

Getting to Know the Unknown Unknowns

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Vancouver, May 1, 2015



Do We Know What We Don't Know?



- There are known knowns
 - ▶ there are things we know we know
- There are known unknowns
 - ▶ we know there are some things we do not know
- **But there are also unknown unknowns**
 - ▶ **the ones we don't know we don't know**

Do We Know What We Don't Know?

It is the latter category that tends to be the difficult ones.



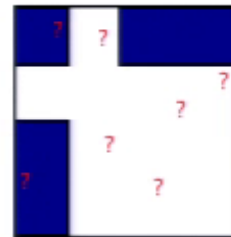
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 - ▶ there are things we know we know
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Where Is Data Mining?

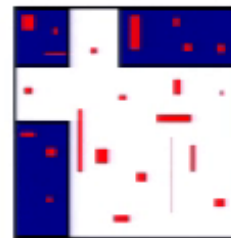
- Known knowns
 - ▶ noise-free data



- Known unknowns
 - ▶ missing values



- Unknown unknowns
 - ▶ values (possibly) flipped due to noise



Unknown Unknowns: a Closer Look

- False positives ($0 \rightarrow 1$) and false negatives ($1 \rightarrow 0$) are often not equally likely
- E.g. some 0s might be due to a lack of observation



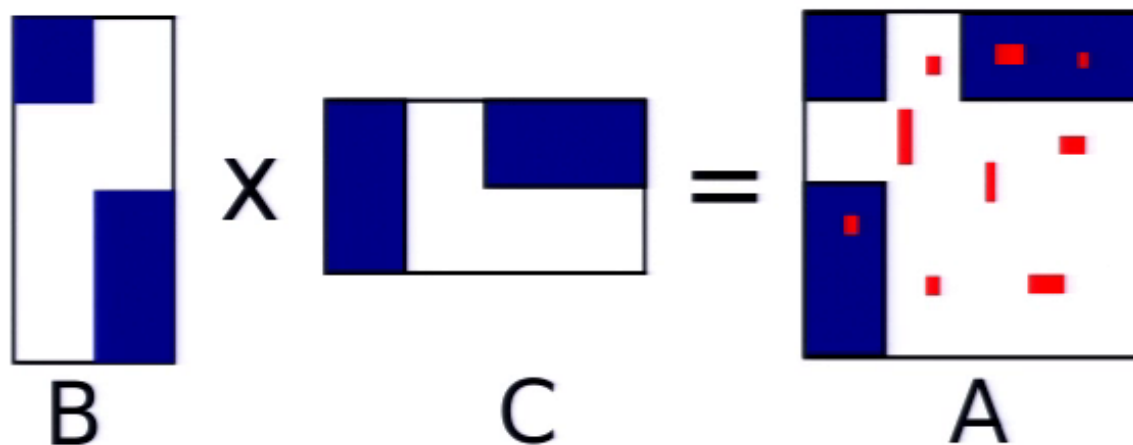
- Example data
 - ▶ columns are locations
 - ▶ rows are animal species
 - ▶ 1 if present, 0 if not

In This Talk

- Represent the data as a union of noisy patterns
- Nassau: a new algorithm for BMF
 - ▶ minimizes the description length
 - ▶ uses MDL to find the rank (number of patterns)
 - ▶ dynamically corrects its previous mistakes when new information is found

Summarizing Noisy Patterns Using BMF

- Binary data with noise
- Decompose A into a Boolean product of low rank factors + noise



