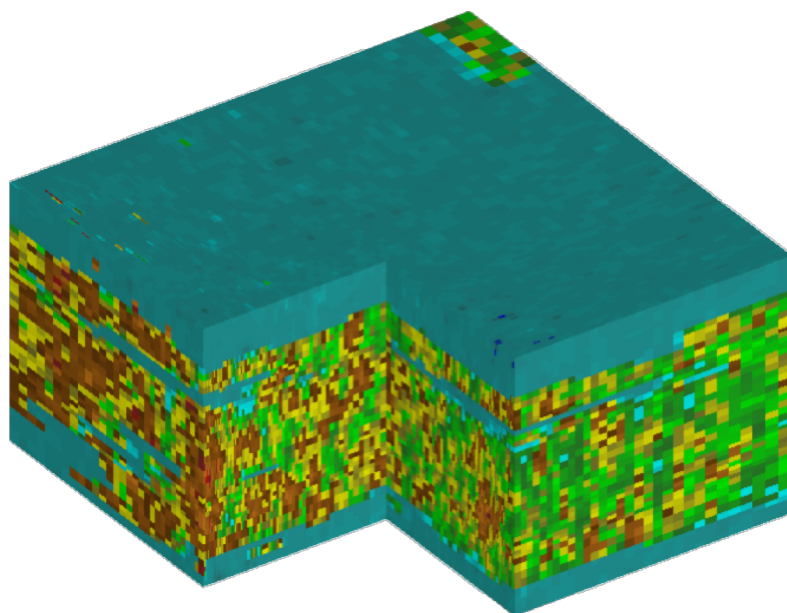
Nonlinear Algebraic Form

Spatial Discretization

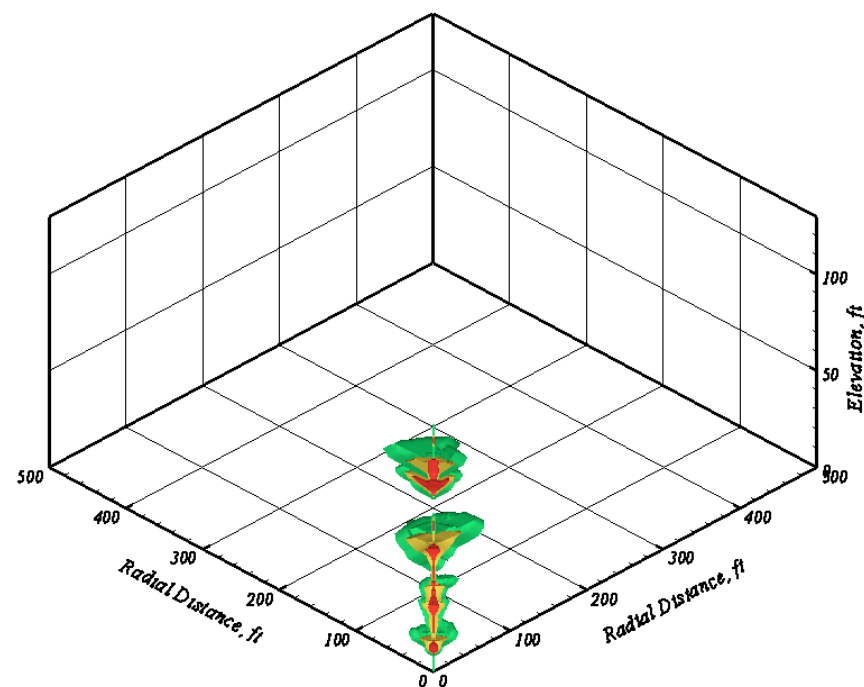
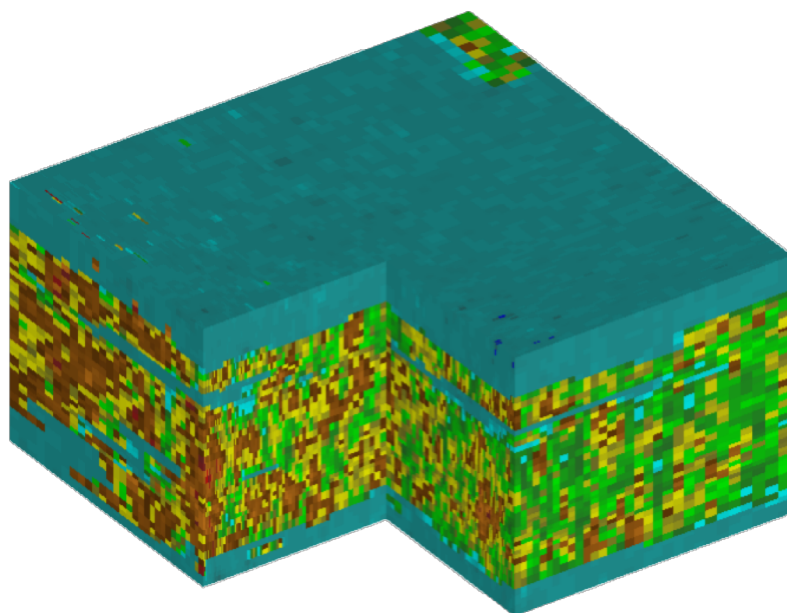
High-Pressure CO₂-Brine Systems



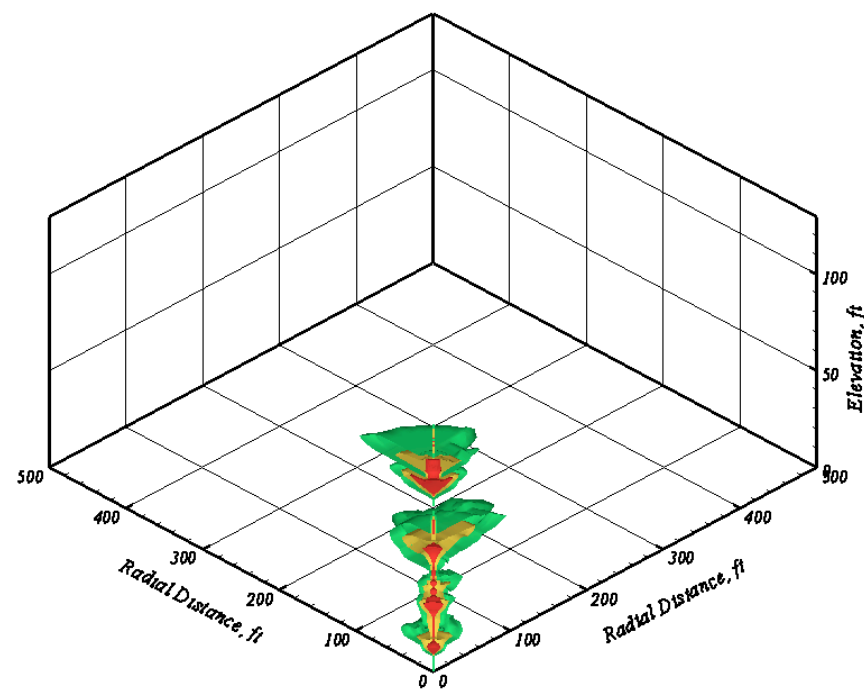
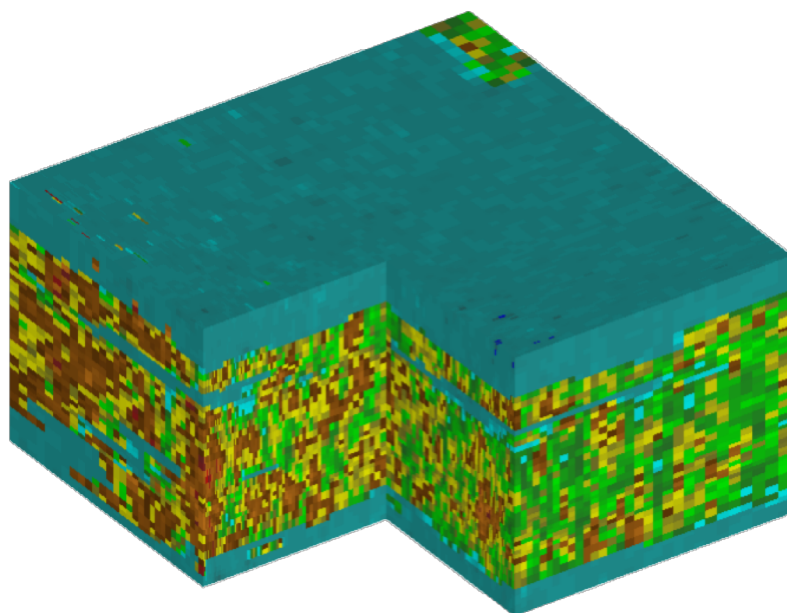
High-Pressure CO₂-Brine Systems: Example of Injection into Heterogeneous Domain



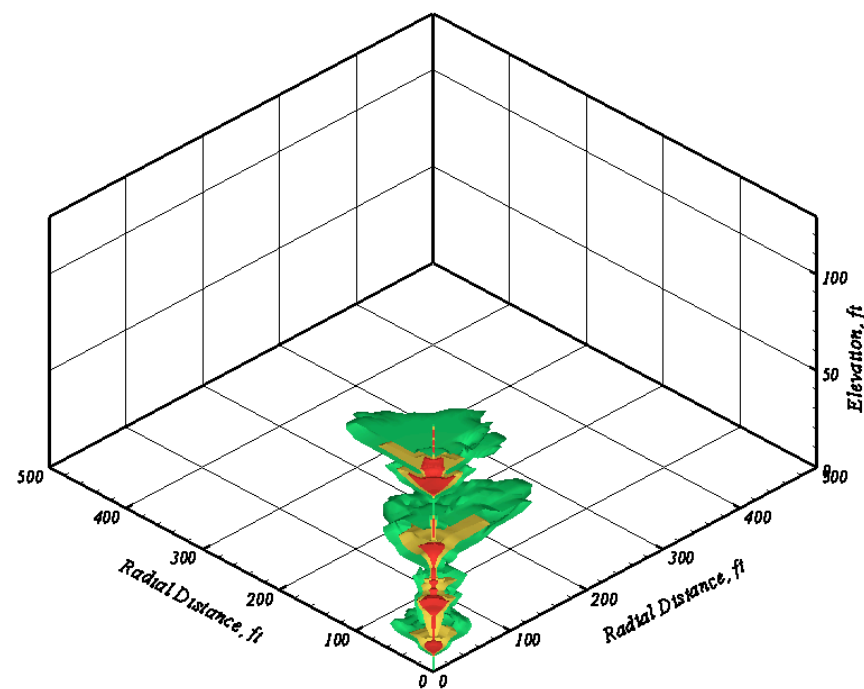
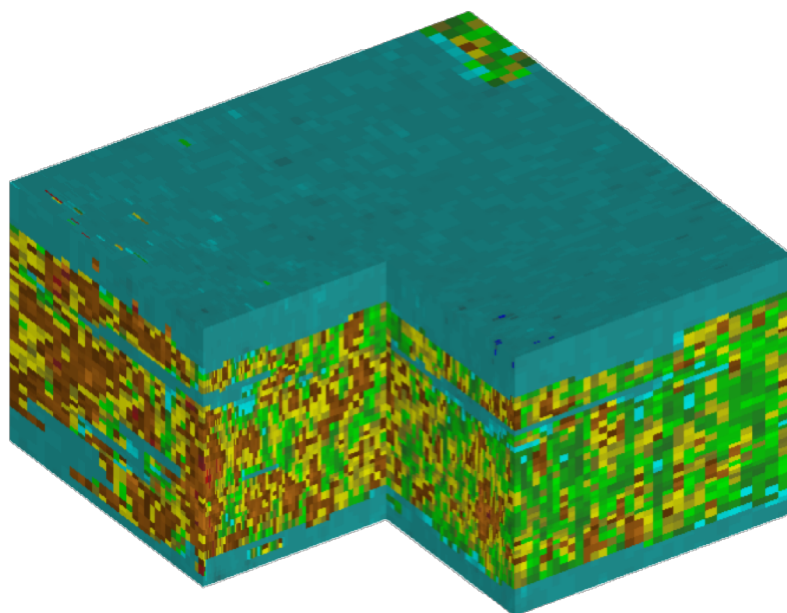
High-Pressure CO₂-Brine Systems: Example of Injection into Heterogeneous Domain



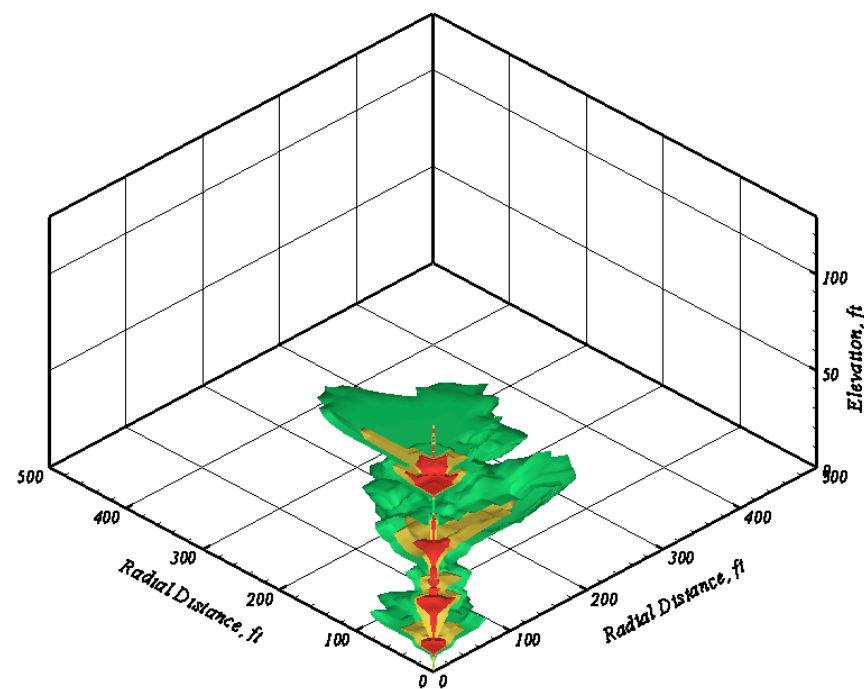
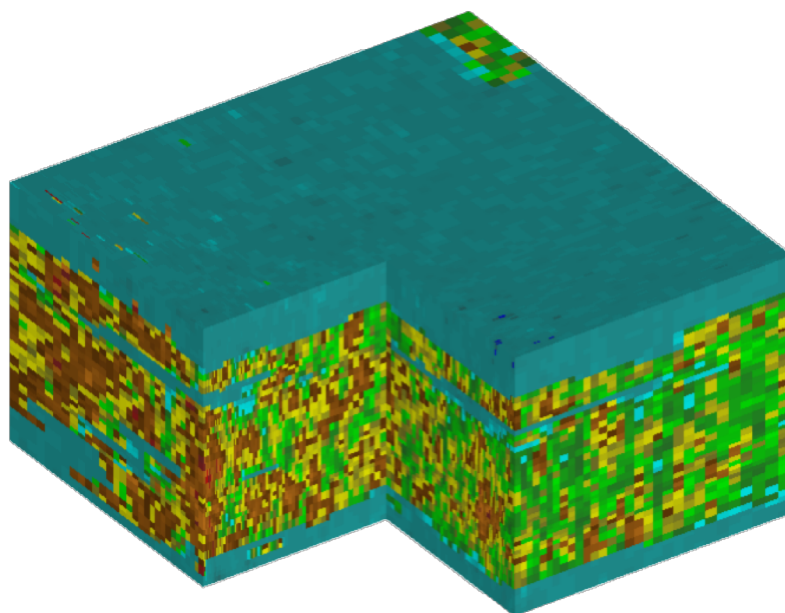
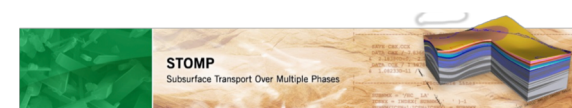
High-Pressure CO₂-Brine Systems: Example of Injection into Heterogeneous Domain