Summarizing Noisy Patterns Using BMF

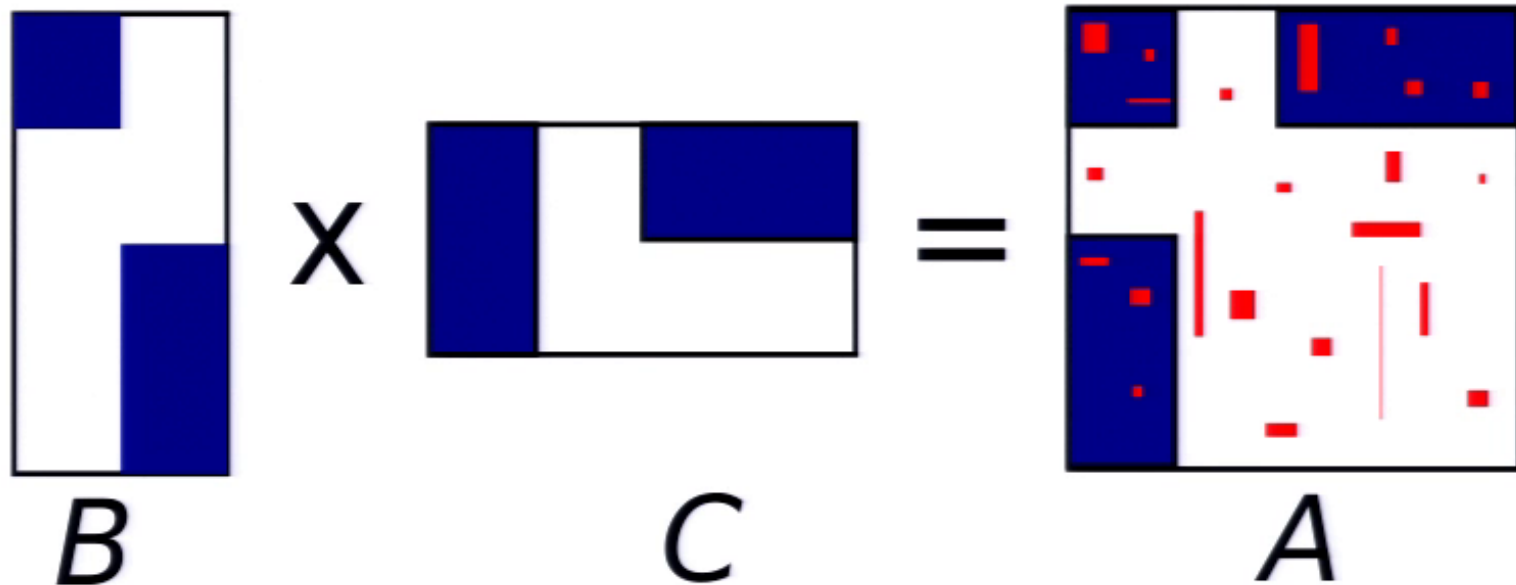
- Binary data with noise
- Decompose A into a Boolean product of low rank factors + noise

$$\begin{bmatrix} \text{blue} \\ \text{white} \end{bmatrix} \times \begin{bmatrix} \text{blue} & \text{white} & \text{blue} \end{bmatrix} + \begin{bmatrix} \text{white} \\ \text{blue} \end{bmatrix} \times \begin{bmatrix} \text{blue} & \text{white} \end{bmatrix} = \begin{bmatrix} \text{blue} & \text{white} & \text{blue} \\ \text{white} & \text{white} & \text{white} \\ \text{blue} & \text{white} & \text{white} \end{bmatrix}$$

- A can now be seen as a sum of rank-1 matrices (blocks)