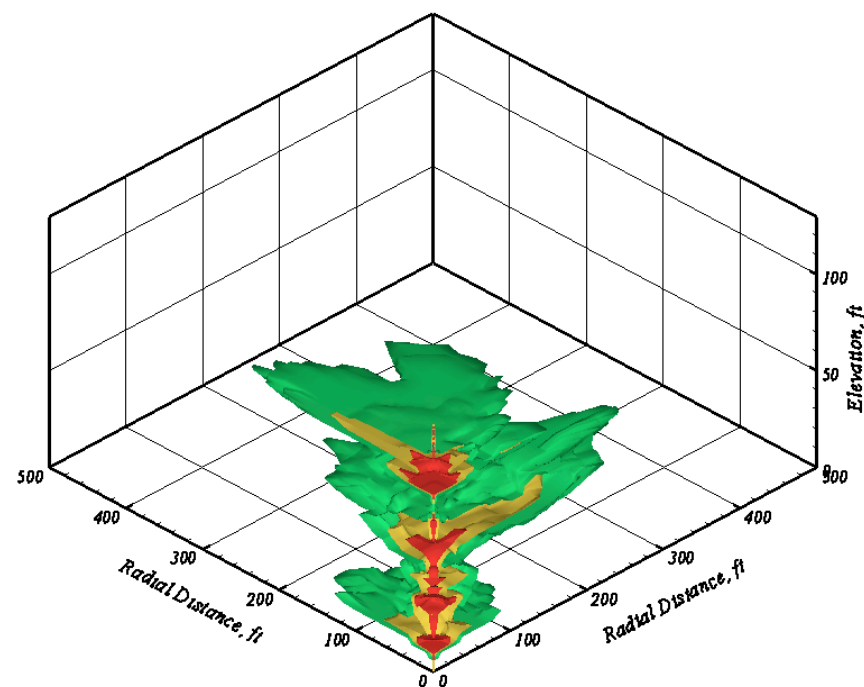
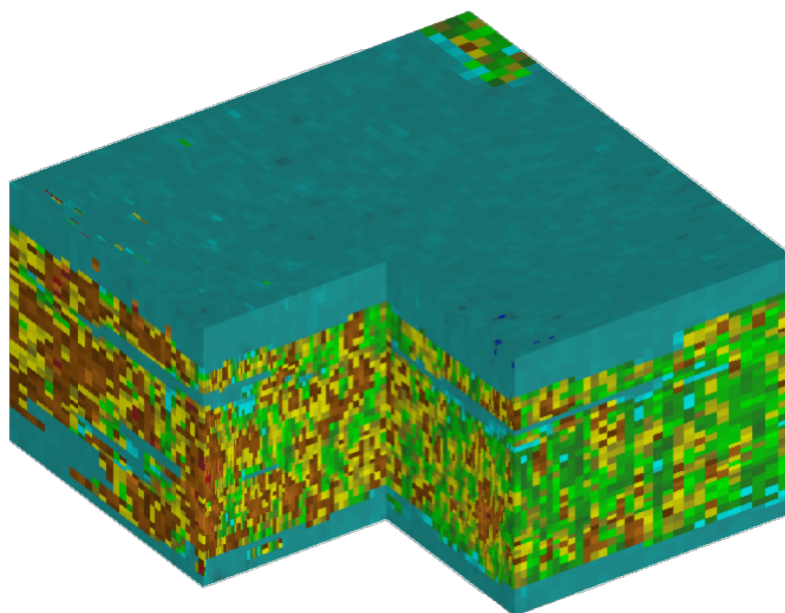
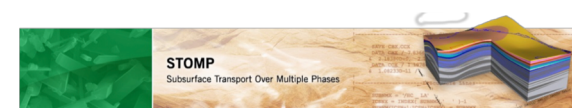
High-Pressure CO₂-Brine Systems: Example of Injection into Heterogeneous Domain



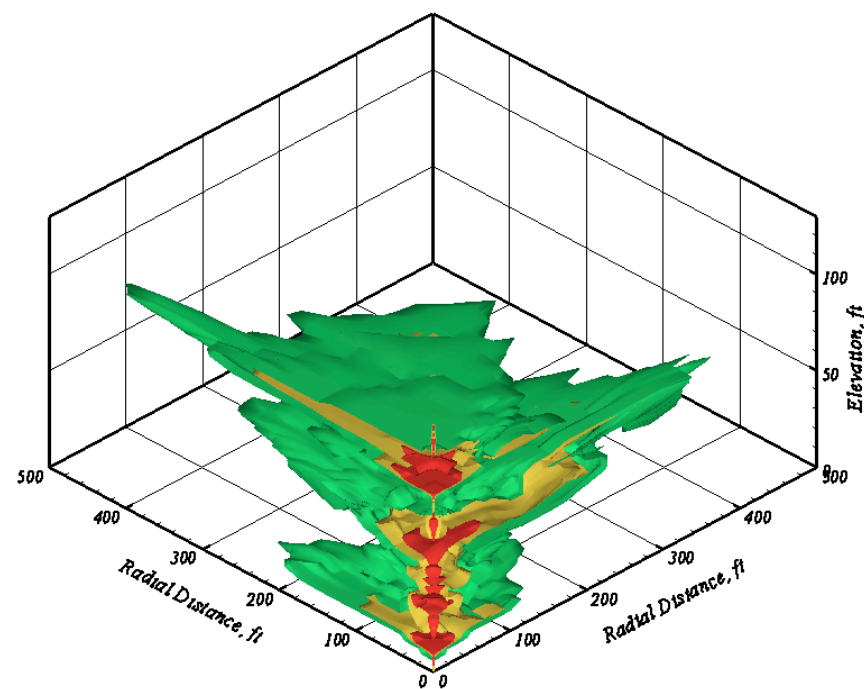
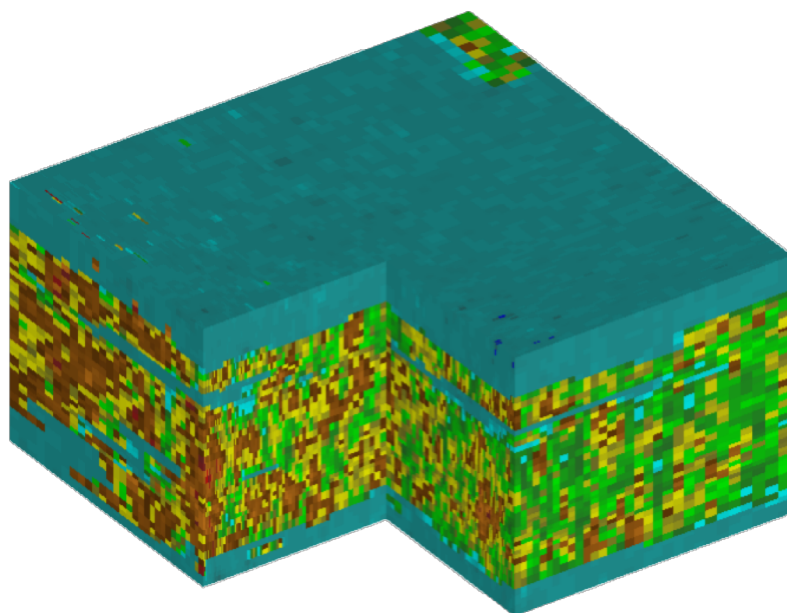
High-Pressure CO₂-Brine Systems: Example of Injection into Heterogeneous Domain



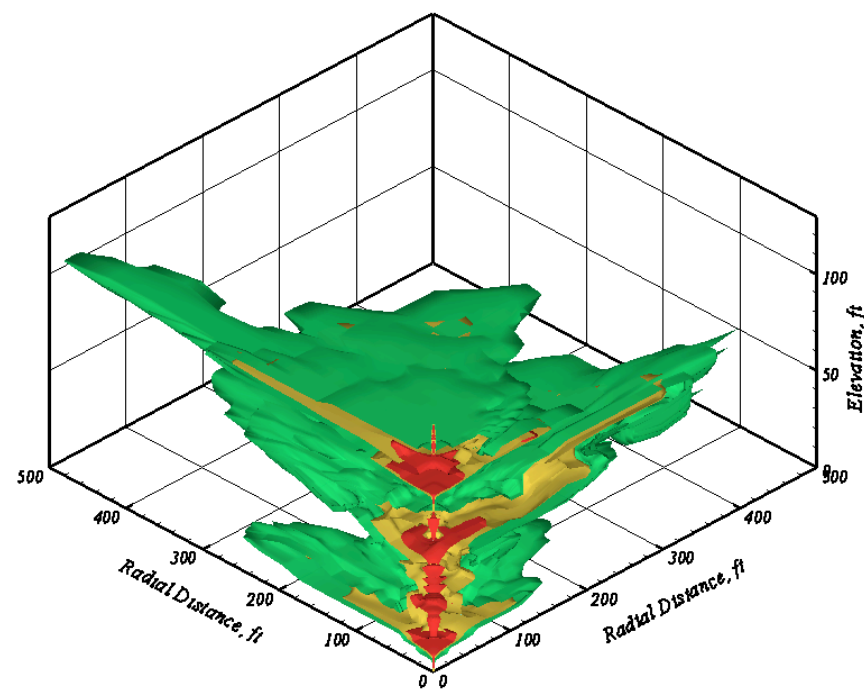
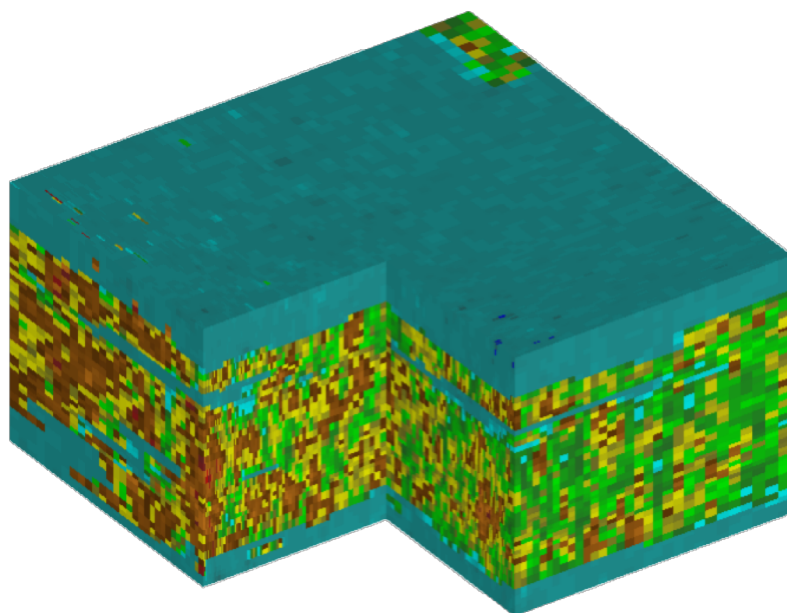
High-Pressure CO₂-Brine Systems: Example of Injection into Heterogeneous Domain



High-Pressure CO₂-Brine Systems: Example of Injection into Heterogeneous Domain



High-Pressure CO₂-Brine Systems: Example of Injection into Heterogeneous Domain



High-Pressure CO₂-Brine Systems: Phase Conditions

Phase Conditions

1. Saturated without Trapped Gas

- Energy – Temperature
- Water Mass – Aqueous Pressure
- CO₂ Mass – Aqueous CO₂ Mole Fraction
- Salt Mass – Total Brine Mass Fraction

2. Partially Saturated

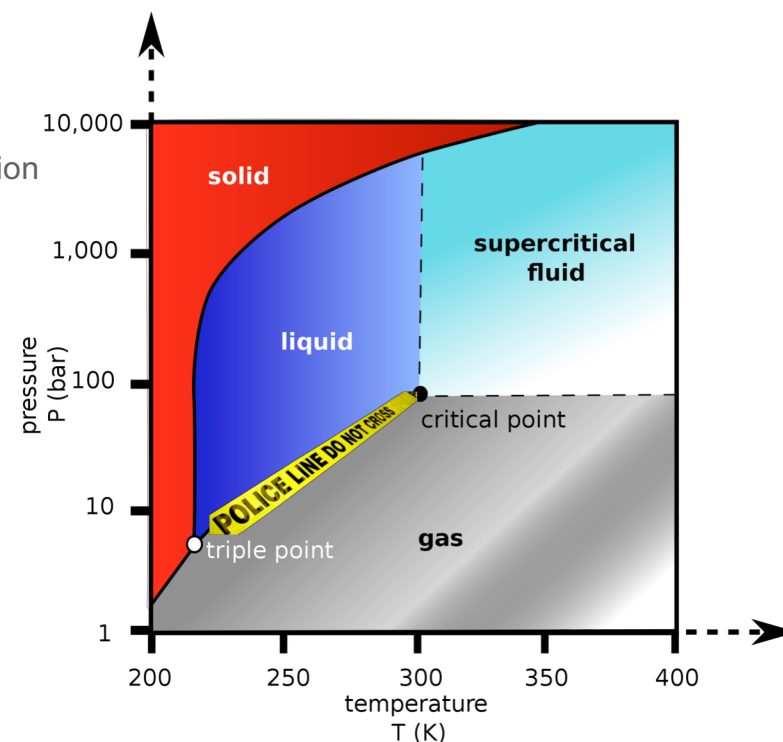
- Energy – Temperature
- Water Mass – Aqueous Pressure
- CO₂ Mass – Gas Pressure
- Salt Mass – Total Brine Mass Fraction

3. Saturated with Trapped Gas

- Energy – Temperature
- Water Mass – Aqueous Pressure
- CO₂ Mass – Trapped Gas Saturation
- Salt Mass – Total Brine Mass Fraction

4. Fully Unsaturated

- Energy – Temperature
- Water Mass – Water Vapor Partial Pressure
- CO₂ Mass – Gas Pressure
- Salt Mass – Salt Mass



High-Pressure CO₂-Brine Systems: Phase Conditions and Transitions

Phase Conditions

1. Saturated without Trapped Gas

- Energy – Temperature
- Water Mass – Aqueous Pressure
- CO₂ Mass – Aqueous CO₂ Mole Fraction
- Salt Mass – Total Brine Mass Fraction

2. Partially Saturated

- Energy – Temperature
- Water Mass – Aqueous Pressure
- CO₂ Mass – Gas Pressure
- Salt Mass – Total Brine Mass Fraction

3. Saturated with Trapped Gas

- Energy – Temperature
- Water Mass – Aqueous Pressure
- CO₂ Mass – Trapped Gas Saturation
- Salt Mass – Total Brine Mass Fraction

4. Fully Unsaturated

- Energy – Temperature
- Water Mass – Water Vapor Partial Pressure
- CO₂ Mass – Gas Pressure
- Salt Mass – Salt Mass



PGA – CO₂ partial pressure
 PGW – water partial pressure
 PG – gas pressure
 PL – aqueous pressure
 SG – gas saturation
 SL – aqueous saturation

PGA = FUNC(XMLA)
 PGW = FUNC(T, PCAP)
 PG = PGW + PGA
 PCAP = PG – PL
 SL = FUNC(PCAP)
 SG = 1.D+0 – SL
 IF(SG > 1.D-3) NPHAZ = 2

High-Pressure CO₂-Brine Systems: Phase Conditions and Transitions

Phase Conditions

1. Saturated without Trapped Gas

- Energy – Temperature
- Water Mass – Aqueous Pressure
- CO₂ Mass – Aqueous CO₂ Mole Fraction
- Salt Mass – Total Brine Mass Fraction

2. Partially Saturated

- Energy – Temperature
- Water Mass – Aqueous Pressure
- CO₂ Mass – Gas Pressure
- Salt Mass – Total Brine Mass Fraction

3. Saturated with Trapped Gas

- Energy – Temperature
- Water Mass – Aqueous Pressure
- CO₂ Mass – Trapped Gas Saturation
- Salt Mass – Total Brine Mass Fraction

4. Fully Unsaturated

- Energy – Temperature
- Water Mass – Water Vapor Partial Pressure
- CO₂ Mass – Gas Pressure
- Salt Mass – Salt Mass



PG – gas pressure
PL – aqueous pressure
ASL – apparent aqueous sat.
SGT – trapped gas sat.

PCAP = PG – PL
ASL = FUNC(PCAP)
IF(ASL == 0 && SGT == 0)
NPHAZ = 1

High-Pressure CO₂-Brine Systems: Phase Conditions and Transitions

Phase Conditions

1. Saturated without Trapped Gas

- Energy – Temperature
- Water Mass – Aqueous Pressure
- CO₂ Mass – Aqueous CO₂ Mole Fraction
- Salt Mass – Total Brine Mass Fraction

2. Partially Saturated

- Energy – Temperature
- Water Mass – Aqueous Pressure
- CO₂ Mass – Gas Pressure
- Salt Mass – Total Brine Mass Fraction

3. Saturated with Trapped Gas

- Energy – Temperature
- Water Mass – Aqueous Pressure
- CO₂ Mass – Trapped Gas Saturation
- Salt Mass – Total Brine Mass Fraction

4. Fully Unsaturated

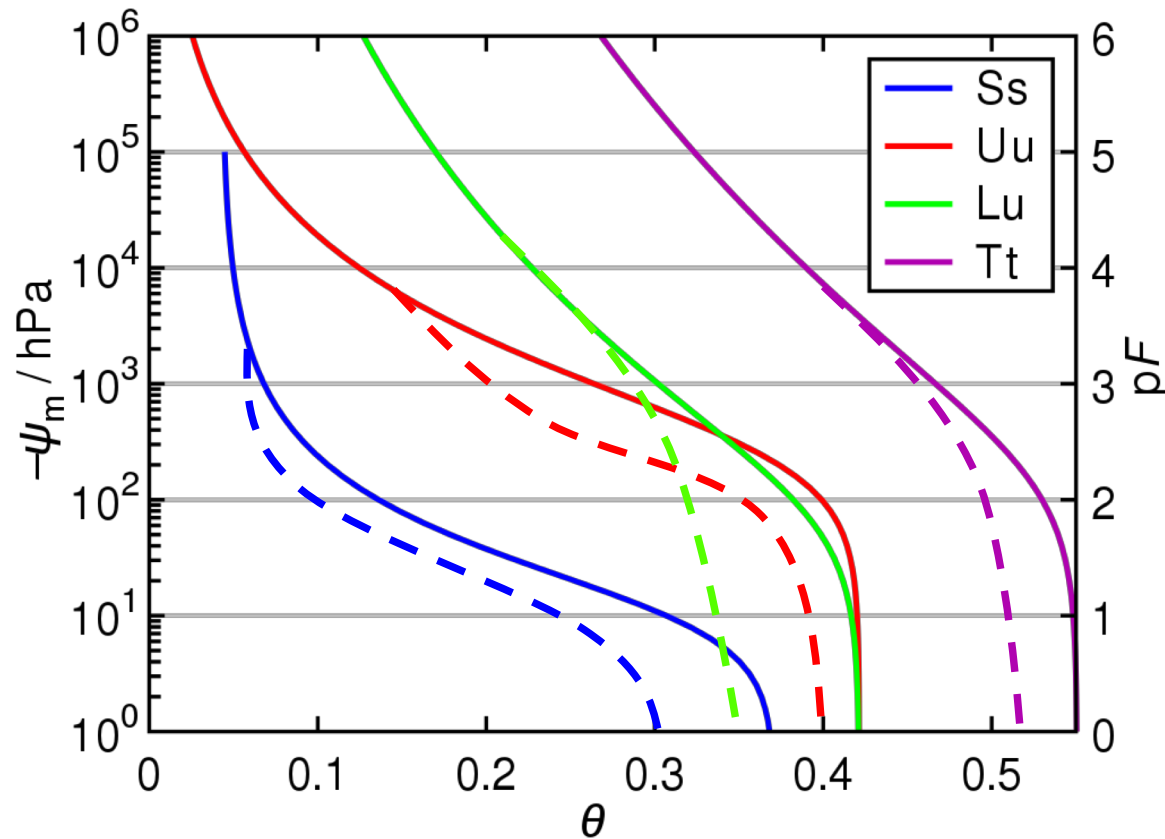
- Energy – Temperature
- Water Mass – Water Vapor Partial Pressure
- CO₂ Mass – Gas Pressure
- Salt Mass – Salt Mass



PG – gas pressure
PL – aqueous pressure
ASL – apparent aqueous sat.
SGT – trapped gas sat.

PCAP = PG – PL
ASL = FUNC(PCAP)
IF(ASL == 0 && SGT > 0)
NPHAZ = 3

Low-Pressure Air-Water Systems: Phase Conditions and Transitions



Ss – sand

Uu – silt or clay loam

LU – loam-silt or clay

Tt – clay or peat

High-Pressure CO₂-Brine Systems: Phase Conditions and Transitions

Phase Conditions

1. Saturated without Trapped Gas

- Energy – Temperature
- Water Mass – Aqueous Pressure
- CO₂ Mass – Aqueous CO₂ Mole Fraction
- Salt Mass – Total Brine Mass Fraction

2. Partially Saturated

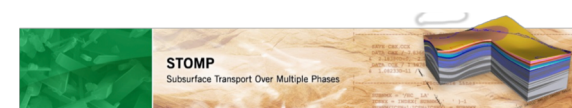
- Energy – Temperature
- Water Mass – Aqueous Pressure
- CO₂ Mass – Gas Pressure
- Salt Mass – Total Brine Mass Fraction

3. Saturated with Trapped Gas

- Energy – Temperature
- Water Mass – Aqueous Pressure
- CO₂ Mass – Trapped Gas Saturation
- Salt Mass – Total Brine Mass Fraction

4. Fully Unsaturated

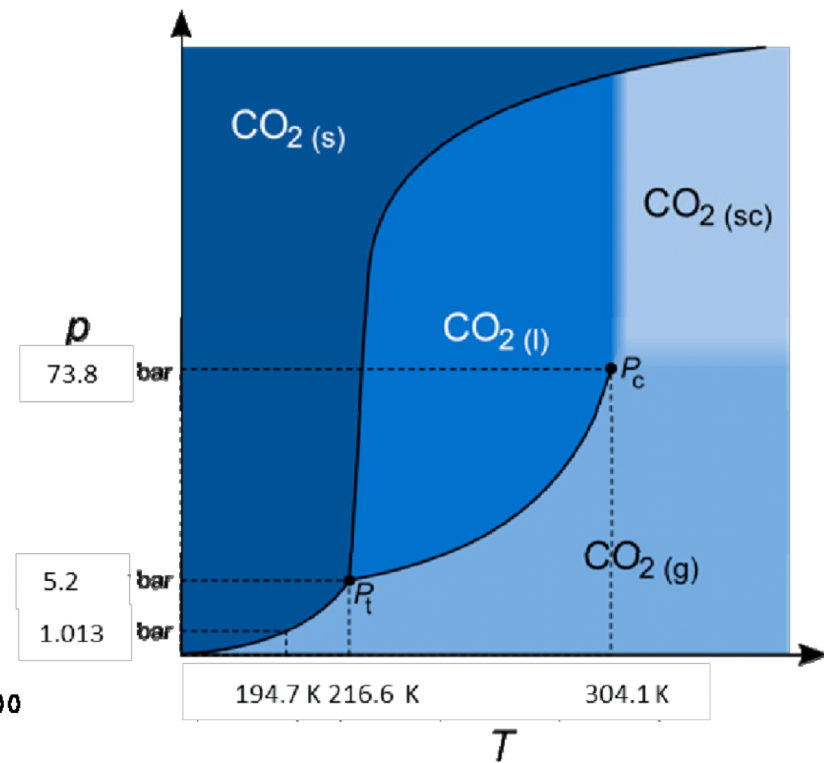
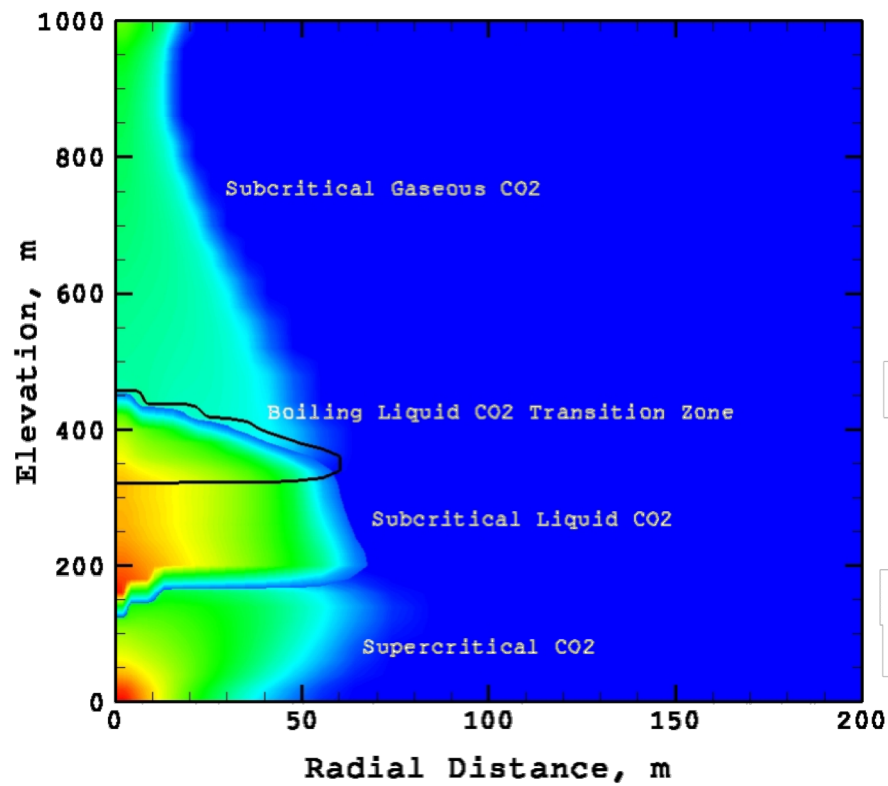
- Energy – Temperature
- Water Mass – Water Vapor Partial Pressure
- CO₂ Mass – Gas Pressure
- Salt Mass – Salt Mass



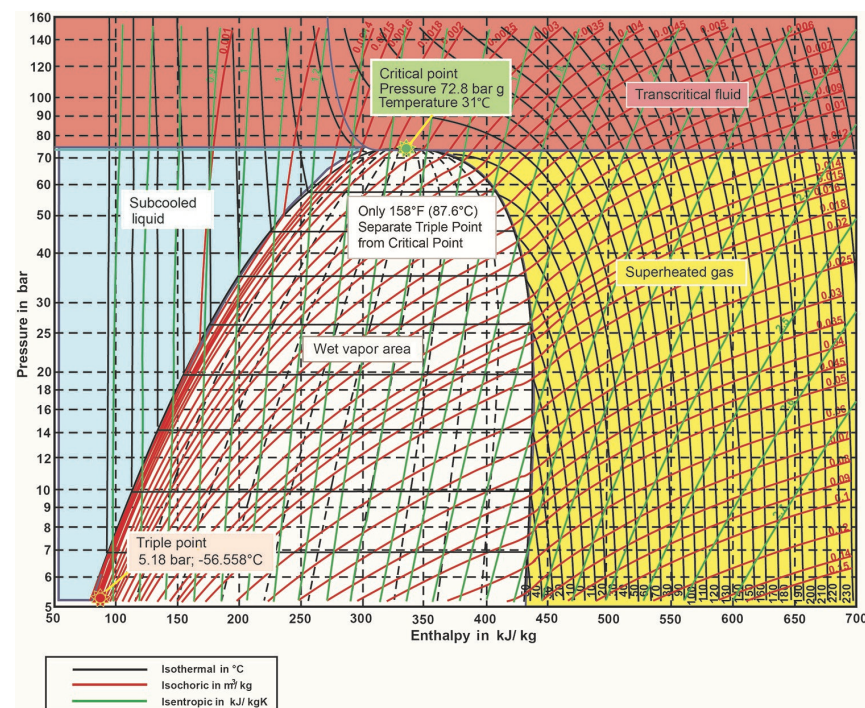
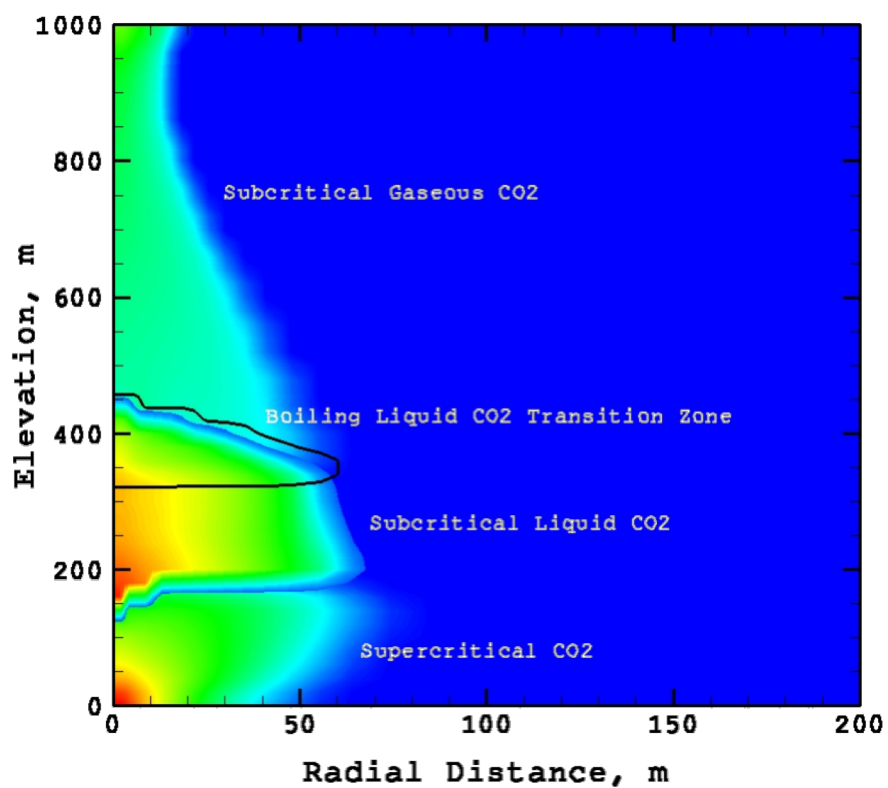
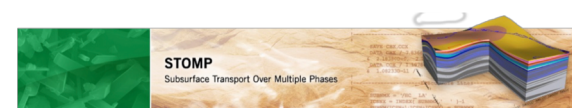
PG – gas pressure
 PL – aqueous pressure
 ASL – apparent aqueous sat.
 SL – aqueous saturation
 SGT – trapped gas sat.

PCAP = PG – PL
 ASL = FUNC(PCAP)
 SL = ASL – SGT
 IF(SL == 0) NPHAZ = 4

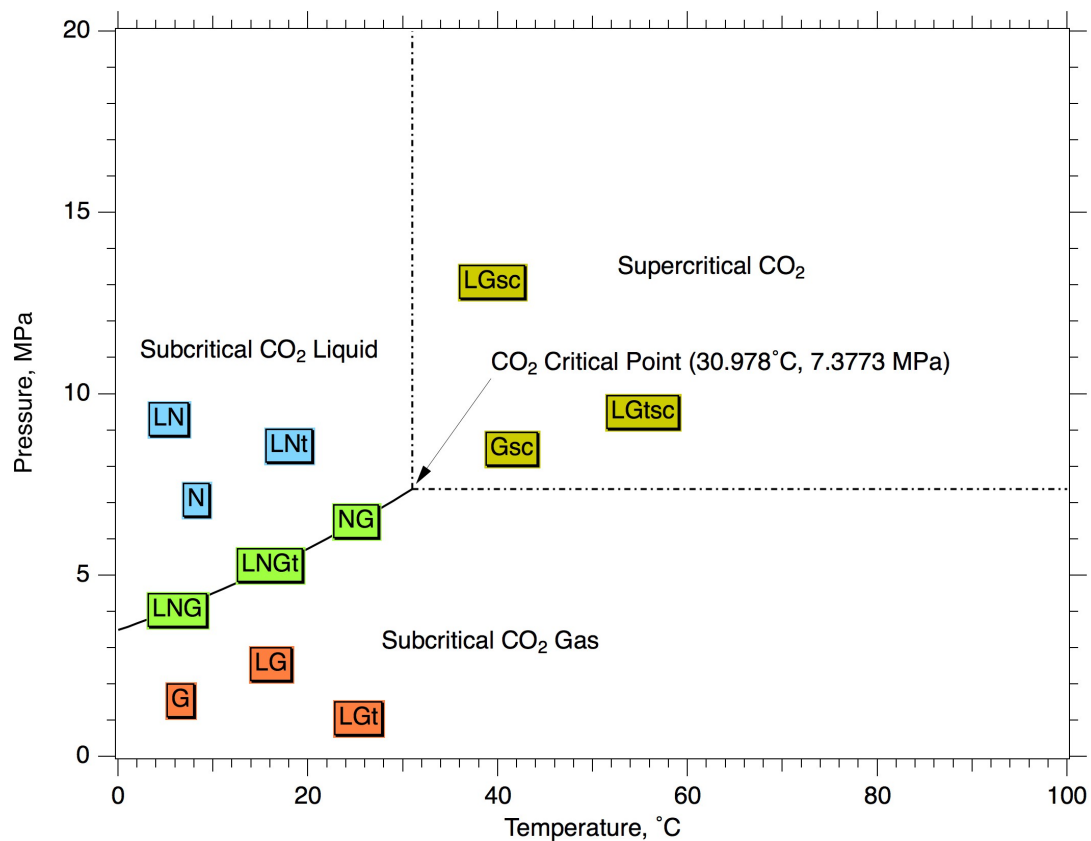
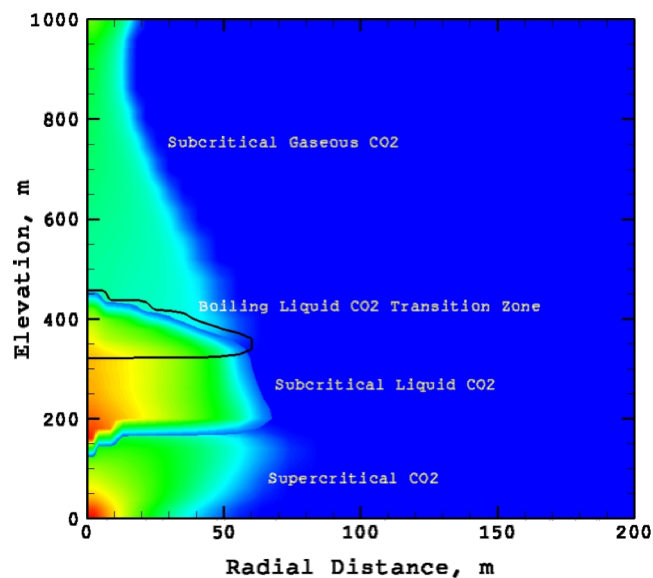
Leakage of CO₂ from Deep Reservoirs to the Ground Surface