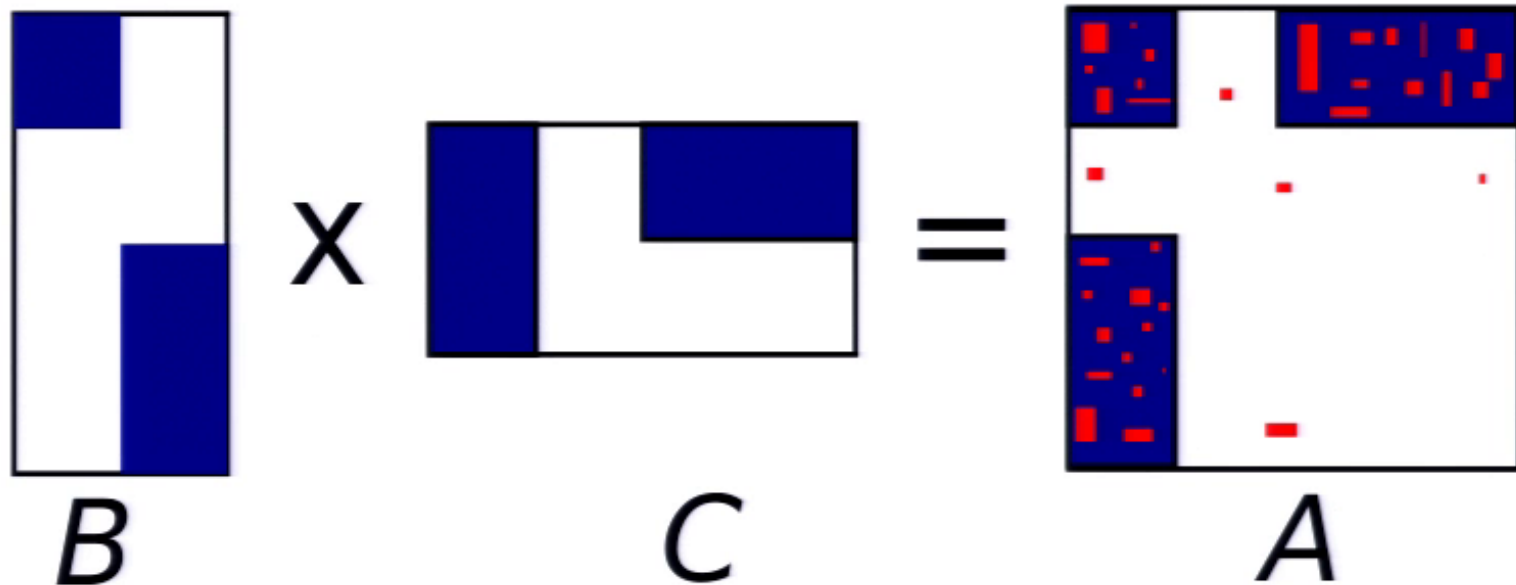
Different Kinds of Noise

- In ideal world
 - ▶ use 0/1 error as the cost
 - ▶ treat additive ($0 \rightarrow 1$) and destructive ($1 \rightarrow 0$) noise equally



Different Kinds of Noise

- In ideal world
 - ▶ use 0/1 error as the cost
 - ▶ treat additive ($0 \rightarrow 1$) and destructive ($1 \rightarrow 0$) noise equally
- In real world
 - ▶ additive and destructive noise are likely to be imbalanced
 - ▶ need to find the right ratio



BMF with MDL

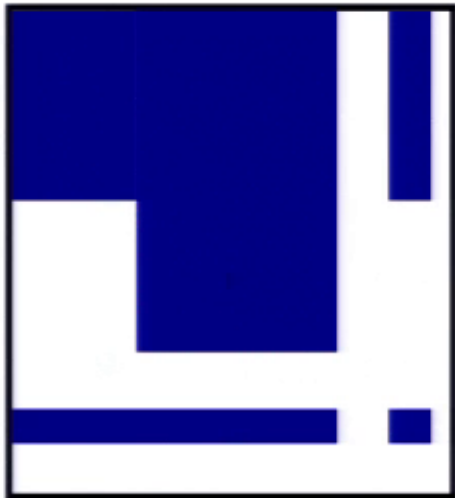
- Objectives
 - ▶ isolate flipped elements (unknown unknowns)
 - ▶ find optimal rank for the data
- Minimum description length (MDL)
 - ▶ patterns in the data can be used to compress it
 - ▶ \Rightarrow the more we compressed the data, the more we learned about it
- Encoding BMF
 - ▶ $A = B \circ C + E$, where E is the error matrix
 - ▶ total description length $L(A, B, C) = L(B) + L(C) + L(E)$

Algorithm

- Nassau: a new BMF algorithm
- directly optimizes the description length
 - ▶ helps to deal with the imbalance between different types of noise
- nonhierarchical
 - ▶ rank- k decomposition doesn't have to be a part of rank- $(k + 1)$ decomposition
 - ▶ helps to fix earlier mistakes

Algorithm: Factor Updates Example

• Data



• Factors



• Result



Algorithm: Factor Updates Example

• Data



• Factors

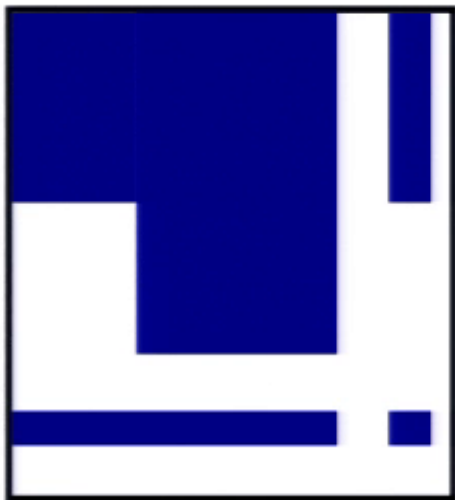


• Result

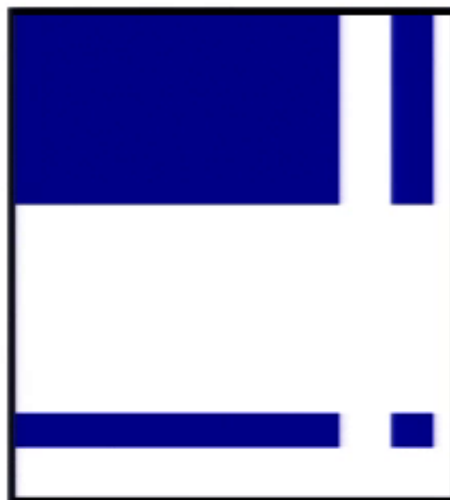


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Algorithm: Factor Updates Example

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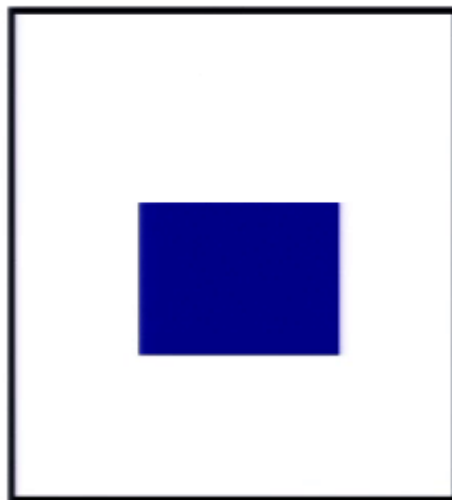


Algorithm: Factor Updates Example

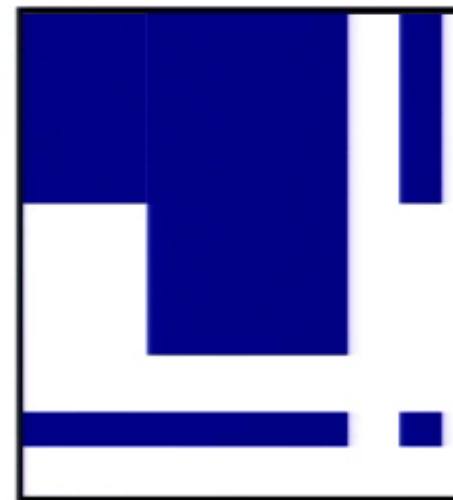
• Data



• Factors



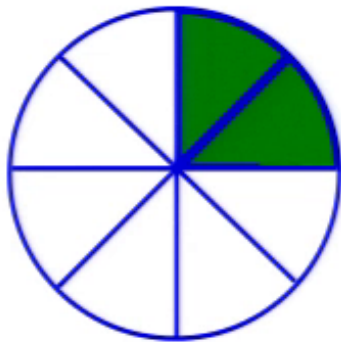
• Result



Algorithm: Summary

- Nassau

- ▶ optimize the description length
- ▶ add new block while the cost improves
- ▶ update previous blocks in a cyclic fashion

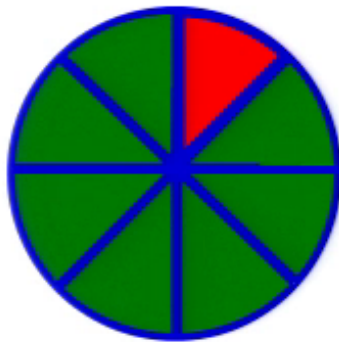


- Stage 1: adding new blocks
- Stage 2: Cyclic updates

Algorithm: Summary

- Nassau

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- Stage 1: adding new blocks
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Results

- Compression ratio in % of the original description length
 - ▶ smaller numbers mean better compression