Leakage of CO₂ from Deep Reservoirs to the Ground Surface



Three-Phase System for CO₂ Migration through the Subsurface: Phase Condition Mapping

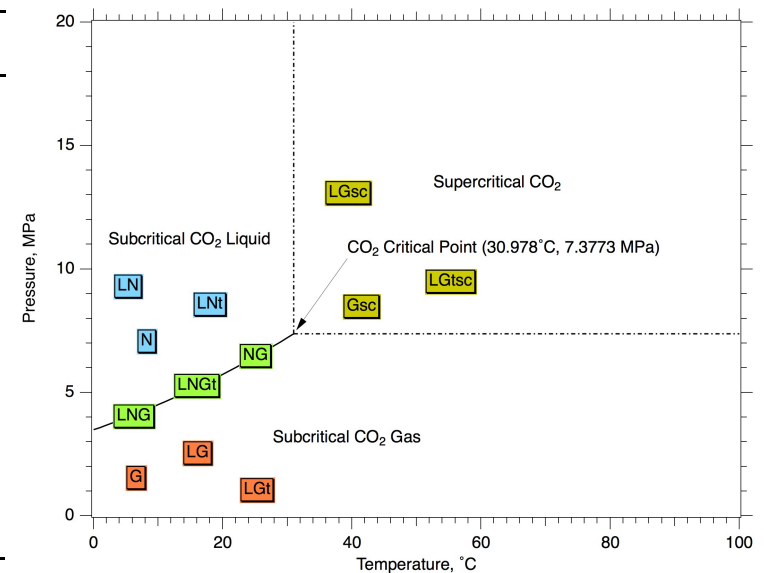


Three-Phase System for CO₂ Migration through the Subsurface: Phase Conditions and Primary Variables

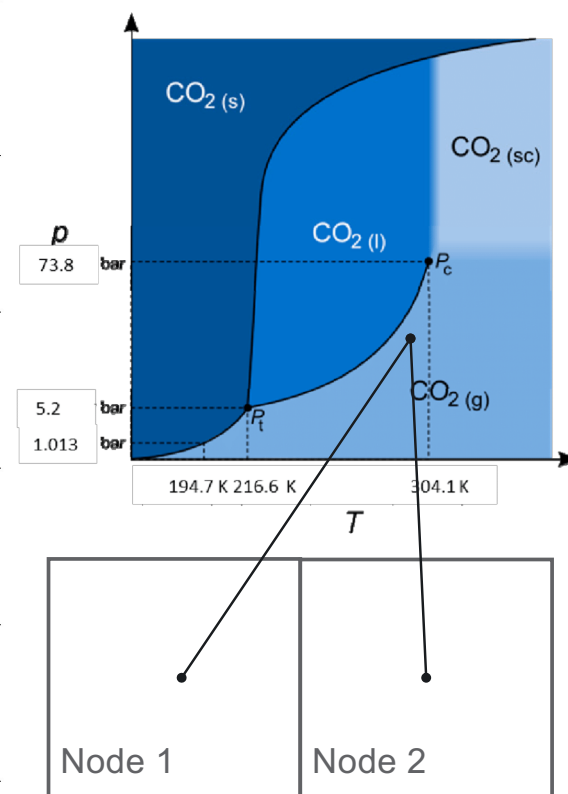
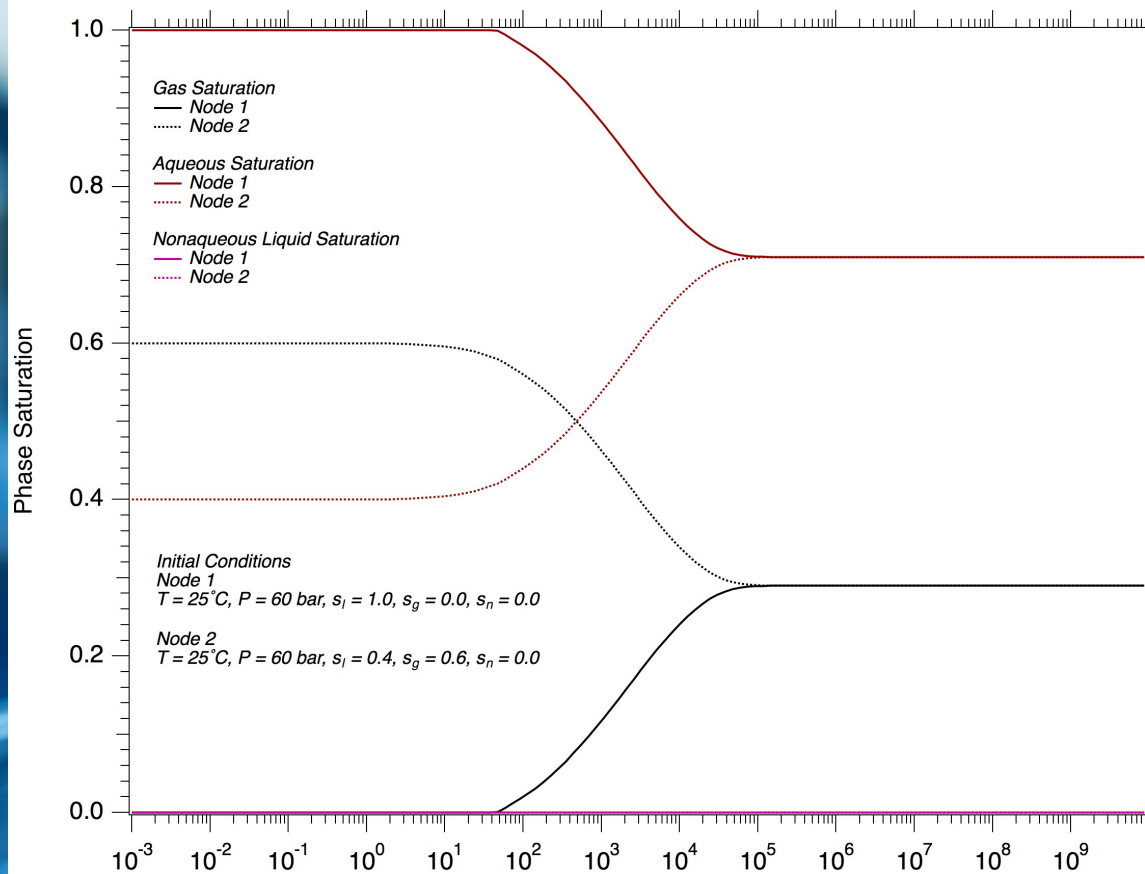


Table 1. STOMP-SEQ primary variable switching scheme.

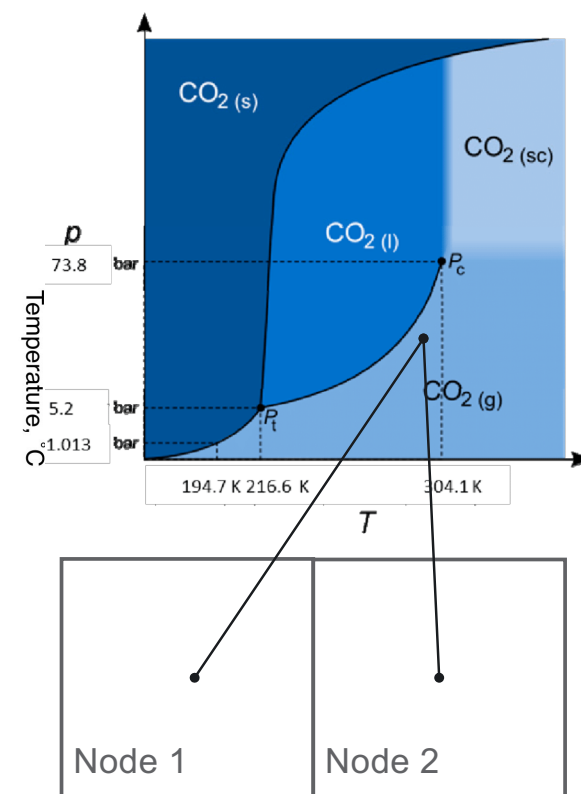
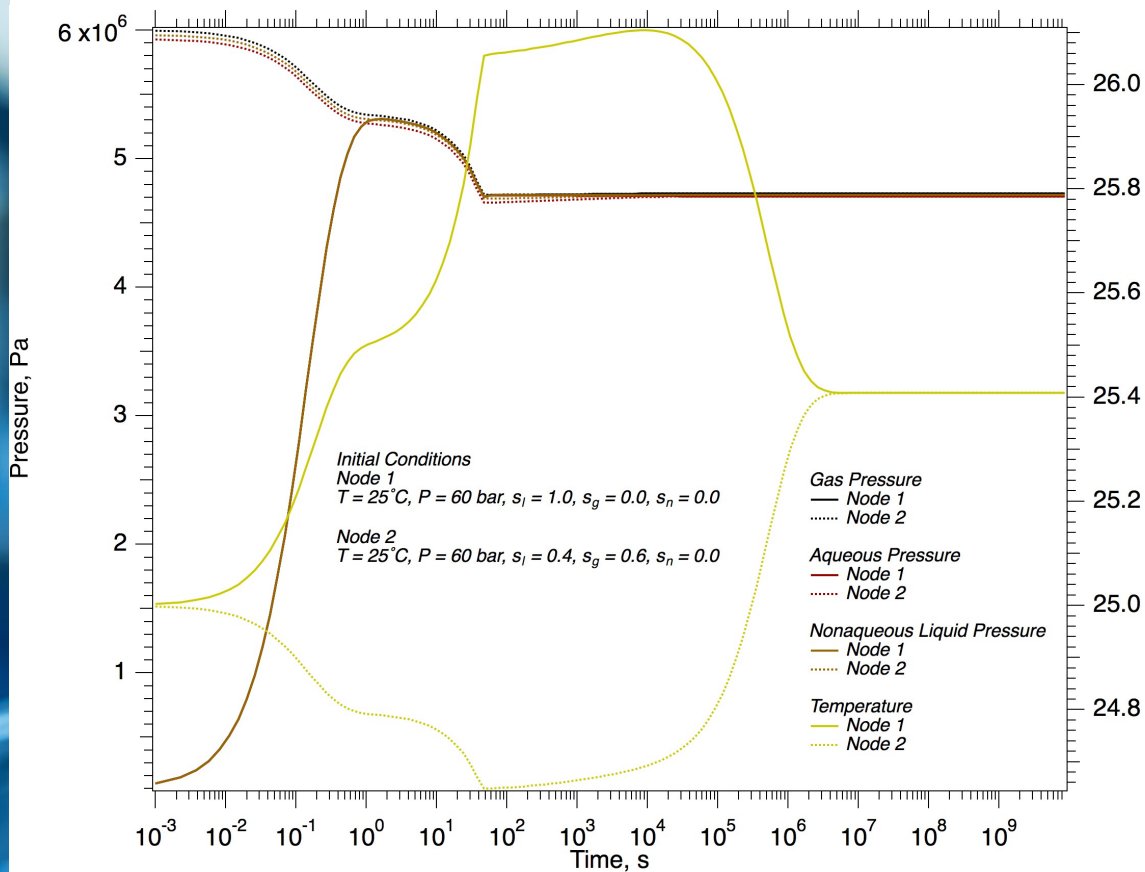
Phase Condition	Energy Equation	Water Mass Equation	CO ₂ Mass Equation	Salt Mass Equation
L	T	P_ℓ	ω_ℓ^C	y_ℓ^S
G	T	P_v^W	P_g	T_m^S
Gsc	T	P_v^W	P_g	T_m^S
N	T	P_v^W	P_n	T_m^S
LG	T	P_ℓ	P_g	y_ℓ^S
LGt	T	P_ℓ	s_{gt}	y_ℓ^S
LGsc	T	P_ℓ	P_g	y_ℓ^S
LGtsc	T	P_ℓ	s_{gt}	y_ℓ^S
LN	T	P_ℓ	P_n	y_ℓ^S
LNt	T	P_ℓ	s_{nt}	y_ℓ^S
NG	T	P_v^W	β	T_m^S
LNG	T	P_ℓ	β	y_ℓ^S
LNGt	T	$s_{gt} + s_{nt}$	β	y_ℓ^S



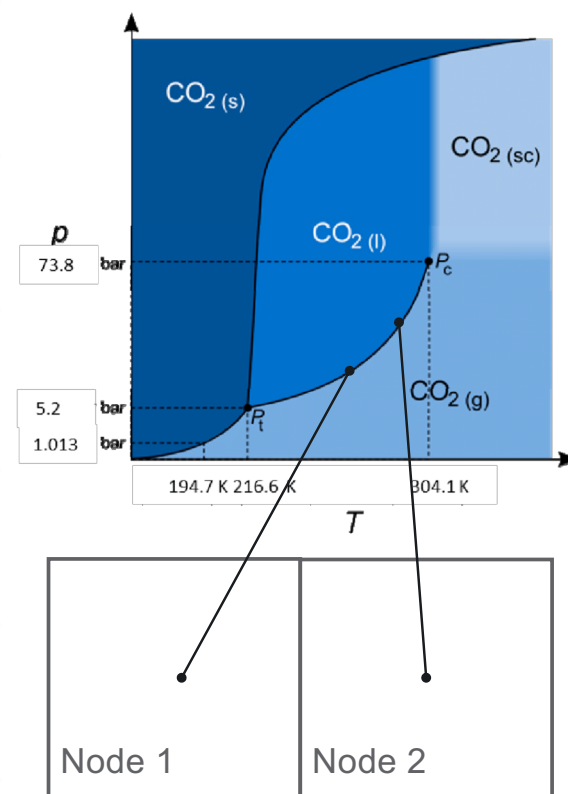
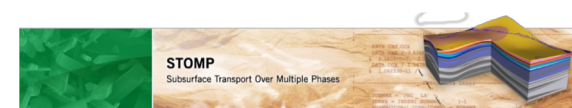
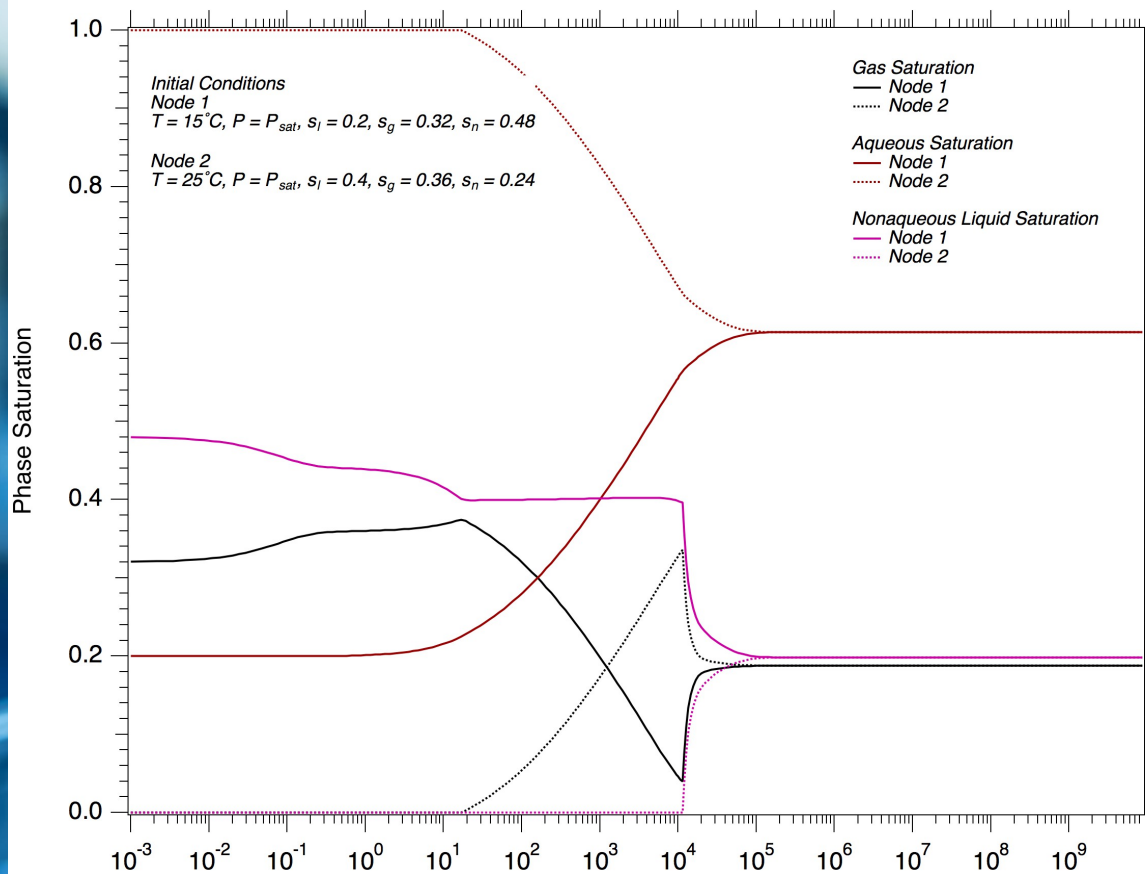
Code Validation via False Transients to Equilibrium Conditions