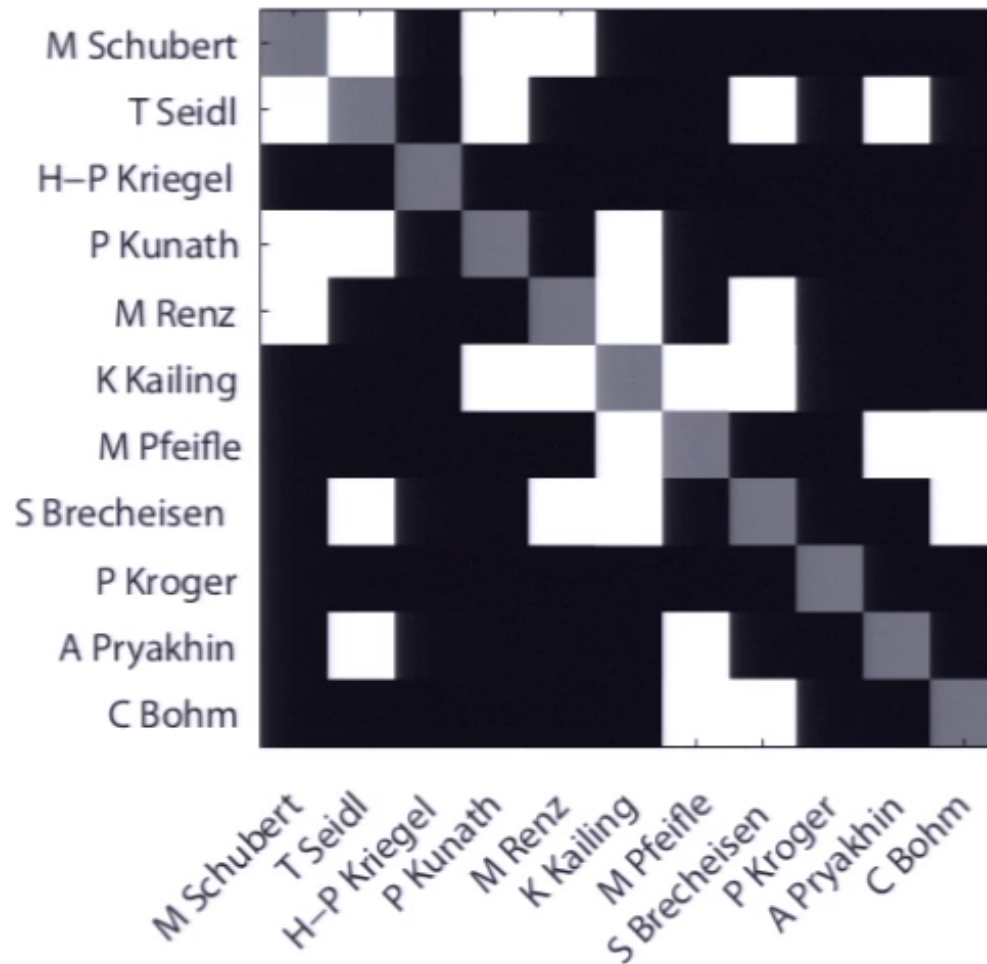
| Dataset | Nassau | | Panda+ ¹ | | Asso ² | |
|----------------------|-------------|----------|---------------------|----------|-------------------|----------|
| | <i>L%</i> | <i>k</i> | <i>L%</i> | <i>k</i> | <i>L%</i> | <i>k</i> |
| <i>4News</i> | 93.1 | 12 | 92.7 | 5 | 93.6 | 17 |
| <i>DBLP co-auth.</i> | 94.1 | 60 | 95.9 | 11 | 95.8 | 178 |
| <i>Dialect</i> | 42.0 | 30 | 57.3 | 17 | 48.8 | 37 |
| <i>DNA Amp.</i> | 43.6 | 100 | 63.4 | 20 | 49.8 | 58 |
| <i>Mammals</i> | 54.5 | 29 | 66.8 | 8 | 64.6 | 17 |
| <i>Mushroom</i> | 72.6 | 4 | 63.6 | 15 | 50.6 | 59 |
| <i>Paleo</i> | 89.7 | 15 | 91.2 | 3 | 91.4 | 19 |

¹C. Lucchese, S. Orlando, and R. Perego. A unifying framework for mining approximate top-k binary patterns. 2014

²P. Miettinen, T. Mielikäinen, A. Gionis, G. Das, and H. Mannila. The discrete basis problem. 2008

DBLP

- Example submatrices of *DBLP-coauth* selected by Nassau
- size 2345-by-2345, 60 factors



European Mammals

- Distribution of European mammals across different locations
- Pictured are the first four factors obtained by algorithms
- size 2670-by-194, 29 factors found