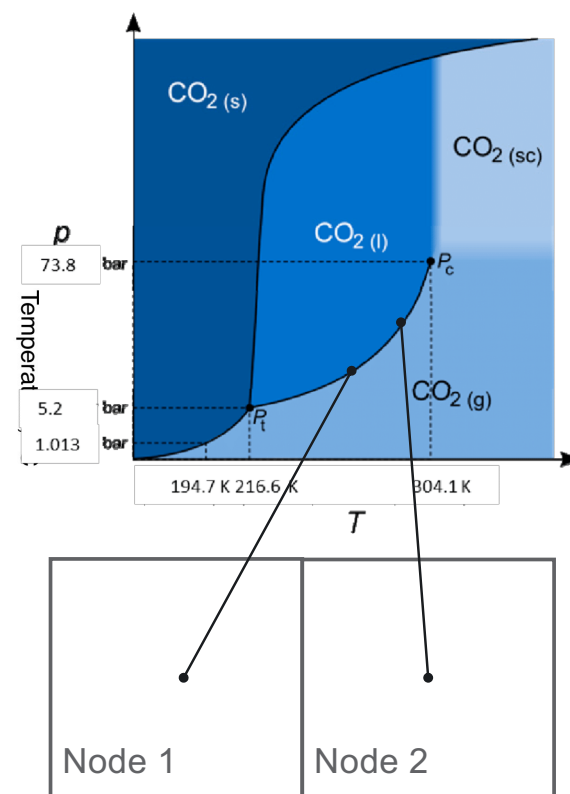
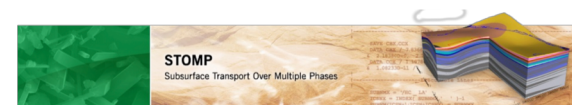
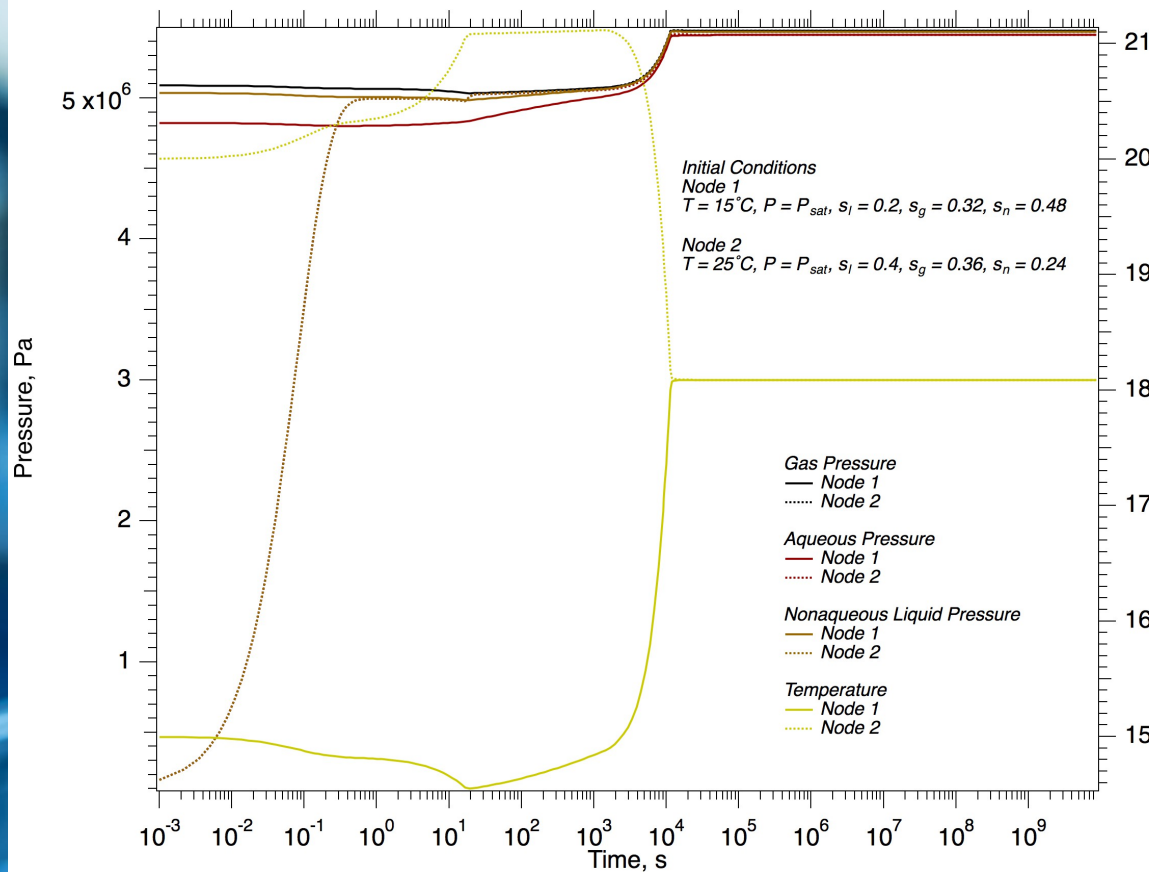
Code Validation via False Transients to Equilibrium Conditions



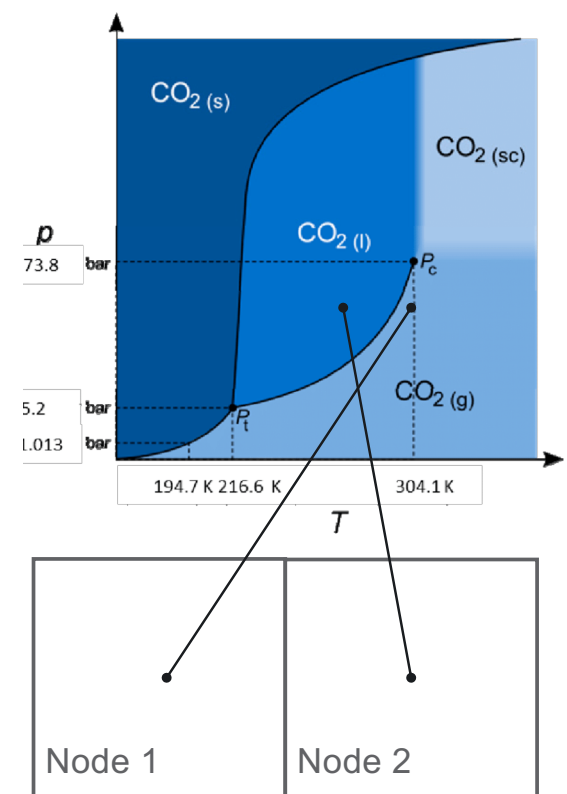
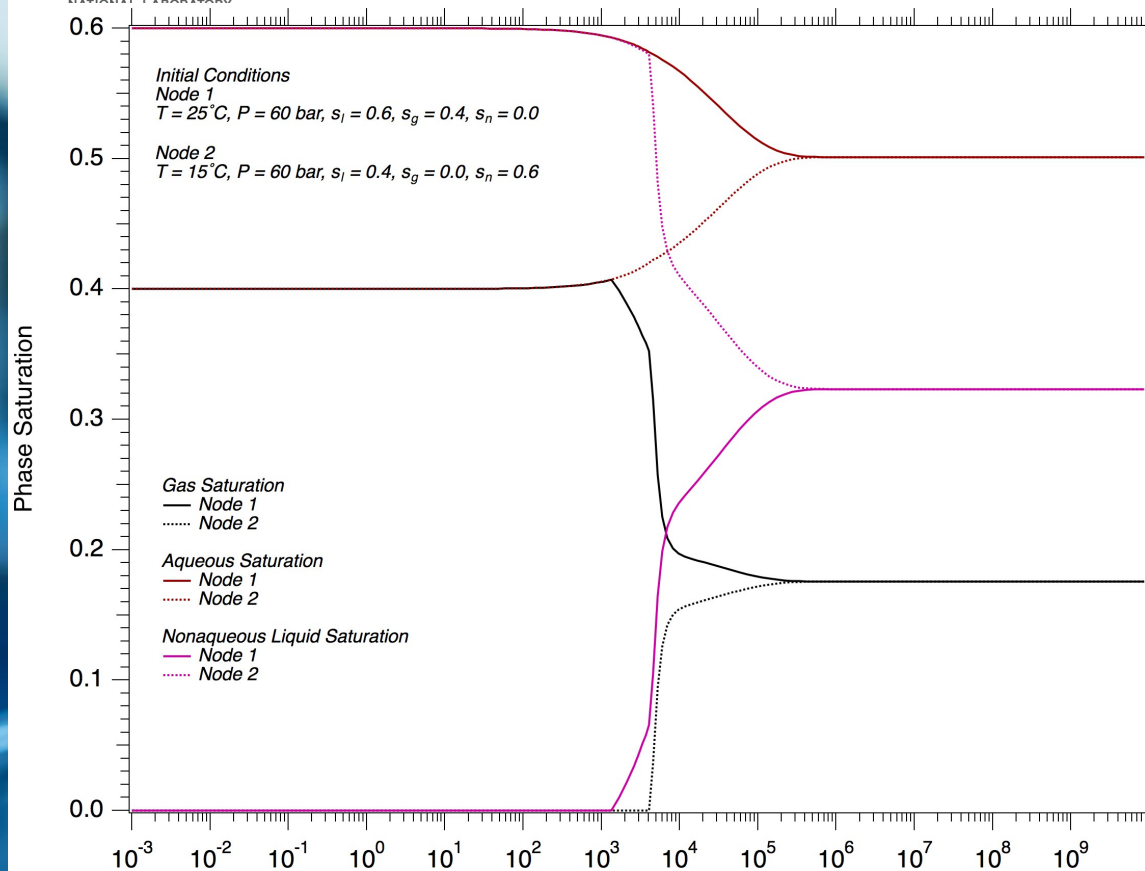
Code Validation via False Transients to Equilibrium Conditions



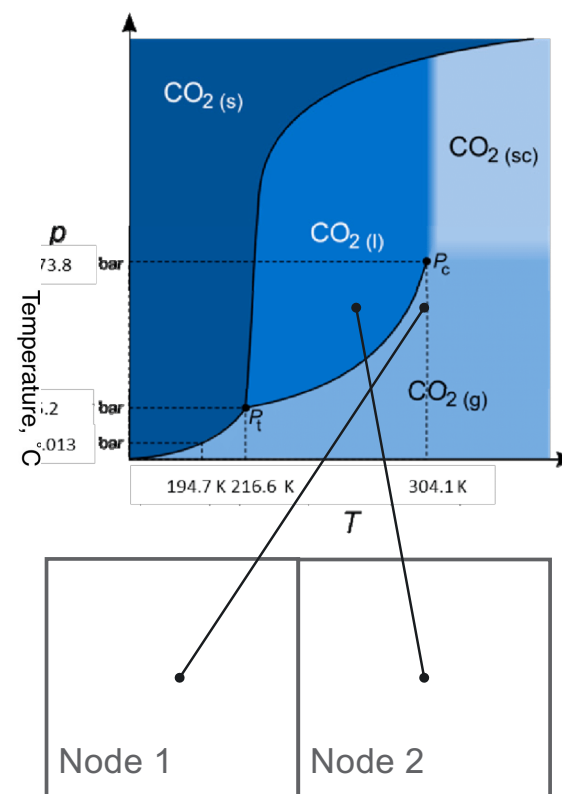
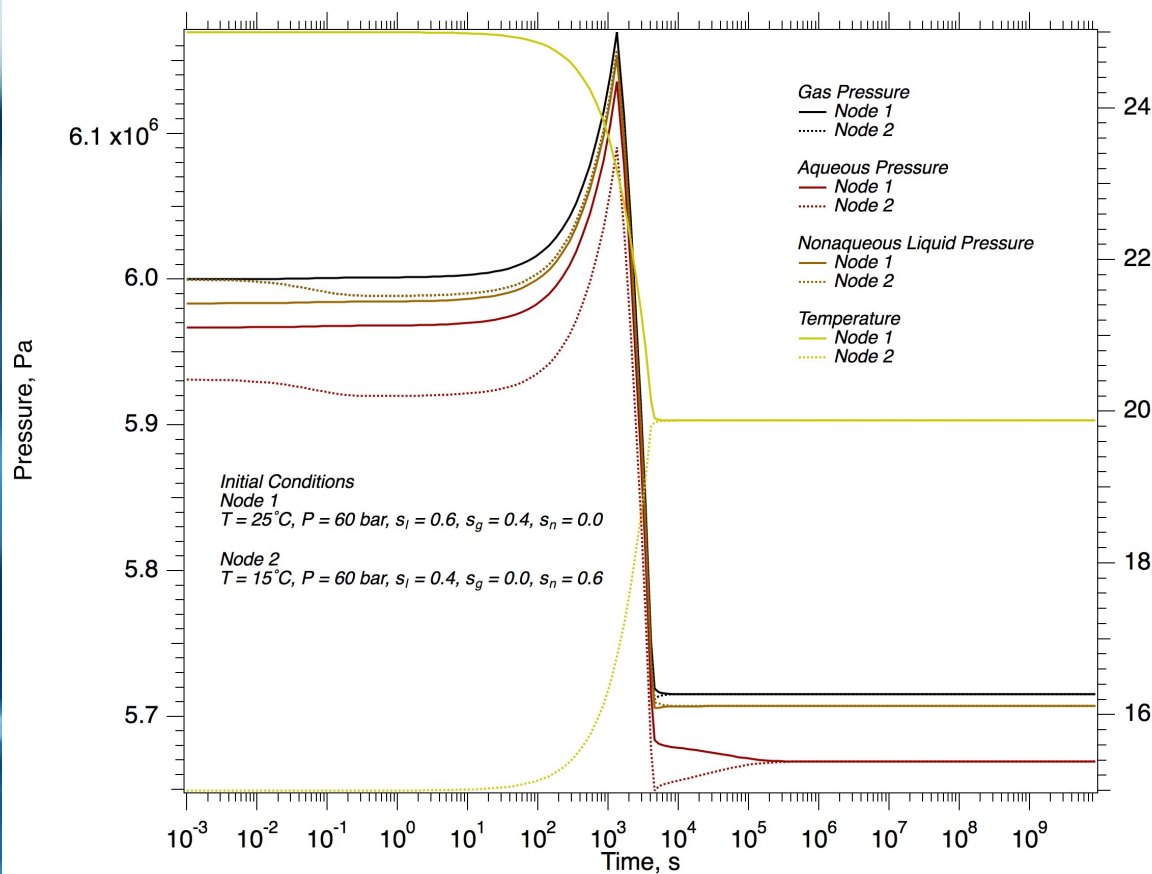
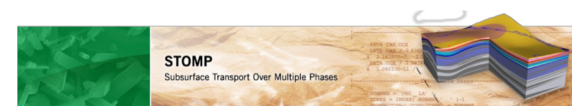
Code Validation via False Transients to Equilibrium Conditions



Code Validation via False Transients to Equilibrium Conditions



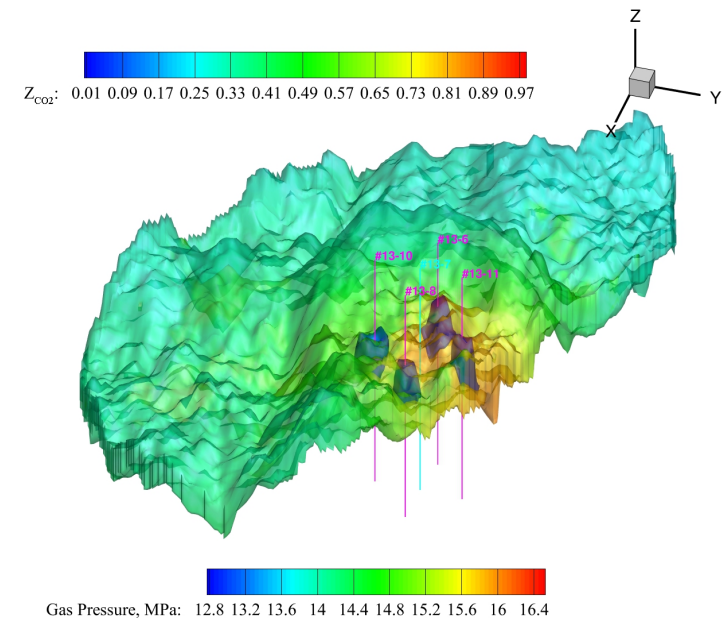
Code Validation via False Transients to Equilibrium Conditions



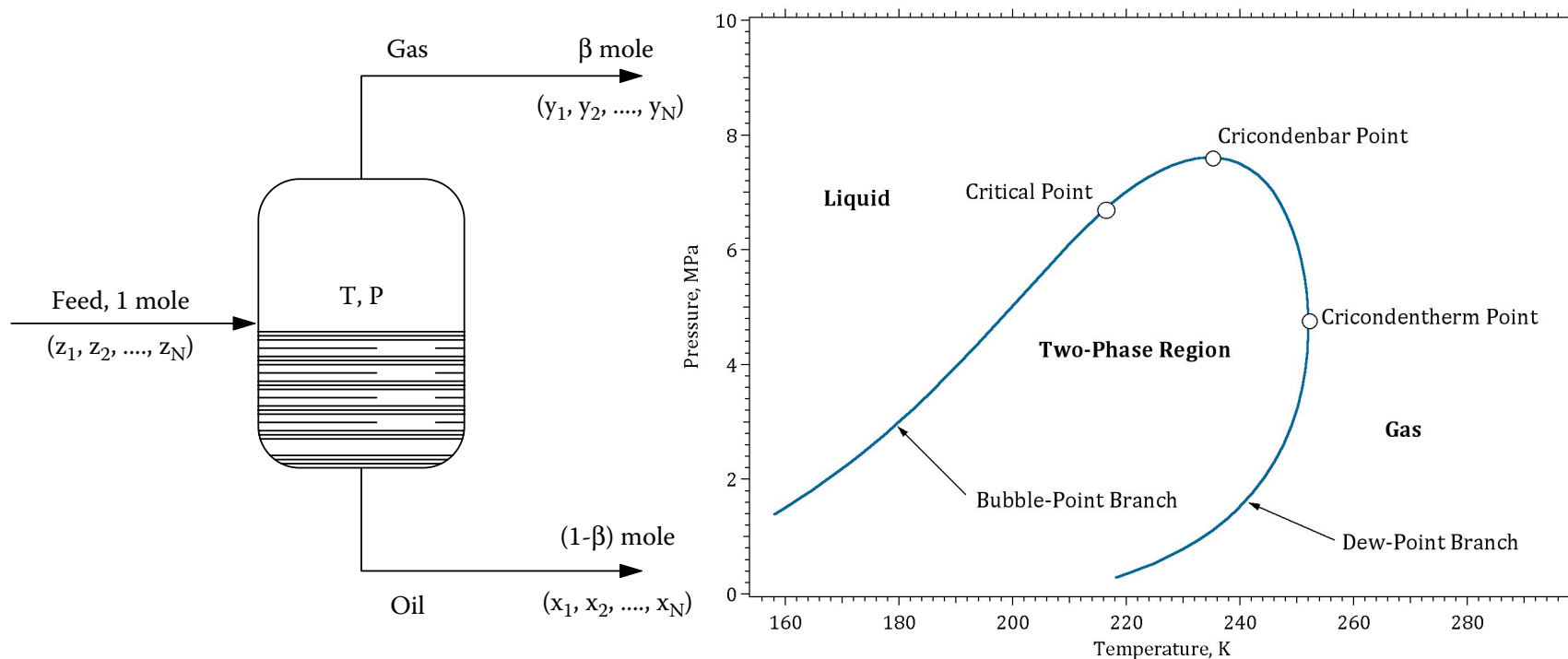
Three-Phase System for Enhanced Oil Recovery: Basics



- Mobile phases
 - Aqueous (water, CO₂, salt)
 - Nonaqueous liquid (CO₂, CH₄, n-petroleum components)
 - Gas (CO₂, CH₄, n-petroleum components)
- Phase equilibria from cubic equation of state
 - Peng-Robinson
 - Soave-Redlich-Kwong
- Phase properties
 - Cubic equation of state
 - Corresponding state method
 - Empirical correlations

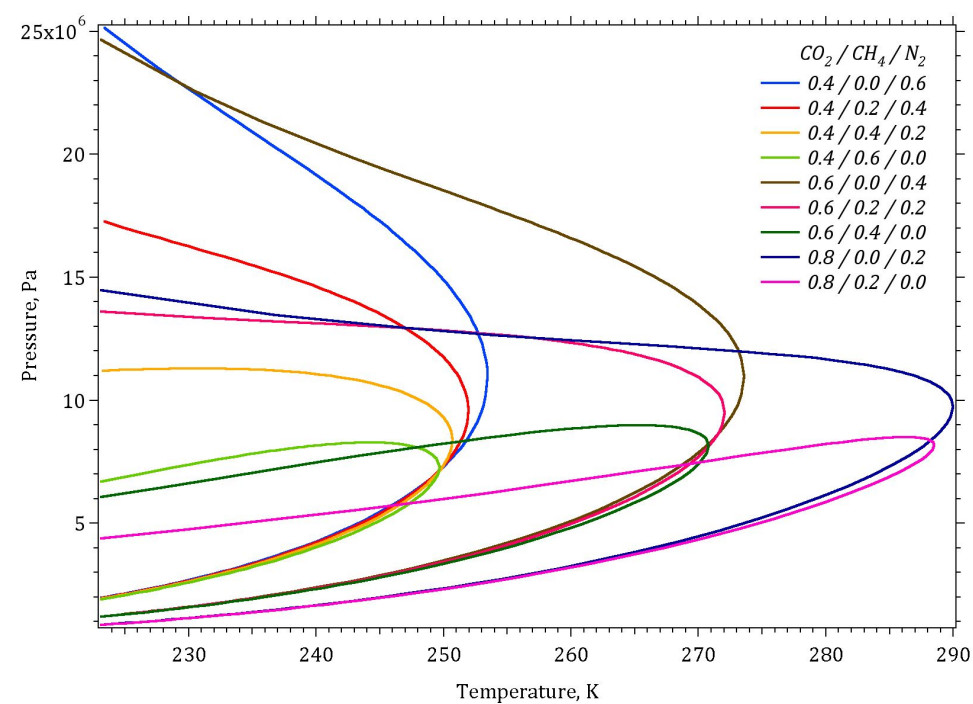
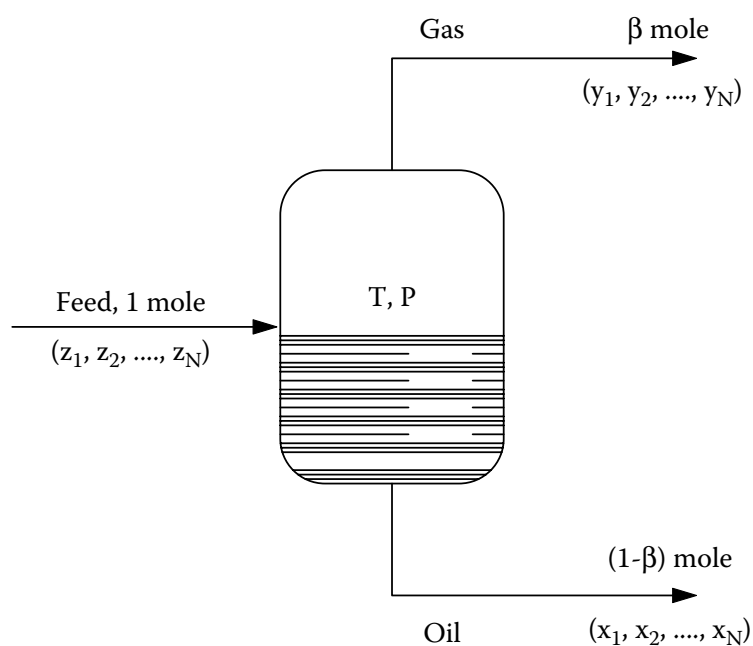


Three-Phase System for Enhanced Oil Recovery: Phase Equilibria



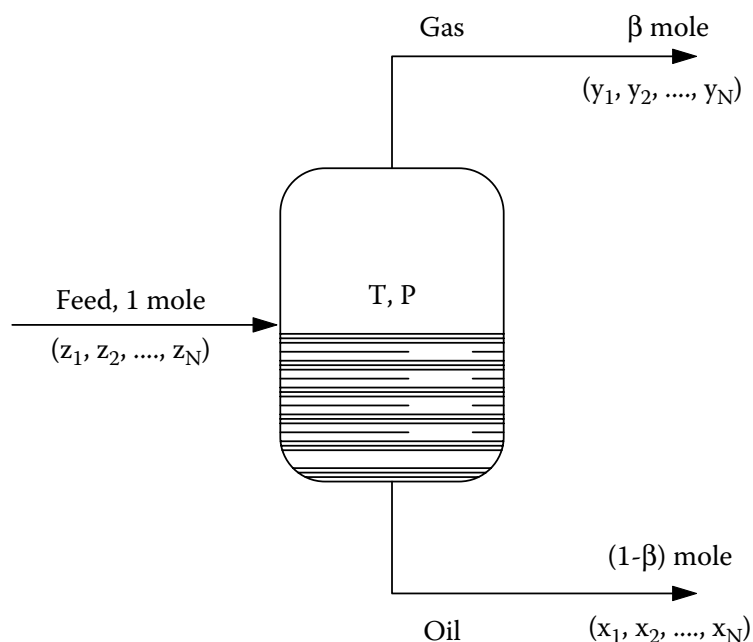
Source: Pedersen, K. S., and P. L. Christensen. 2007. *Phase Behavior of Petroleum Reservoir Fluids*. CRC Taylor & Francis, New York.

Three-Phase System for Enhanced Oil Recovery: Phase Equilibria



Source: Pedersen, K. S., and P. L. Christensen. 2007. *Phase Behavior of Petroleum Reservoir Fluids*. CRC Taylor & Francis, New York.

Three-Phase System for Enhanced Oil Recovery: Michelsen Reference



Source: Pedersen, K. S., and P. L. Christensen. 2007. *Phase Behavior of Petroleum Reservoir Fluids*. CRC Taylor & Francis, New York.



Computers & Chemical Engineering
Volume 16, Supplement 1, May 1992, Pages S19-S29



Phase equilibrium calculations. What is easy and what is difficult?

Michael L. Michelsen

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Abstract

Calculation of phase equilibrium for a mixture of given composition requires specification of two process variables, typically chosen among the following: Temperature, pressure, vapour fraction, enthalpy, entropy or volume. The difficulties associated with solving the equilibrium equations are strongly related to the chosen selection of these process variables. The aim of the present paper is to outline the characteristics associated with the different types of specification in order to provide guidelines for efficient and robust solution algorithms.

Three-Phase System for Enhanced Oil Recovery: Phase Conditions and Primary Variables

- State #1 (aqueous saturated)

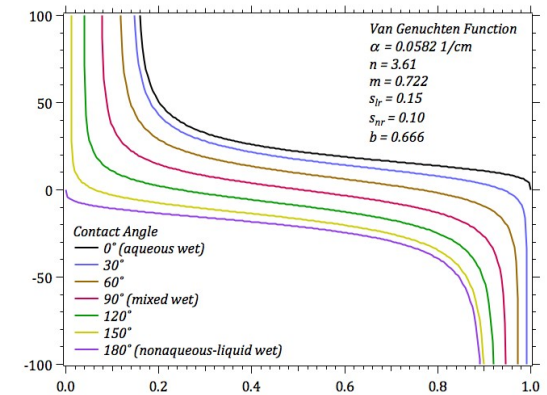
$$T, P_l, \omega_l^{\text{CO}_2}, m^{\text{CH}_4}, m^i, \omega_l^{\text{salt}} \text{ for } i = 3, n$$

- State #2 (aqueous + nonaqueous)

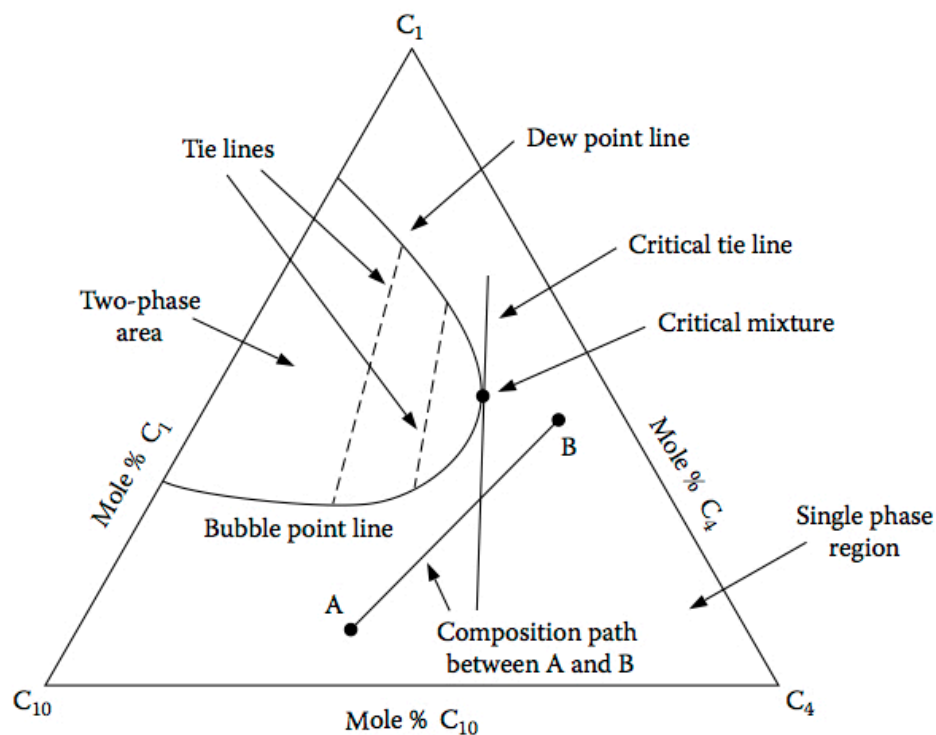
$$T, P_l, P_{ng}, \chi_t^{\text{CO}_2}, \chi_t^{\text{CH}_4}, \chi_t^i, \omega_l^{\text{salt}} \text{ for } i = 3, n-1$$

- State #3 (nonaqueous saturated)

$$T, m^{\text{water}}, P_{ng}, \chi_t^{\text{CO}_2}, \chi_t^{\text{CH}_4}, \chi_t^i, m^{\text{salt}} \text{ for } i = 3, n-1$$



Three-Phase System for Enhanced Oil Recovery – First Contact



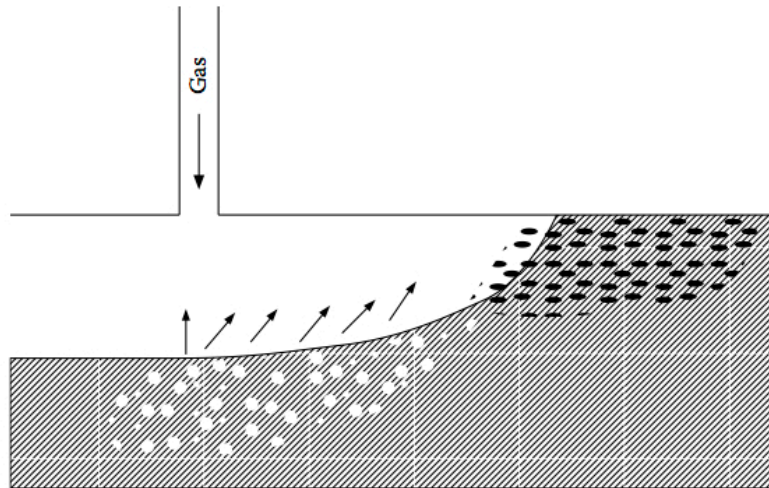
A – Composition of Oil

B – Composition of Gas

Fixed temperature & pressure

Source: Pedersen, K. S., and P. L. Christensen. 2007. *Phase Behavior of Petroleum Reservoir Fluids*. CRC Taylor & Francis, New York.

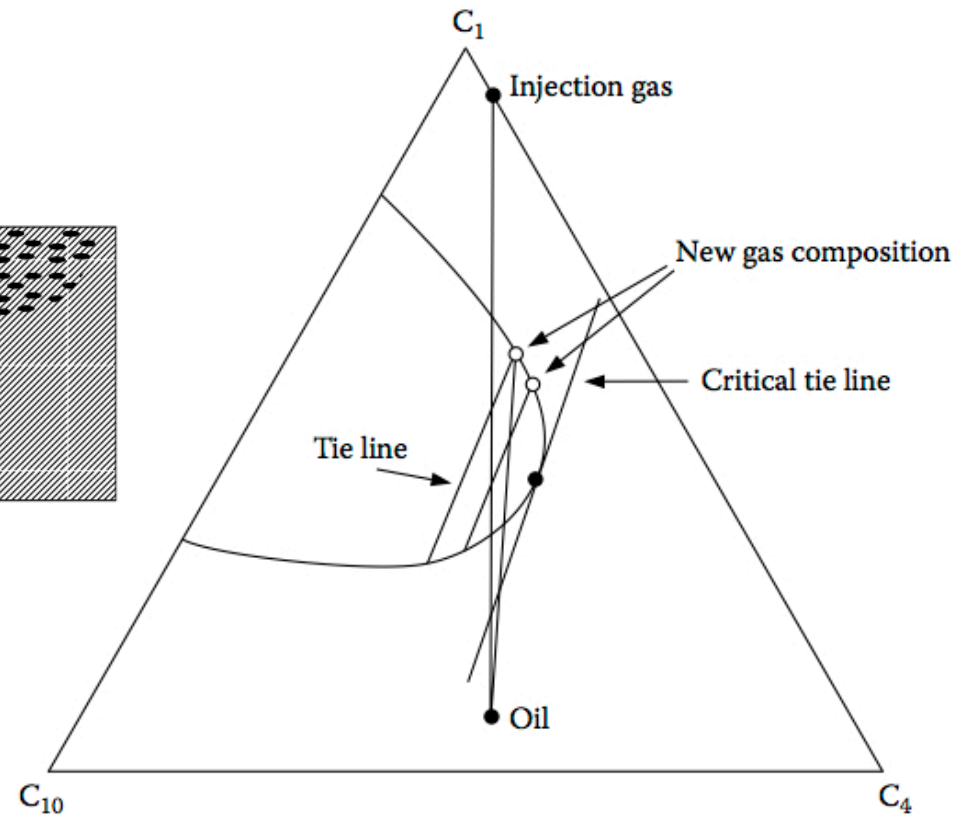
Three-Phase System for Enhanced Oil Recovery – Vaporization Drive



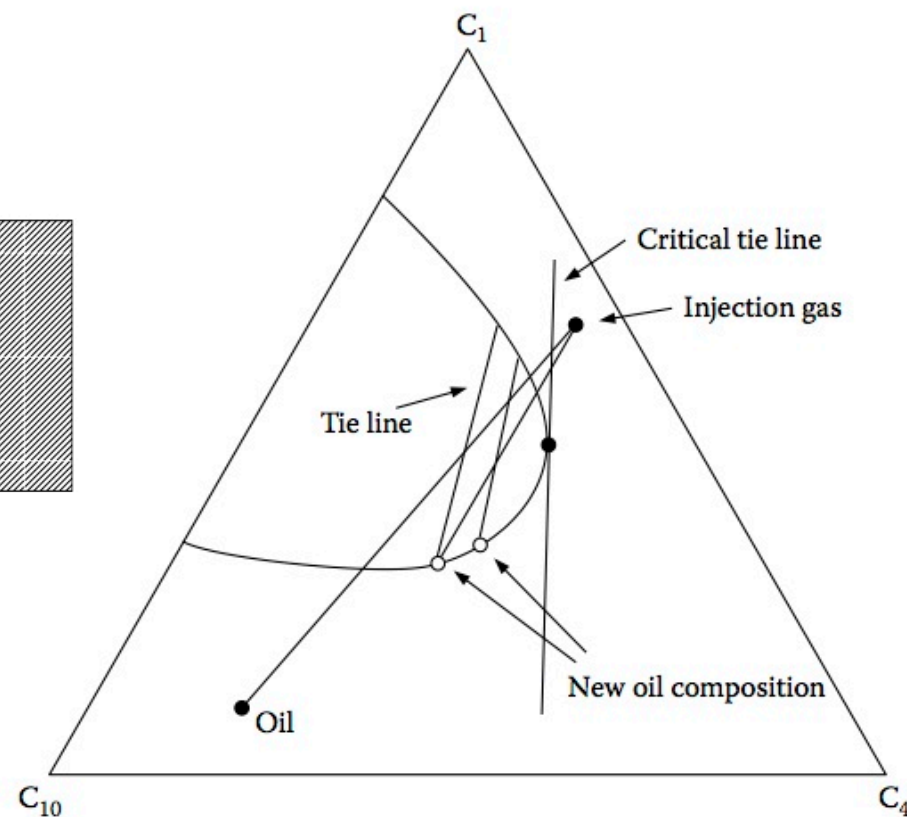
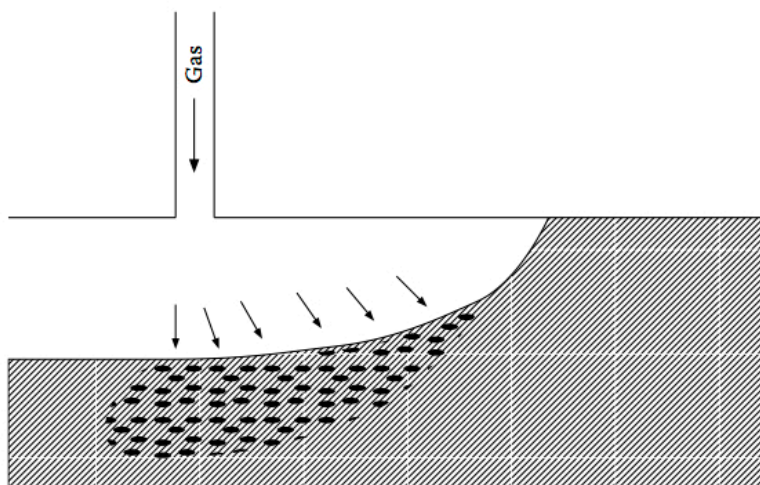
A – Composition of Oil

B – Composition of Gas

Fixed temperature & pressure



Three-Phase System for Enhanced Oil Recovery – Condensing Drive

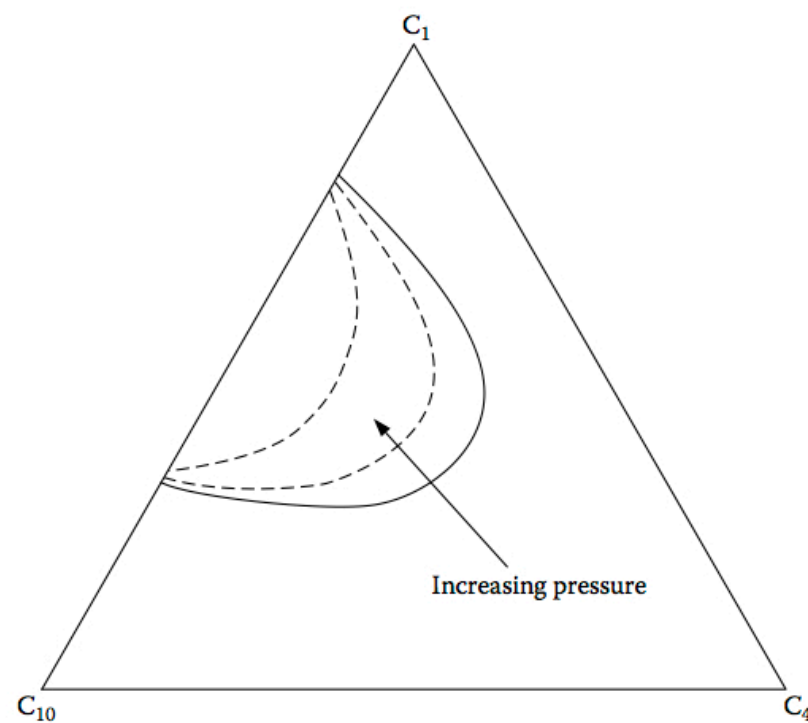
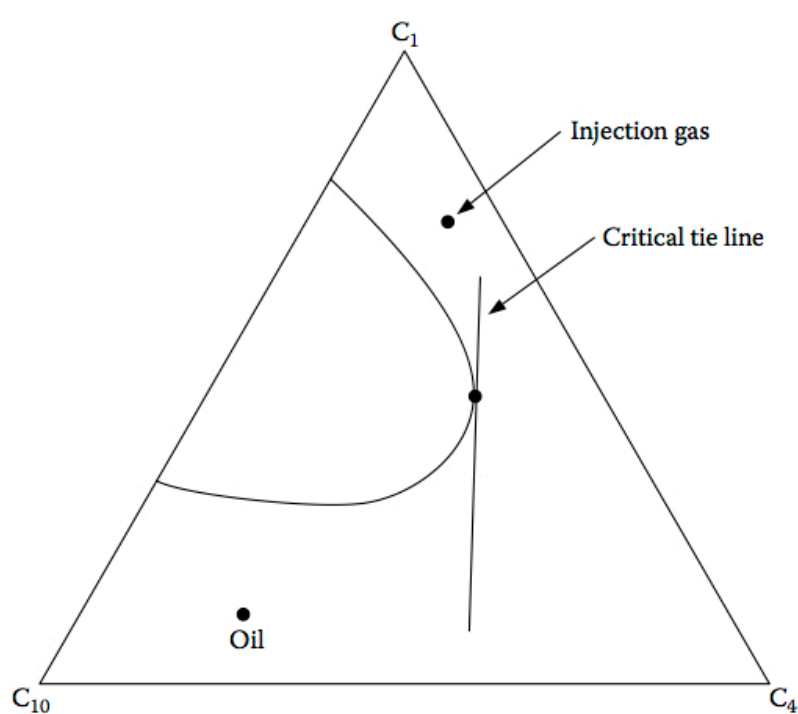


A – Composition of Oil

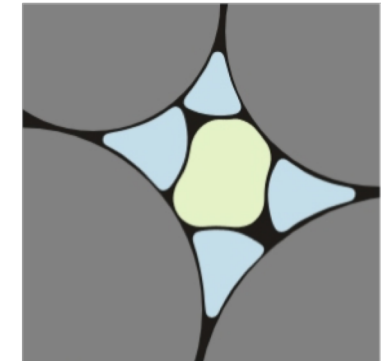
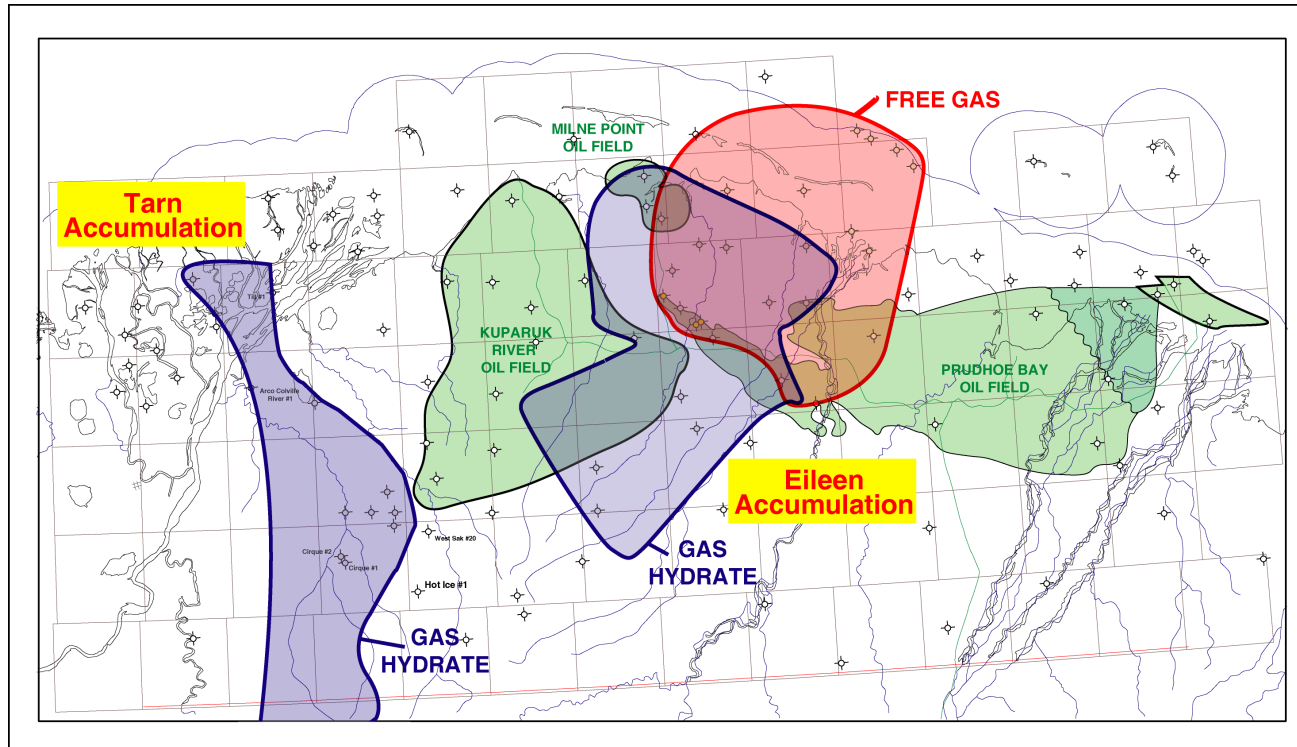
B – Composition of Gas

Fixed temperature & pressure

Three-Phase System for Enhanced Oil Recovery – Miscibility & Pressure



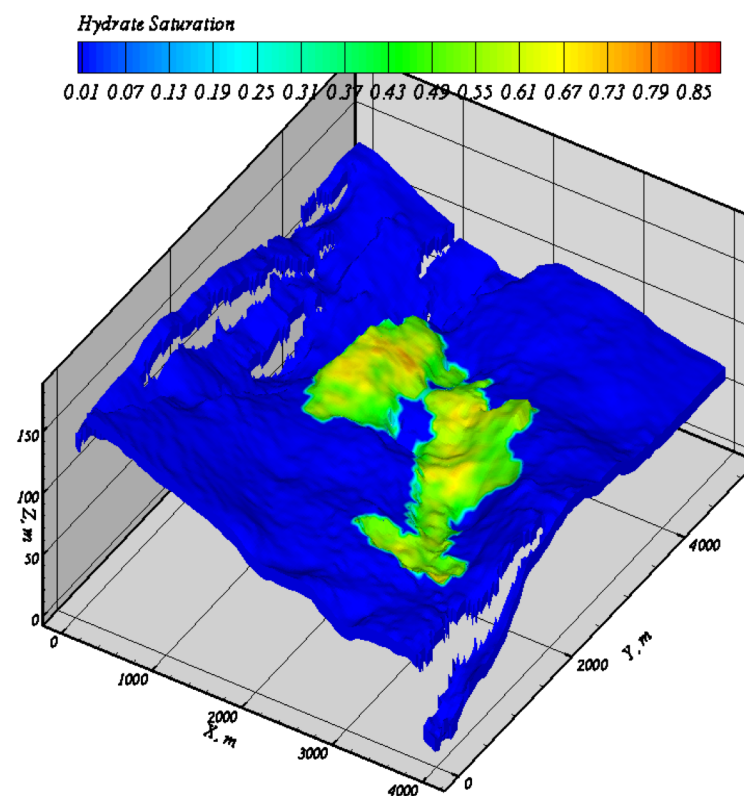
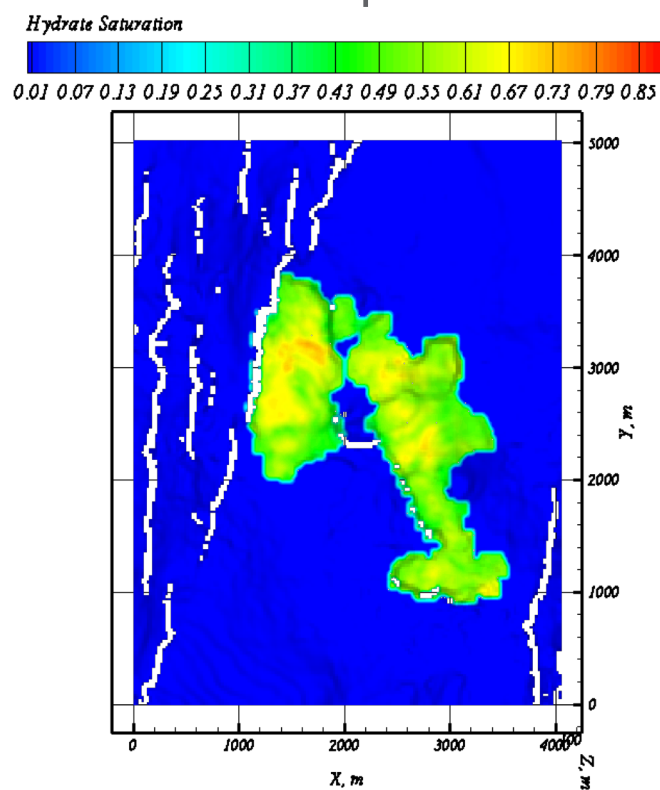
Gas Hydrate Systems



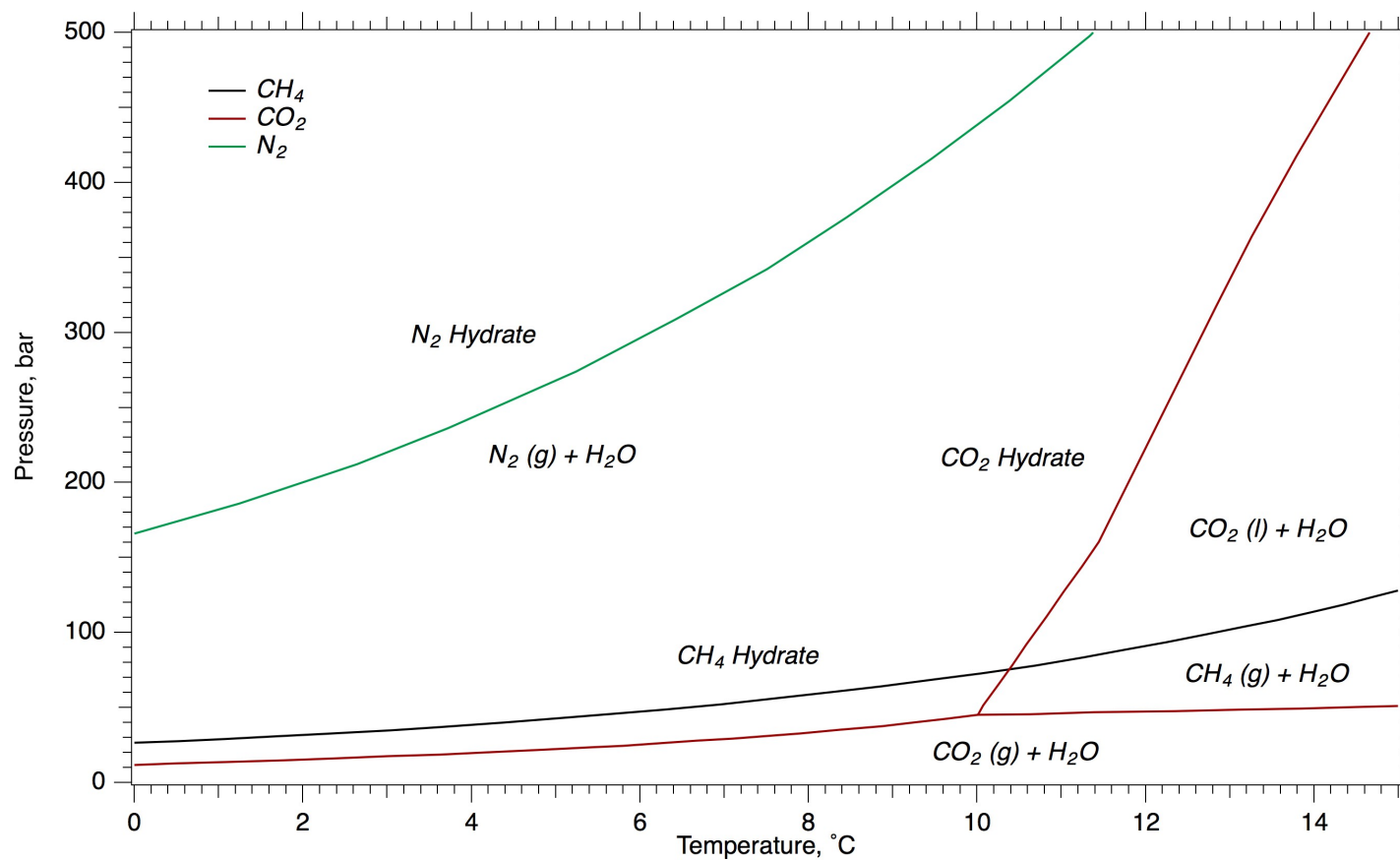
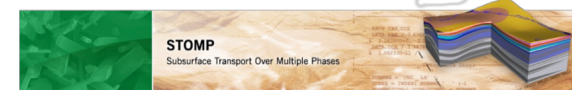
 Gas	 Grain
 Hydrate	 Aqueous



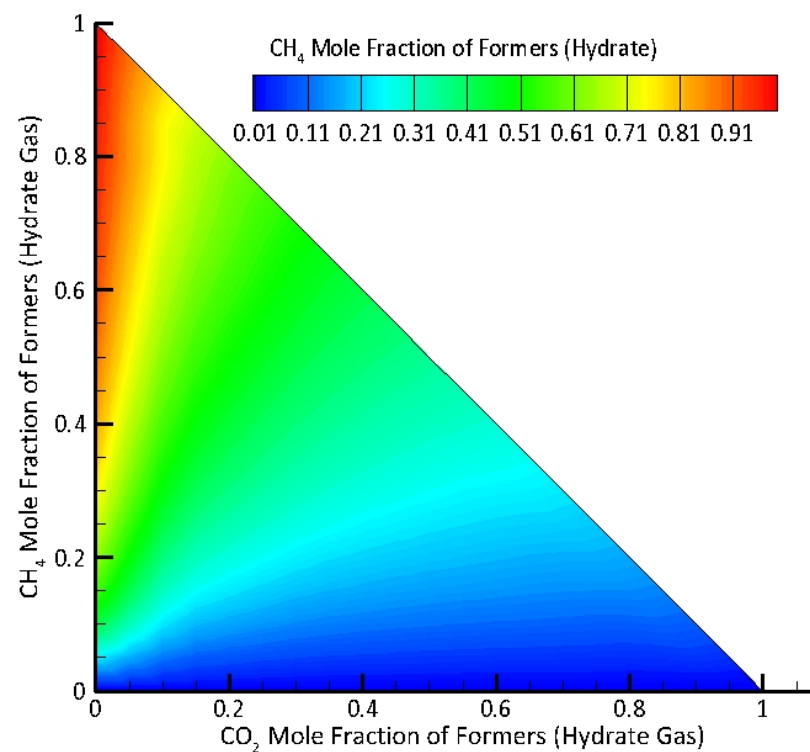
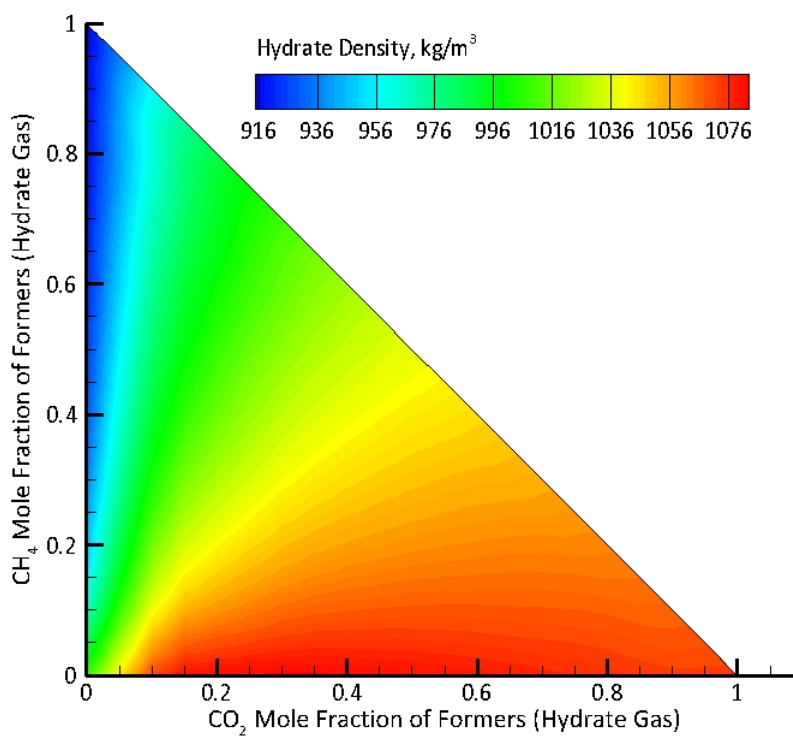
Gas Hydrate Systems: Hydrate Distributions on the Alaska Northslope



Gas Hydrate Systems – Hydrate Phase Equilibria



Gas Hydrate Systems – Ternary Hydrate Properties from Tables



Gas Hydrate Systems – Phase Conditions and Primary Variables



Phase Condition #10 Series $s_h = 0.0, s_n + s_g = 0.0, s_\ell + s_i = 1.0$

Energy	T	Temperature
Water Mass	P	Pressure
Mobile CO ₂ Mass	$P_v^{CO_2}$	CO ₂ Vapor Pressure
Mobile CH ₄ Mass	$P_v^{CH_4}$	CH ₄ Vapor Pressure
Mobile N ₂ Mass	$P_v^{N_2}$	N ₂ Vapor Pressure
Hydrate CO ₂ Mass	$M_h^{CO_2}$	Hydrate CO ₂ Mass
Hydrate CH ₄ Mass	$M_h^{CH_4}$	Hydrate CO ₂ Mass
Hydrate N ₂ Mass	$M_h^{N_2}$	Hydrate CO ₂ Mass
Salt	y_ℓ^S	Brine Mass Fraction of Total Salt

Gas Hydrate Systems – Phase Conditions and Primary Variables



Phase Condition #20 Series $s_h = 0.0, s_n + s_g > 0.0, s_\ell + s_i < 1.0$

Energy	T	Temperature
Water Mass	$s_\ell + s_i$	Aqueous + Ice Saturation
Mobile CO ₂ Mass	$z_m^{CO_2}$ or P	CO ₂ Mole Fraction or Pressure
Mobile CH ₄ Mass	$z_m^{CH_4}$ or P	CH ₄ Mole Fraction or Pressure
Mobile N ₂ Mass	$z_m^{N_2}$ or P	N ₂ Mole Fraction or Pressure
Hydrate CO ₂ Mass	$M_h^{CO_2}$	Hydrate CO ₂ Mass
Hydrate CH ₄ Mass	$M_h^{CH_4}$	Hydrate CO ₂ Mass
Hydrate N ₂ Mass	$M_h^{N_2}$	Hydrate CO ₂ Mass
Salt	y_ℓ^S	Brine Mass Fraction of Total Salt

Gas Hydrate Systems – Phase Conditions and Primary Variables



Phase Condition #30 Series $s_h > 0.0, s_n + s_g > 0.0, s_\ell + s_i < 1.0$

Energy	T	Temperature
Water Mass	$s_\ell + s_i$	Aqueous + Ice Saturation
Mobile CO ₂ Mass	$z_m^{CO_2}$ or P	CO ₂ Mole Fraction or Pressure
Mobile CH ₄ Mass	$z_m^{CH_4}$ or P	CH ₄ Mole Fraction or Pressure
Mobile N ₂ Mass	$z_m^{N_2}$ or P	N ₂ Mole Fraction or Pressure
Hydrate CO ₂ Mass	$\psi_h^{CO_2}$ or s_h	CO ₂ Mole Fraction of Former
Hydrate CH ₄ Mass	$\psi_h^{CH_4}$ or s_h	CH ₄ Mole Fraction of Former
Hydrate N ₂ Mass	$\psi_h^{N_2}$ or s_h	N ₂ Mole Fraction of Former
Salt	y_ℓ^s	Brine Mass Fraction of Total Salt

Gas Hydrate Systems – Phase Conditions and Primary Variables



Phase Condition #40 Series $s_h > 0.0, s_n + s_g = 0.0, s_\ell + s_i < 1.0$

Energy	T	Temperature
Water Mass	P	Pressure
Mobile CO ₂ Mass	$P_v^{CO_2}$	CO ₂ Vapor Pressure
Mobile CH ₄ Mass	$P_v^{CH_4}$	CH ₄ Vapor Pressure
Mobile N ₂ Mass	$P_v^{N_2}$	N ₂ Vapor Pressure
Hydrate CO ₂ Mass	$\psi_h^{CO_2}$ or s_h	CO ₂ Mole Fraction of Former
Hydrate CH ₄ Mass	$\psi_h^{CH_4}$ or s_h	CH ₄ Mole Fraction of Former
Hydrate N ₂ Mass	$\psi_h^{N_2}$ or s_h	N ₂ Mole Fraction of Former
Salt	y_ℓ^s	Brine Mass Fraction of Total Salt

Gas Hydrate Systems – Phase Transitions



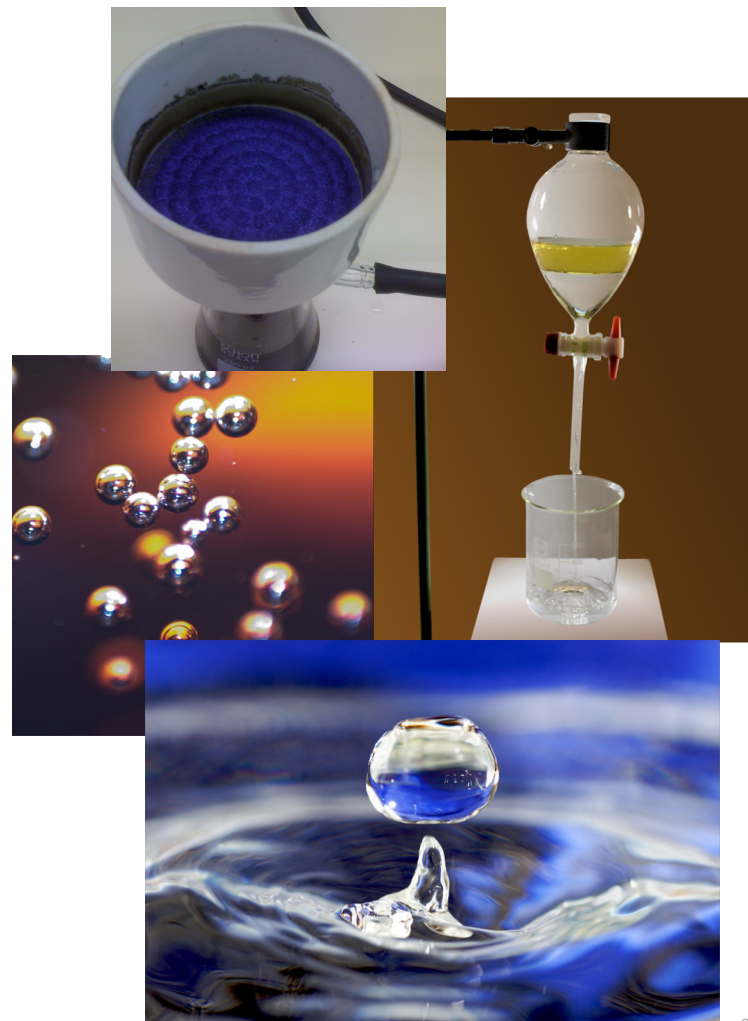
Phase Condition #10 Series $s_h = 0.0, s_n + s_g = 0.0, s_\ell + s_i = 1.0$

- Assume a hydrate phase exists (common approach!)
- Compute a hydrate equilibrium pressure $P_h^{eq} = func[T, \psi_h^{CO_2}, \psi_h^{CH_4}, \psi_h^{N_2}]$
- Compute the vapor pressure of formers $P_v = P_v^{CO_2} + P_v^{CH_4} + P_v^{N_2}$
- Compute the total gas pressure $P_g = P_v^{CO_2} + P_v^{CH_4} + P_v^{N_2} + P_v^{H_2O}$
- *if* ($P_v > P_h^{eq}$) *then* hydrate forms
- *if* ($P_g > P_\ell + P_{entry}$) *then* hydrate forms

Phase Condition #30 Series $s_h > 0.0, s_n + s_g > 0.0, s_\ell + s_i < 1.0$

Takeaways / Conclusions

- Primary variable switching is an effective scheme for modeling phase transitions
- Select primary variables that yield direct calculations of all secondary variables
- Phase equilibria calculations are harder than they appear
- Discontinuities slow convergence
- Be creative in defining primary variables and phase conditions





Thank you

